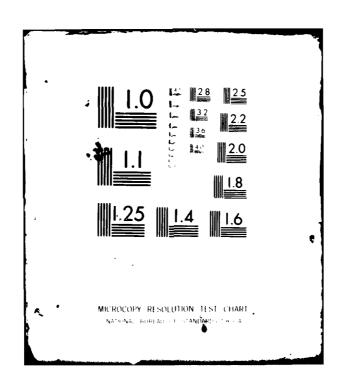
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Optical power spectralanalysis for machine-readablefactor maps

Robert D. Leighty

DECEMBER 1980



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U.S. ARMY CORPS OF ENGINEERS
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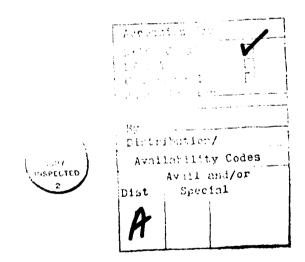
#### **PREFACE**

This study was conducted under DA Project 4A161102B52C, Task S2. Work Unit 0007, "Optical Power Spectral Analysis for Pattern Recognition."

The author wishes to express his appreciation to Mr. David Rall and Mrs. Rosalinda Barron for their assistance in the preparation of the illustrations for this report.

The study was done during the period October 1977 to September 1978 under the general supervision of Mr. Melvin Crowell, Jr., Director, Research Institute.

COL Philip R. Hoge, CE and LTC William T. Stockhausen, CE were Commanders and Directors and Mr. Robert P. Macchia was Technical Director of the Engineer Topographic Laboratories during the study period.



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# OPTICAL POWER SPECTRAL ANALYSIS FOR MACHINE-READABLE FACTOR MAPS

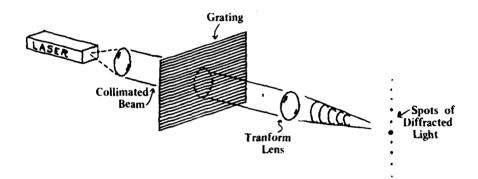
#### I. INTRODUCTION

A preliminary investigation of the application of Optical Power Spectral Analysis (OPSA) approaches to machine-readable factor maps for use in terrain information systems is presented. The objective is to offer a more compact, simpler, and cheaper data base storage and retrieval system than would be available by all-digital technology. In the basic concept of the systems, OPSA is used to decode data from reduced factor maps that have been encoded by spatial frequency and direction of optical gratings.

Alternative concepts to high-priced, large volume, and relatively slow digital mass storage systems for operation in the field are few. For this reason, a preliminary study of the application of OPSA was conducted in depth. The basic concept of optical coding and OPSA decoding of terrain factor maps is presented in Chapter 2. Chapter 3 contains an analytical characterization of the OPSA sampling system and its use in detection of Ronchi gratings. Chapter 4 presents a digital simulation program and simulation results from its use under a range of operational parameters. The preliminary design of an optical subsystem for detection of grating maps is developed in Chapter 5 to show how the interaction of parameters forces the designer to make trade-offs for realistic optical system specification. In Chapter 6 the technology for producing grating maps is reviewed and approaches for extending capabilities to produce gratings with increased storage capacity are outlined. Chapter 7 outlines more general system concepts which integrate optical, electronic, digital, and storage and retrieval subsystems and an example of a grating detection system is described to illustrate subsystem interactions. Chapter 8 presents the conclusions.

#### II. BASIC CONCEPT

If we insert a uniform grating in a collimated coherent light beam, as in figure 1, at the back focal plane of the transform lens, we will detect a number of collinear light spots. The spacing of the light spots will be determined by the grating frequency and type of grating, with the intensity of the spots related to the type of grating. The orientation of the line of spots will be perpendicular to the direction of the linear grating. If we change the grating, the spots will change accordingly in the back focal plane of the lens.



Note: This Uniform grating is illuminated by a collimated coherent light beam that results in collinear diffraction spots in the back focal plane of the transform lens.

FIGURE 1. A Uniform Grating.

Knowing the type of grating employed in the optical system, we can determine without error the grating frequency and orientation by taking a few simple measurements on the light spots.

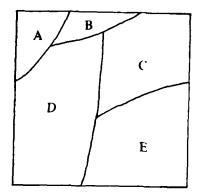
Now consider a simplified attribute map as shown in figure 2, wherein each bounded area is a two-dimensional representation of a range of one or more properties coded by an alphanumeric character. Decoding is accomplished by reading the description associated with the character code in the map's legend. Within each area having the same character code, the properties are expected to have the same range of values, and discontinuities occur only at boundary lines between coded areas. The example of an attribute map in Military Geographic Intelligence (MGI) is, of course, the terrain factor map where separate maps code surface configuration, surface composition, vegetation, etc.

#### \*\*\*

Instead of a alphanumeric character codes, we can use grating codes as shown in figure 2 with the boundaries retained. The code symbols are now a two-tuple  $(w, \phi)$ , with w representing an element or the discrete set of spatial frequencies,  $w \in w$ , and  $\phi$  representing an element of the discrete set of grating directions,  $\phi \in \theta$ .

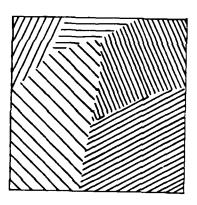
The grating map of figure 2 can be a film transparency with the grating lines having a high optical density and the space between the grating lines having a low optical density. If the optical grating map is placed in the optical power spectrum sampling system shown at the top of figure 3, that part of the grating illuminated by the collimated coherent light beam passing the sampling aperture will result in spots of diffracted light, as indicated in figure 1. When a Recording Optical Spectrum Analyzer (ROSA) detector that has 32 ring detector elements and 32 wedge detector elements with (see figure 3) each element providing an electrical output signal is centered on the optical axis in the back focal plane of the transform lens, the diffracted light spots from any grating will result in a set of detected signals for those elements so illuminated.

The remainder of this report will show that the grating codes can be optimally designed so that when they are encoded in an optical grating map and used in a properly designed optical system the result is several hundred unique coding classes for each map sheet. Each possible pair vector has a unique address in a computer lookup table.



ATTRIBUTE MAP
Legend:

A \_\_\_\_\_\_
B \_\_\_\_
C \_\_\_\_
D \_\_\_\_
E \_\_\_\_



GRATING MAP
Legend:

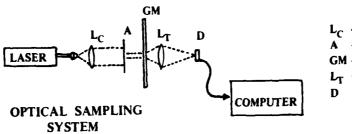
VIIII

Legend:

Le

Note: The attribute map is coded with alphanumeric characters and the grating map—has attributes coded with gratings of different spatial frequency and direction.

FIGURE 2. An Attribute Map and a Grating Map.



L<sub>C</sub> - Collimating Lens

A - Sampling Aperture

GM - Grating Map

L<sub>T</sub> - Transform Lens

D - Detector



# DETECTOR:

32 Ring Detectors

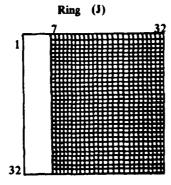
32 Wedge Detectors

Ring Detectors Provide Spatial Frequency Data

Wedge Detectors Provide Directional Data

# COMPUTER LOOK-UP TABLE

$$C(I,J)$$
  $I = 1,32$   $J = 7,32$ 



 $32 \times 26 = 832$  coding classes

FIGURE 3. Optical Power Spectrum Sampling System Employing a ROSA Detector for Sampling Grating Maps.

#### III. ANALYTICAL CHARACTERIZATION

In this chapter the analytical characterization of ROSA and the theoretical aspects of OPSA as applied to optical gratings and their detection will be discussed. This material will serve as a background for subsequent discussions involving a computer simulation program that will demonstrate grating discrimination potential with ROSA systems and involving the design of grating detection systems. The ROSA system hardware has been previously reported,<sup>1</sup> and the system's use for automated pattern recognition research is documented in several publications.<sup>2</sup>,<sup>3</sup>,<sup>4</sup>

The approach used here should not be considered rigorous, but rather more intuitive so as to provide a reader without a background in OPSA with enough foundation to understand the relation of the design variables and the nature of the trade-offs to achieve a useful operational system.

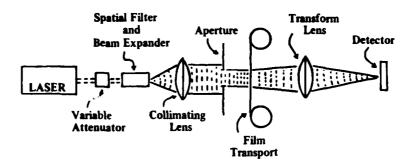
A. ROSA Characterization • The three ROSA subsystems are indicated in figure 4. Here we will be concerned with the signals produced by optical sampling and the nature of the electronic signal processing in the ROSA system. The signal flow and analytical characterization of the optical and electronic signal processing within the ROSA is summarized in figure 5. We will now develop the expressions shown in this illustration.

<sup>&</sup>lt;sup>1</sup>R. D. Leighty, Optical Power Spectrum Analysis (OPSA) (Report No. 1, Recording Optical Spectrum Analyzer System Hardware), U. S. Army Engineer Topographic Laboratories, Fort Belvoir, VA, Report ETL-TR-74-11, May 1975, AD-A016 131.

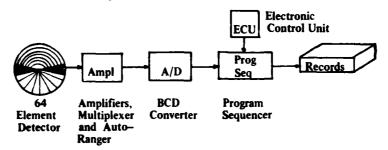
<sup>&</sup>lt;sup>2</sup>R. D. Leighty, and G. F. Lukes, "Cloud Screening From Aerial Photography," Proc. 40th Annual Meeting ASP/ACSM, St. Louis, MO, 1974, pp 309-332.

<sup>&</sup>lt;sup>3</sup>G. F. Lukes, "Cloud Screening from Aerial Photography Applying Coherent Optical Pattern Recognition Techniques," Proc. SPIE, Coherent Optics in Mapping, Vol. 45, 1974, pp 265-272.

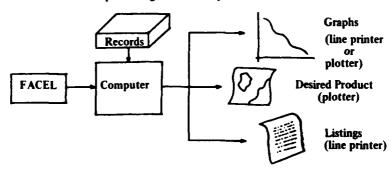
<sup>4</sup>G. E. Lukes, "Rapid Screening of Aerial Photography by OPS Analysis," Proc. SPIE. Data Extraction From Film, Vol. 117, 1977, pp 89-97.



#### A. Coherent optical system configuration

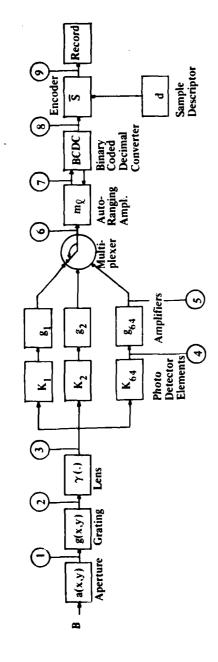


#### B. Electronic processing and record system



#### C. Software processing and output

FIGURE 4. ROSA Subsystems.



() a (x, y)

(2) a(x, y) g(x, y) = h(x,y)

$$\begin{cases} \left\{ z_{n} \right\}_{n=1.64} \\ \left\{ \left\{ m_{\chi} z_{n} \right\}_{\chi=0.3} = \left\{ z_{n} \right\}, n=1.64 \\ 0 \end{cases}$$

(3) 
$$\int \int h(x,y) \exp \left[ \int (xu + yv) / (f\lambda) \right] dxdy = H(u,v)$$
 (8)  $\{ (z_n/10^{\ell}, 3 - \ell)_m \} = \{s_n\}, \ \ell = 0.3, \ n = 1.64$ 

(9) 
$$\{d, \{s_j\}_{j=1.8}$$

(5) 
$$K_n g_n \int \int (...) \rho d\rho d\theta = z_n$$

(4)  $K_n \int_{\rho} \int_{\theta} |H(\rho, \theta)|^2 \rho d\rho d\theta$ , n = 1.64

FIGURE 5. Analytical Characterization of ROSA Optical and Electronic Processing.

The circular sampling aperture a(x, y) of radius r is centered on the optical axis. When illuminated by normally incident coherent plane waves of amplitude B and wavelength  $\lambda$ , the aperture has a transmission function

$$a(x,y) = \begin{cases} B, & \text{if } \sqrt{x^2 + y^2} \leq r \\ 0, & \text{otherwise} \end{cases}$$
 (1)

The light from the aperture is then modulated and diffracted by the transmission function g(x, y) of the grating transparency to yield h(x,y), such that

$$h(x, y) = a(x, y) g(x, y)$$
 (2)

The diffraction-limited, transform lens of focal length f and diameter,  $D_1$ , where  $D_1 >> r$ , then images the Fraunhofer diffraction pattern of h(x,y) in its back focal plane. This process is equivalent to a two-dimensional Fourier transformation F (h (x, y)) except for a constant phase factor, which has no effect upon the results. Thus,

$$F(h(x, y)) = H(u, v) = \frac{1}{\lambda f} \iint_{x,y} a(x, y) g(x, y)$$
 (3)

$$\exp \left[-j2\pi \left(xu + yv\right)/(\lambda t)\right] dxdy$$

where (u, v) represents space coordinates in the detector or focal plane. To express H(u, v) in terms of spacial frequencies  $w_u$  and  $w_v$ , use

$$w_u = \frac{u}{\lambda f}$$
 and  $w_v = \frac{v}{\lambda f}$  (4)

Thus,  $H(u/\lambda f, v/\lambda f) = H(w_u, w_v)$ .

The detector is responsive only to light intensity, and the intensity distribution at the photo detector is equivalent to the squared modulus of the light amplitude, or

$$T(u, v) = |H(u, v)|^2$$
 (5)

Now consider each of the n = 1,64 photo detector elements to have response  $K_n$  for incident light energy. The signal for any detector element is then a function of the element surface area and the responsivity of the material. At this point, u and v can be expressed in polar coordinates, where  $\phi = \sqrt{u^2 + v^2}$  and  $\theta = \tan^{-1}(v/u)$ . Therefore, the signal from any detector element is

$$K_{n} \int_{\rho_{n}} \int_{\theta_{n}} |H(\rho, \theta)|^{2} \rho d\rho d\theta, n = 1, 64$$
 (6)

where  $\rho_n$  and  $\theta_n$  represent both the lower and upper limits for each element considered in the integral.

Each of the signals next passes through two amplifier stages, the first has constant gain  $g_n^a$  with adjustable bias  $c_n^a$ , and the second has variable gain  $g_n^b$  with an adjustable bias  $c_n^b$ . The net amplification being

$$g_n = (g_n^a - w_n^a) + J_n^b$$
 (7)

Signals  $z_n$  at the output of these amplifier was then

$$z_n = g_n K_n \int_{\rho_n}^{\infty} \int_{\theta_n}^{\infty} \operatorname{erf}(\rho, \theta) |^2 \rho d\rho d\theta \qquad (8)$$

The multiplexer steps through each of the n channels to form the set  $[z_n]$ , n=1,64. Next, the signals pass to an autoranging amplifier linked to a binary-coded decimal converter. The amplifier has four gains  $m_p$ , p=0,3, determined by the position of the most significant digit in the converter. Final output of the amplifier is then

$$\{m_p, z_n\}$$
  $p = 0, 3 = q_n, n = 1, 64$  (9)

where

$$m_{p} = \begin{cases} m_{0} = 2 \times 10^{0}, & \text{if } 10^{4} < z_{n} < 10^{5} \\ m_{1} = 2 \times 10^{1}, & \text{if } 10^{3} < z_{n} < 10^{4} \\ m_{2} = 2 \times 10^{2}, & \text{if } 10^{2} < z_{n} \le 10^{3} \\ m_{3} = 2 \times 10^{3}, & \text{if } z_{n} \le 10^{2} \end{cases}$$
(10)

and output from the converter is then the three most significant digits and the decimal characteristic. Thus,

$${S_n} = (q_n / 10^p, 3-p), p = 0, 3, n = 1, 64$$
 (11)

The encoder then reformats  $\{s_n\}$  into eight groups of numbers for recording, along with a six-digit decimal sample descriptor number d input by the operator from the control unit and card number i = 1, 8. The output data is then a set of eight card images

$$\{S\}_{i} = \{d, \{S_{i}\}_{i=1,8}, i\}_{i=1,8}$$
 (12)

from which the sample vector  $\overline{S} = \{s_n\}$ , n = 1, 64 is available for the computer pattern recognition efforts.

Establishing an optimum set of values for the optical and electronic parameters, i.e. aperture diameter, transform lens focal length, amplifier gains, etc., to obtain the best sample vector  $\overline{S}$  for the grating patterns to be investigated is dependent on knowledge of the effects on the output data owing to variables in the analytical expressions just discussed. This point is aptly illustrated when reviewing the optical power spectrum analysis literature to find that authors do not recognize the effects of the sampling aperture on the output data. In equation (3), the sampling aperture a(x, y) is assumed to have a spatially uniform or constant value in a finite area. It is this finite area that sets the integration limits with the result that equation (3) is termed the superposition integral, which reflects spatial frequency domain convolution. If a(x, y) and g(x, y) have respectively the Fourier transforms A(u, v), and G(u, v), then equation (3) can be expressed in the spatial frequency domain by

$$H(u, v) = \frac{1}{\lambda f} A(u, v) ** G(u, v)$$
 (13)

where the double astrisk symbolizes the two-dimensional convolution operation, which in integral form is

$$H(u, v) = \frac{1}{\lambda f} \int \int A(\alpha - u, \beta - v) G(u, v) d\alpha d\beta$$
 (14)

Thus, A(u, v) is convolved with G(u, v) having a smoothing effect, and the amount of smoothing is inversely related to the aperture diameter.

Aperture effects on detection of gratings are of considerable importance for our problem. Therefore, we will provide many illustrations related to diffraction patterns resulting from circular apertures. These illustrations and their underlying concepts will be referenced frequently in the following discussions.  $A(\rho)$  is represented by the first-order Bessel function, often referred to as the Airy function. Hereafter, this will be referred to as the Bessel function. Thus

$$A(\rho) = \beta \pi \frac{D^2}{4} \left[ \frac{2J_1 (\pi \rho D/\lambda f)}{(\pi \rho D/\lambda f)} \right]$$
 (15)

where  $\rho$  is the spatial frequency variable and D is the sampling aperture diameter. In figure 6, the amplitude distribution for circular aperture diffraction patterns is shown for two values for aperture diameter, and associated with each of these patterns are three values of transform lens focal length. The intensity pattern of  $A(\rho)$ ,

$$A(\rho)^{2} = \frac{B^{2}\pi^{2}D^{4}}{16} \left[ \frac{2J_{1}(\pi\rho D/\lambda t)}{(\pi\rho D/\lambda t)} \right]^{2}$$
 (16)

is pictured in figure 7 for an aperture of arbitary diameter. In figure 8, the relation of the intensity function to the amplitude function without weighting is indicated. Note that the intensity function is definitely positive. If we plot the intensity function semilogarithmically as in figure 9, this presentation will clearly depict the intensity function's relation to the logarithmic exposure response of a photographic emulsion as shown in figure 7. If the aperture diameter is decreased, the rings in figure 7 would be further spaced as shown in figure 6, indicating a higher degree of spatial smoothing in equation (14). This spacing is significant when small aperture diameters are required to sample the grating maps so as to retain the boundary definition within some tolerable minimum effective ground-sampling diameter. The scaling effects for five small sampling apertures and two different transform lens focal lengths are shown in table 1. Note the decrease in the first zero crossing (point 2) with increasing aperture diameter. In figure 10 is shown the fraction of the total energy contained within circles of prescribed radii in the diffraction pattern of a circular aperture. Approximately 84 percent of the energy lies within the central lobe of the Bessel function. Therefore, to minimize smoothing effects, this first zero crossing must be as small as possible, i.e. the diameter of the sampling aperture must be as large as possible. Also, note that the amplitude values for the maximums and minimums of the Bessel functions in table 1 have not been scaled for aperture area according to equation (15).

From equation (3) the effect of the lens focal length f and the monochromatic wavelength  $\lambda$  will inversely affect the amplitude of the output as well as the scale of the presentation on the detector.

The optical power spectrum has polar symmetry as indicated in equation (5) since I(u, v) = I(-u, -v). This redundancy allows use of the ring and wedge geometry in design of the ROSA detector without any lost of information.

Detector element responses  $K_n$  are a function of the respective receptive areas as well as the element's responsivity. Thus, all wedges, being of the same area, are expected to have the same response for a given constant responsivity; whereas, the responses for rings will increase with radius from the center. If the second stage amplifier gain  $g_n^b$  in (7) is adjusted so that

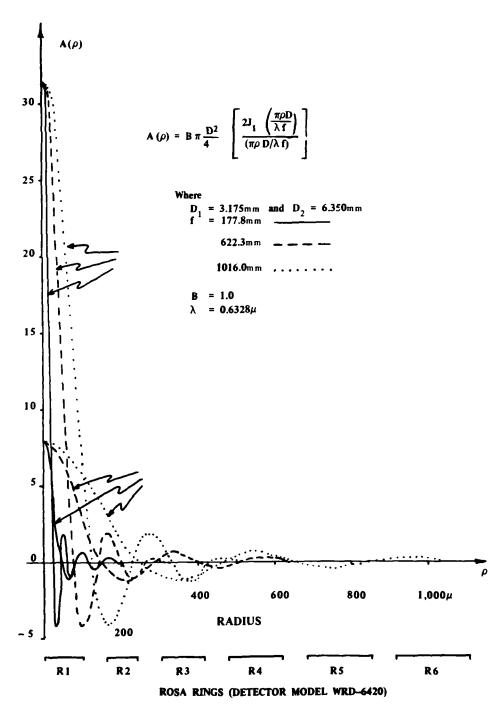


FIGURE 6. Amplitude of Circular Aperture Diffraction Patterns.

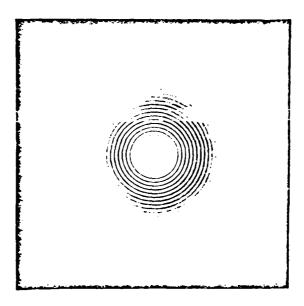


FIGURE 7. Optical Power Spectrum of a Circular Aperture.

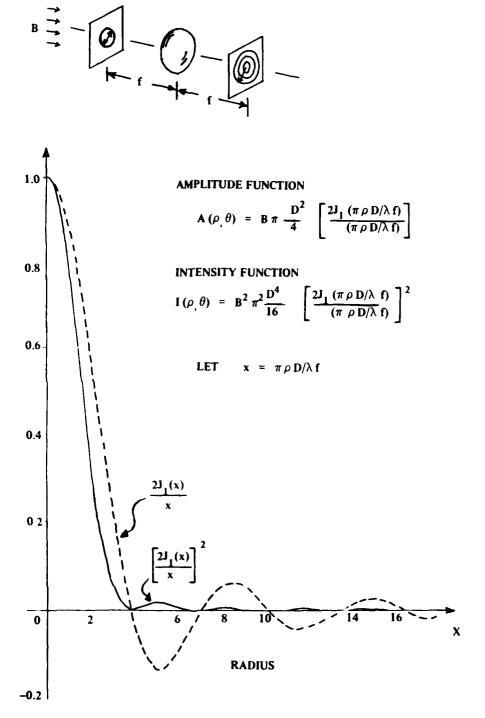
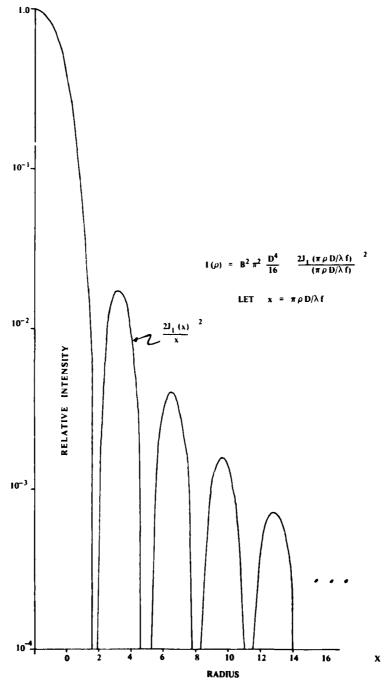


FIGURE 8. Diffraction From a Circular Aperture.



**FIGURE 9.** Log-Linear Plot of Relative Intensity of a Circular Aperture Diffraction Pattern.

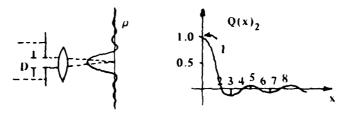


 TABLE
 1. Aperture-Diameter Scaling of Bessel Function.

LET		WHERE
Q(x) =	$\frac{2I_{1}(\pi \rho D/\lambda f)}{(\pi \rho D/\lambda f)}$	$x = \pi \rho D/\lambda f$ $\rho = \frac{x \lambda f}{\pi D} \text{ and if } C_i = X_i/\pi$ Then $\rho = C_i \frac{\lambda f}{D}$

# DISTANCE FROM OPTICAL AXIS, $\rho$ in mm.

DISTANCE FROM OPTICAL AXIS, $\rho$ in mm.								
	$t = 177.8 \text{ mm}, \qquad \lambda = 0.6325 \text{ x } 10^{-3} \text{mm}$							
		AP	ERTURE	DIAMET	ER, D in	mm.		
i	$C_{i}$	Q(x)	0.075	0.10	0.25	0.50	0.75	1.00
١	0.0	+1.000	0	0	0	0	0	0
2	1.220	0	1.830	1.373	0.549	0.275	0.183	0.137
1 2 3	1.635	-0.1323	2.453	1.870	0.734	0.368	0.245	0.187
4	2.233	0	3.350	2.512	1.005	0.502	0.335	0.251
5	2.679	+0.0648	4.019	3.014	1.206	0.603	0.402	0.301
6	3.238	0	4.858	3.643	1.457	0.729	0.486	0.364
7	3,699	-0.0400	5.549	4.162	1.665	0.832	0.555	0.416
8	4.241	0	6.362	4.772	1.909	0.954	0.636	0.477
							1	
	f				= 0.63		mm	
		AP	ERTURE	DIAMET	ER, D in	mm.		
i	$C_{i}$	Q(x)	0.075	0.10	0.25	0.50	0.75	1.00
ı	0.0	+1.000	0	0	0	0	0	0
2	1.220	0	1.029	0.772	0.309		0.103	0.077
3		-0.1323	1.380	1.035	0.414	0.207	0.138	0.104
4	2,233	0	1.884	1.413	0.565		0.188	0.141
5	2.679			1.695	0.678		0.226	0.170
6	3.238	0	2.732	2.049	0.820	0.410	0.273	0.205
7		-0.0400		2.341	0.936		0.312	0.234
8	4.241	0	3.578	2.683	1.073		0.358	0.268

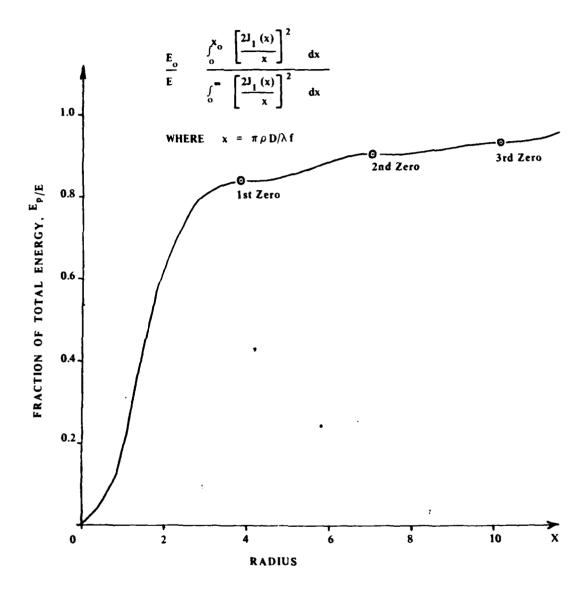


FIGURE 10. Fraction of the Total Energy Contained Within Circles of Prescribed Radii in the Diffraction Pattern of a Circular Aperture.

$$|g_n^a + c_n^a| = |g_n^b + c_n^b|$$
 (17)

then the responsivity differences of detector elements is ignored. Although if  $g_n$  = constant, i.e. if the outputs from all second-stage amplifiers are equal, then detector element areas are normalized. However, the flexibility exists with software to adjust data for desired area response; thus, the former approach is generally used in practice.

B. Gratings in OPS Systems • A transmission grating will be defined as a one-dimensional repeating optical transmission function. For example,

$$g(x, y) = g(x) = A \cos(2\pi x/p)$$
 (18)

is a cosine function of amplitude A in the x-direction that repeats every p units of x, and the value of the function at any point x is the same for all values of y. The spatial frequency of a grating in line pairs per millimeter (mm) is the reciprocal of the grating period in millimeters, i.e.

$$w = 1/p \tag{19}$$

The Fourier transform of g(x) is G(w), which will be symbolized as shown in equation (3), i.e. F[g(x)] = G(w). As in equation (18) where the grating can be expressed in one dimension, it is frequently advantageous to present expressions as F[g(x,y) = g(x)] = G(u, o)  $G(p, \theta)$ , where p is a radial distance and  $\theta$  is a direction angle. Since the grating transform for a specific grating will have  $\theta = a$  constant, we can then talk in general of  $G(p, \theta_1) = G(p)$ . By equation (4), we have  $w = p/\lambda f$ , thus  $G(p/\lambda f) = G(w)$ .

As shown in figure 11, the Fourier transform for a cosine grating is equal to two delta functions,  $\delta(w \pm 1/p)$ , with amplitudes of A/2 positioned at  $\pm 1/p$  in the spatial frequency presentation. This results from the equality

$$\cos (w_0 x) = \frac{e^{jw_0 x} + e^{-jw_0 x}}{2}, j^2 = -1$$

and since  $F[e^{jw_0x}] = \delta$  (w-w<sub>0</sub>), where w<sub>0</sub> = 1/p in 1p/mm, we have for equation (18)

$$F[A\cos(2\pi x/p)] = A/2[\delta(w-1/p) + \delta(w+1/p)]$$
 (20)

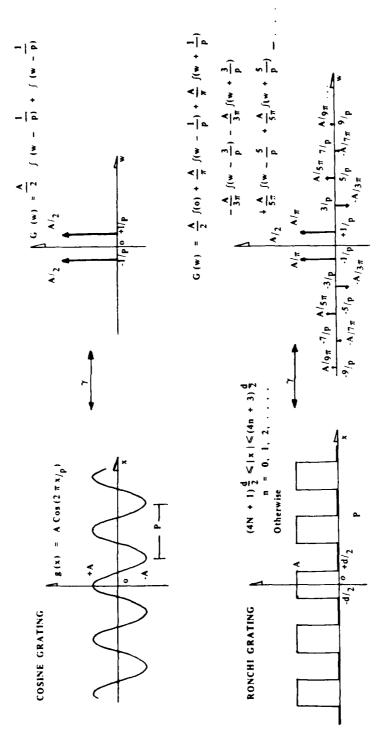


FIGURE 11. Cosine and Ronchi Grating Functions and Their Amplitude Fourier Transform Spatial Frequency Spectrums.

A few words about delta functions is necessary. A delta function  $\delta$  (t), also known as a unit impulse function, may be defined in many ways. Here the following definition will be used:

$$\delta(t) = \begin{cases} 0, & \text{if } t = 0 \\ \infty, & \text{if } t = 0 \end{cases}$$

$$\int_{-\infty}^{\infty} \delta(t) dt = \int_{-\epsilon}^{\epsilon} \delta(t) dt = 1, \epsilon > 0$$
(21)

The first relation indicates that  $\delta$  (t) is zero except at t = 0, where it becomes infinite in such a way that the second relation is satisfied. Delta functions have many useful mathematical properties, which we will only reveal as needed to clarify the concepts under discussion.

Delta functions in optics are point sources of light; and since the cosine grating has only two delta functions, each of which has infinite resolution in the frequency domain, it would appear that this grating would be ideal for OPSA applications such as we are investigating. Indeed, if we had means for fabricating cosine gratings of selected spatial frequencies with the desired spatial boundary conditions, it would be ideal: unfortunately we do not.

A square wave grating would be much simpler to realize, except that we cannot obtain negative light values with optical transparencies. We can however use a 'Ronchi' grating, which is a square wave grating with a positive A/2 bias.

Another unique characteristic of a Ronchi grating is that the grating width, d, is one-half of the grating period, p. The disadvantage of using Ronchi gratings instead of cosine gratings is that harmonic delta functions are found in the Fourier transform, as shown in figure 11. These harmonics decrease in amplitude with increasing spatial frequency and alternate plus and minus in amplitude. To obtain the functional expression for Ronchi grating transforms, we use the Fourier series representation for a square wavetrain with a constant bias. Using the Fourier series results in an infinite number of coefficients. An infinite number of cosine waves are required to realize perfect square waves, but if we select the first n coefficients, where n is a modest number, we can transform each Fourier series term and the result is that each Fourier series term has its unique delta function in the spatial frequency domain.

By using Ronchi gratings, we trade simplicity of grating fabrication for complexity in detection of the grating transforms. We will show that the detection of ideal Ronchi gratings can be made at sufficiently high signal-to-noise ratios to yield unique signals for OPSA applications.

C. Grating and Aperture Transform Convolution. • Equation (14) is the convolution integral for a general signal function, G (u, v), and a general aperture function, A (u, v). In this section we will be more specific and use grating functions and small circular sampling aperture functions. The objective is to indicate the nature of the resulting function indicated by equation (14) when parameter values of the aperture and grating function are varied.

To introduce the concepts with minimum complexity, we will first assume that a cosine grating is illuminated by a collimated, coherent light beam passing through a circular sampling aperture. We will rewrite equation (14) in one-dimensional form as

$$H(w) = \frac{1}{\lambda f} \int_{-\infty}^{\infty} A(a) G(w-a) da$$

Now substitute equations (15) and (20)

$$H(w) = \frac{1}{\lambda t} \int_{-\infty}^{\infty} \frac{D^2}{4} \frac{2J_1(\pi aD/\lambda t)}{(\pi aD/\lambda t)} \frac{A}{2} \left[\delta(w-1/p-a) + \delta(w+1/p-a)\right] da$$

With the relation,

$$F(w) * \delta(w - w_0) = \int_{-\infty}^{\infty} (a - w_0) F(a) da = F(w_0)$$

Then.

$$H(w) = \frac{1}{\lambda f} - \frac{AB\pi D^2}{8} \left[ \frac{2J_1(\pi(w-1/p)D/\lambda f)}{(\pi(w-1/p)D/\lambda f)} + \frac{2J_1(\pi(w+1/p)D/\lambda f)}{(\pi(w+1/p)D/\lambda f)} \right] (22)$$

Expression (22) tells us that convolving an optical cosine grating transform with the first-order Bessel function, which is the transform of the aperture function, is equivalent to creating two new first-order Bessel functions with one positioned at the spatial frequency 1/p, and the other at -1/p. The Bessel functions will have their same spatial frequency distribution as that of the aperture function, but will be scaled by a factor of one-half in amplitude. Another important revelation of expression (22) is the potential for significant interaction between the two Bessel functions resulting from the convolution. We have seen from figure 6 and table 1 how the Bessel function is scaled in spatial frequency inversely with the diameter of the sampling aperture. Then, for very small sampling apertures and low spatial frequency gratings, one could expect to have overlapping Bessel functions that add algebraically to yield a net amplitude spectrum somewhat different than that of the individual Bessel functions. We will show examples of these implications in the simulations to follow.

Using the results of expression (22) as a guide, we can easily extrapolate to a simple expression for an ideal Ronchi grating illuminated by collimated, coherent light passing through a circular sampling aperture. The major differences between the expressions that result from the differences between the cosine transform function and the Ronchi grating transform function are as indicated earlier, and as shown in figure 11. The infinite expression for Ronchi grating convolution is then more complicated in appearance and is given by

$$H(w) = \frac{B\pi D^{2}}{4\lambda f} \frac{A}{2} \frac{2J_{1}(\pi wD/\lambda f)}{(\pi wD/\lambda f)} + \frac{A}{\pi} \frac{2J_{1}(\pi (w-1/p)D/\lambda f)}{(\pi (w-1/p)D/\lambda f)} + \frac{A}{\pi} \frac{2J_{1}(\pi (w-1/p)D/\lambda f)}{(\pi (w-1/p)D/\lambda f)} - \frac{A}{3\pi} \frac{2J_{1}(\pi (w-3/p)D/\lambda f)}{(\pi (w-3/p)D/\lambda f)} - \frac{A}{3\pi} \frac{2J_{1}(\pi (w+3/p)D/\lambda f)}{(\pi (w+3/p)D/\lambda f)} + \dots$$
(23)

This convolution is indicated in figure 12. Note the net amplitude spectrum resulting from the individual overlapping Bessel amplitude spectra. Since only the intensity spectrum is detectable, the bottom of figure 12 shows the intensity spectrum to be the magnitude squared of the net amplitude spectrum, as indicated in equation (6). Thus,

$$I(w) = |H(w)|^2$$
 (24)

To understand the intensity function of equation (24) in terms of the individual Bessel function in equation (23), we will generalize (23) to

$$H(w) = K [A_1J(w) + A_2J(w+w_1) + A_2J(w-w_1) - A_3J(w+3w_1) - A_3J(w-3w_1) + ...] (25)$$

The first term within the parenthesis is a Bessel function centered on the optical axis, the second and third terms represent the positive and negative first harmonics, respectively, and the fourth and fifth terms represent the positive and negative third harmonics. Higher order terms have been omitted from equation (25).

When (25) is squared, as in (24), interaction terms result.

$$H^{2}(w) = K^{2} [A_{1}^{2}J^{2}(w) + A_{2}^{2}J^{2}(w + w_{1}) + A_{2}^{2}J^{2}(w - w_{1}) - A_{3}^{2}J^{2}(w + 3w_{1}) - A_{3}^{2}J^{2}(w + 3w_{1}) + .... + A_{1}A_{2}J(w)J(w + w_{1}) + A_{1}A_{2}J(w)J(w - w_{1}) - A_{1}A_{3}J(w)J(w + 3w_{1}) - A_{1}A_{3}J(w)J(w - 3w_{1}) - A_{2}A_{3}J(w + w_{1})J(w + 3w_{1}) - A_{2}A_{3}J(w - w_{1})J(w - 3w_{1}) + .... }$$
(26)

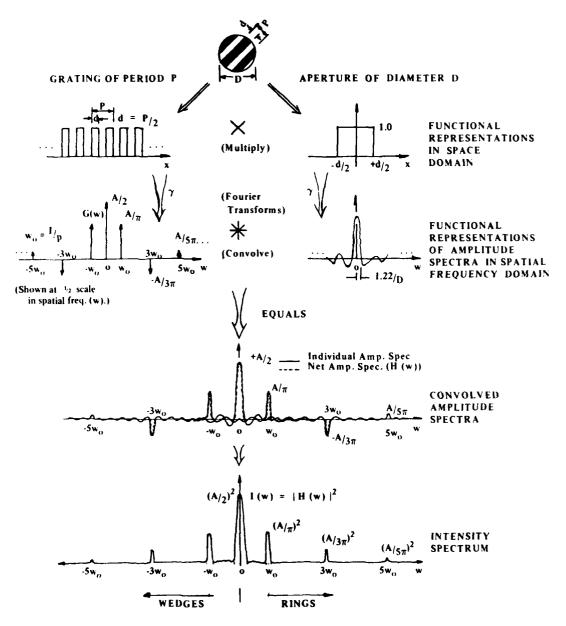


FIGURE 12. Convolving Amplitude Spectra From the Sampling Aperture and Grating to Yield a Detectable Intensity Spectrum.

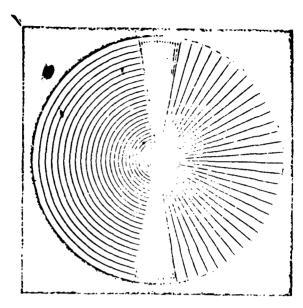
The significance of the interaction terms is dependent upon the scaling of the Bessel function, as dictated by the size of the sampling aperture and the focal length of the transform lens, and upon the positioning of the functions as determined by the Ronc' i grating frequency, w<sub>1</sub>. If the sampling aperture is large, the interaction terms will be insignificant; but when the sampling aperture is small and the grating frequency is small, then some of the interaction terms can be significant. This will be discussed later.

It should be noted that (23) implies that the Ronchi grating is a real function, i.e., has no phase components. In practice this is never fully realized, and the effects include even-order harmonics. This will be discussed subsequently.

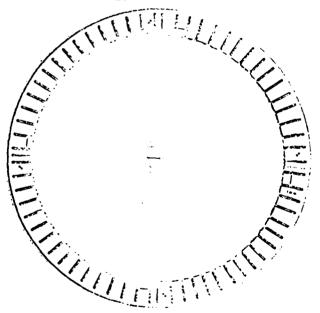
D. Geometry of ROSA Detectors. • Equation (23) indicates the nature of the amplitude signal on the detector. Here we describe the geometrical nature of ROSA detectors that will partition or sample the incident grating spectra, and the following section will discuss the sampling of grating spectra.

Two ROSA detector models are available from Recognition Systems Inc., each has 32 ring elements and 32 wedge elements; however, the detectors have some major differences. The detection of Ronchi gratings was simulated for both detectors with slightly different results that are better understood with a knowledge of the detectors and their differences.

The older detector, Model WRD-6420, has two 20° scratch wedges (usually oriented normal to the direction of roll-film travel in a manner such that emulsion scratches will not yield false diffraction signals), and the newer detector, Model WRD-6400, has no scratch wedges. The face plates of these detectors is shown in figure 13. Table 2 lists the dimensions of the ROSA Model WRD-6420 detector and table 3 presents similar data for the Model WRD-6400 detector. In both tables, the data is presented for each detector ring element. The least and maximum radius and their radial difference give the dimensions of the concentric detector rings that integrate incident energy. For each ring, the mid-radius is a key dimension in the later simulations because the gratings will be designed to have their first harmonic positioned at the mid-radius. The tables indicate the spatial frequencies associated with the mid-radii for four different focal length transform lenses. In figure 14, the relation is plotted between radial distance and spatial frequency in the back focal plane of these four lenses as given by equation (4). The remaining dimension shown in tables 2 and 3 concerns the wedge width at mid-radius. This dimension will be used to analyze grating direction detection in the simulations



a. Model WRD-6420



b. Model WRD-6400

FIGURE 13. Face Plates of Two ROSA Detectors.

TABLE 2. ROSA Detector, Model WRD-6420.

				NOTE:		Wedge detector	elements have	5.0 wedge angle,	inner radius is	I.176 mm and outer	radius is 15.3€7 mm	for all wedges.																						
			0.32	0,56	3.86	1.20	1.58	5.00	2.46	2.95	3.49	4.07	4.68	5.32	6.00	6.71	7.46	8 24	9.06	9.91	10.79	11.71	12.67	13.66	14.68	15.74	16.83	17.95	13.11	20.31	21.54	22.80	24.10	
	RESUBSICA (Mar) f (1) is one for		0.52	. 32	© ₹.	1.35	्. ज	3.26	6.4	4.82	5.70	6,65	7.64	8.59	9.79	10.96	12.17	13.45	14.79	16.18	17.62	19.12	10.69	22.30	23.97	25.69	27.47	29.31	31.21	33.16	35.16	37.22	39,34	
	MID-RING SPATIAL FREGUENCY 1900 on for 1700 on for File		:.75	3.23	4.31	6.85	9.32	11.42	14.94	16.87	19.53	23.26	26.72	30,39	34.27	39.34	42.61	47.08	51.75	56.61	61.67	66.93	72.40	78.04	83,88	99.92	96.16	102.59	109.21	116.05	123.07	130.28	137.69	
	MID f > 135.5 mm		3.22	5.74	3.72	12.17	16.04	20.31	24.97	36.01	35.45	41.36	47.52	54.05	60.94	68.17	75.76	83.71	22.02	100.62	109.66	119.01	128.73	138.76	149.13	159.88	170.97	182.41	134.20	206.34	213.82	231.64	244.80	
	Wedge Width	,	•	ı		,	1	0.112	0.138	0.166	0.196	0.228	9.262	9,238	0.336	0.376	0.418	0.462	0.508	0.556	0.605	0.657	9.711	0.756	0.823	0.883	0.944	1.007	1.672	1.139	1.208	1.279	1.351	
	Radius Difference	,	0.0747	0.1113	0.1397	97910	0.1956	5,2185	5,2438	0.2667	0.2933	9,3023	0.3251	0,3430	9,3768	0,3937	0.4141	0,4354	0.4537	3,4826	6.5023	0.5284	0.5486	0.5690	0.5913	0.6147	0.6375	0.6579	0.6807	0.7036	0.7239	0.7467	0.7671	
الب.	Maximum Radius	3,1016	0.2438	0.4131	3,6223	0.3534	1.1125	1.3945	1.7018	2.0320	2.3001	2.7636	3.1633	3.5941	4.0411	4.5115	5,0013	5.5163	6.0528	6.6116	7.1307	7,7953	8.4201	9.0653	9,7333	10.4242	11.1379	11,8720	12.6239	13,4087	14.2083	15.0317	15.3750	
MENSINGEMENTS IN HIM	Mid-Radius	,	0,2045	5.3632	0.5525	0.7696	0.0147	1.2853	1.5733	1.3337	2,2435	2.6175	3.0074	3.4201	3.8557	4.3142	4.7943	5.2972	5.3230	6.3703	6.3333	7.5311	8.1458	3.7808	3.4374	10,1169	10.8132	11.5431	12.2886	13.0569	13.3469	14,6534	15.4915	
5. 5. 2.	Least Radius	5.5	0.1651	0.3073	0.4326	3,5853	0.3163	1.1763	1.4580	1.7653	2,3363	2,4663	2.3443	3.2461	3.5703	4,1173	4,5872	5.0775	5,5931	6.1290	6.6378	7.2663	7.3715	8.4963	9.1415	9.3095	10.5004	11.2:41	11.9482	12.7051	13,4849	14.2850	15.1079	
	2 ing		. C1	m	• •	'n	9	7	or	رمي	2	-	2	ŗ.	::	5.	9	17	63	61	20	21	22	23	\$ E	25	25	27	23	53	33	31	32	

TABLE 3. ROSA Detector, Model WRD-6400.

MEASUPEMENTS 11

		MOTE:		All wedge detector	6]67675 ABJO 5.675	wedge angles, incer	radius of Aedoe.	16 and 17 is 866 mm	and all other wedges	have inner radii	of 3,544 mm. outer	radii of all wedges	are 15.900																			
- 116.5 7	•	5.28													3,14	3,56	4.33	4,56	37.3	5.35	.9.9	7.45	\$ <b>7.</b> 8	9.51	10.71	12.05	13,53	15.16	16.96	18.35	21.12	23.51
EQUENCY (**/mm) f = 622.3 mm f	•	0.46	5.71	9.36	1.22	1.43	1.76	20.5	2.37	1.71		3,52	3.33	25.	5. 5. 6.		6.1	37.7	Ģ	J. 6	.0.69	12.20	13,77	15.53	17,49	19,61	50.03	34,76	27.70	30,34	34,43	33,38
ii.	•	1.62	55.5	3,38	4.27	6	6.16	7.13		9.50	1; 33	12.32	13.36	5.33	77.34	3	8		12.6	; ; ;;	37.73			35 36	27.13	35	27,32	36,65	36.36	10.27	173,71	134,35
MIO-PING SPATIAL f s log, mr f s 177,s mm	•	2.33	· 1		7,53	9,23	35	. 7.5	4.74			8.13	~ .	: '	. T.	, e		28.35	ī.	1,33		4.	# * * * * * * * * * * * * * * * * * * *	FF, 65	5.77		11.24	154, 8	177, 36	137,51	0.50	* * * * * * * * * * * * * * * * * * * *
Wedge	,	•			•	3,057*	26.		÷.		. :		: .	<i>z</i> .		•,	••			•	:: <u>:</u>	٠.				. 52	.5.		12.			• •
Afing Angle	361.1										., :.					<i>:</i> .	· :.	:			 : .			· .	· ::			;; ;;				
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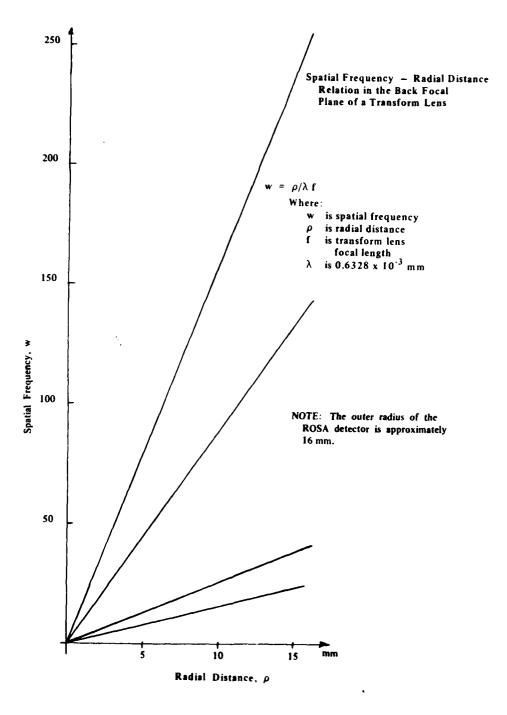
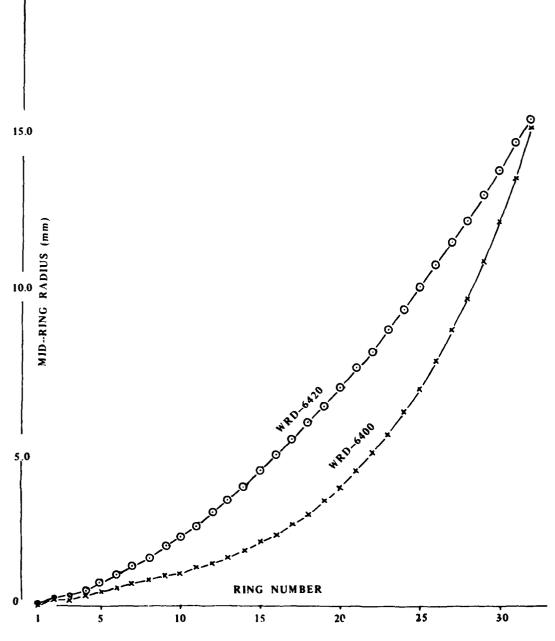


FIGURE 14. Spatial Frequency-Radial Distance Relation in the Back Focal Plane of a Transform Lens.

The wedge angles for the WRD-6420 detector are 5.000°, and the wedge angles for the WRD-6400 detector are 5.625°; therefore, the wedge widths will be different for each detector.

Note that the inner radius for WRD-6420 detector wedges is 1.176 millimeter. Therefore, only ring-wedge combinations for rings 7 through 32 are available for grating detection. For the Model WRD-6400 detector, wedges have an inner radius of 0.544 millimeter, except for wedges 16 and 17, which have an inner radius of 0.660 millimeter corresponding to rings 6 and 7 respectively. The outer radius of the wedges for Model WRD-6420 detectors is 15.367 millimeters; whereas, the maximum radius for Ring 32 is 15.875 millimeters. This will have significance in later simulations. For the WRD-6400 detector, the outer wedge radius and the maximum radius for Ring 32 are all equal to 15.900 millimeters.

In figures 15 and 16, linear and semi-log plots of the mid-radii for the two detectors are presented. In general, figure 15 indicates that the WRD-6400 detector has greater frequency domain resolution than the WRD-6420 detector up to about Ring 20 and less resolution at higher spatial frequencies. Figure 16 indicates that the rings of detector WRD-6400 are spaced logrithmically beyond Ring 6. In figures 17 and 18, linear and semi-log plots of the ring widths for the two detectors are presented. Here figure 17 shows the ring widths for the WRD-6420 detector to increase in a linear manner: whereas, those of the WRD-6400 detector are shown to be nonlinear. In the semi-log plot of figure 18, both are quasi semi-log in nature, but with different slopes.



LIGURE 15. Linear Plot of Mid-Ring Radii for Two ROSA Detectors.

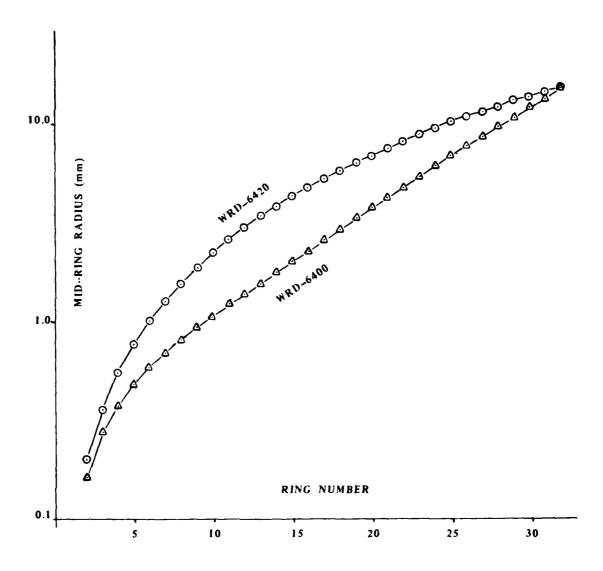


FIGURE 16. Semi-Log Plot of Mid-Ring Radii for Two ROSA Detectors.

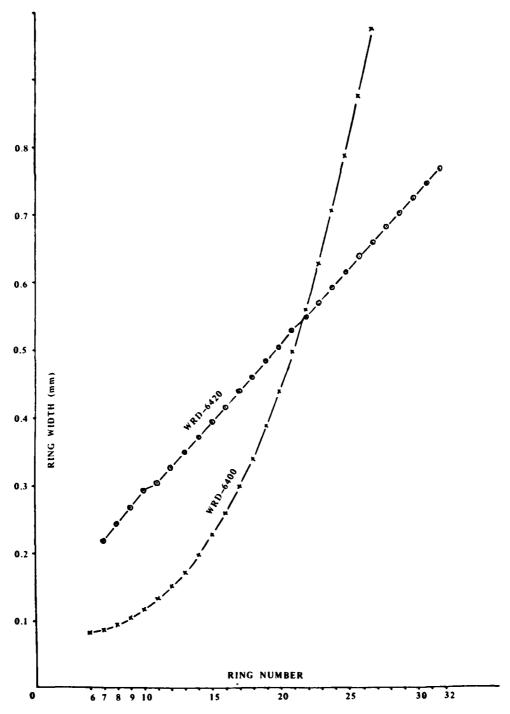


FIGURE 17. Linear Plot of Detector Ring Width for Two ROSA Detectors.

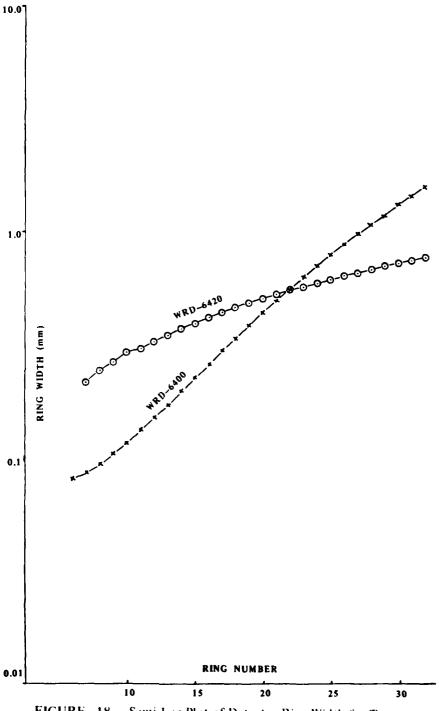


FIGURE 18. Semi-Log Plot of Detector Ring Width for Two ROSA Detector.

E. ROSA Sampling of Grating Spectra. • In the ROSA characterization section, we analytically outlined the general optical and electrical signal flow through the ROSA system. The next section introduced gratings in OPS systems, and the following section dealt with grating and aperture convolution. Then the previous section introduced the geometry of the ROSA detectors. In this section, we integrate the previous material and discuss Ronchi grating sampling with ROSA detector ring and wedge elements.

For this discussion, we assume the condition of equation (17) to be valid, i.e., the gain and bias of the amplifiers are adjusted to normalize responsivity differences of the detector elements and also normalize detector element areas. This condition implies a point source of light imaged on any detector element will yield the same output. This simplifying assumption in no way restricts the generality of the approach, as a review of the ROSA characterization section will indicate that any set of amplifier gains and biases can be used to compute any other set, if so desired.

Now, consider that each ring element of the detector has a finite width with an inner radius and outer radius and that each ring element is separated by a nonsensitive band. We can use these radii for each ring for the limits of integration in equation (6) for determining the signal from any intensity spectrum. This can be visualized by considering the one-dimensional intensity spectra at the bottom of figure 12 with the detector ring radii converted to their spatial frequency equivalents for a given scaling factor of the transform lens focal length and wavelength of light. The signal for each detector element is then proportional to the area of the curve between the ring's inner and outer radii.

We can see from figure 1 that there may be one or more Bessel functions within the area of a wedge, depending upon the spatial frequency of the Ronchi grating illuminated by the aperture. Suppose one side of the intensity spectrum in figure 12 represents the center line of a wedge; the signal for the detector wedge element can be visualized by considering the area under the curve. Depending upon the diameter of the sampling aperture and scaling by the transform lens focal length, the adjacent detector wedge elements will have detectable signal levels owing to the portions of the Bessel functions imaged onto their surfaces.

If we can uniquely fabricate ideal Ronchi rulings at 26 selected grating periods such that with a selected focal length of a transform lens a unique signal will result for each ring element of the detector between 7 and 32, and if we further have the capability of fabricating these Ronchi gratings with 5-degree differences in direction, we then have

the potential capability of encoding 832 separate types of information for the WRD-6420 detector. In the following section, we will simulate the grating detection process for both detectors to show that unique signals can be detected, even for small sampling apertures.

A few comments on the sampling at grating boundary locations in OPS systems are warranted in discussing ROSA grating sampling. Let us begin with equation (3), the basic expression for the grating illuminated by coherent light passing through a sampling aperture. Suppose the grating map g(x, y) is such that  $g(x, y) = g_1(x, y) + g_2(x, y)$ , where  $g_1(x, y)$  and  $g_2(x, y)$  are nonoverlapping, contiguous grating functions. For the moment, suppose the sampling aperture diameter is very large: therefore, the aperture convolution effects can be neglected, e.g. if D = 50.0 mm then the central lobe of the Bessel function has a diameter of 0.0055 mm, as indicated in table 1 for a transform lens focal length of 177.8 mm and a wavelength of light of 0.6328 x  $10^{-3}$  mm.

If the illumination is uniform over the aperture and the aperture is located immediately adjacent to the transparency along the optical axis, then

$$g(x, y) = c_1 g_1(x, y) + c_2 g_2(x, y)$$
 (27)

where  $c_1$  and  $c_2$  represent the percentage of the aperture illuminated by  $g_1$  (x, y) and  $g_2$  (x, y), respectively. If the respective Fourier transforms of  $g_1$  (x, y) and  $g_2$  (x, y) are  $G_1$  (u, v) and  $G_2$  (u, v), then the linearity property of the Fourier transformation indicates

$$[c_1 g_1(x,y) + c_2 g_2(x,y)] = \frac{1}{\lambda f} (c_1 G_1(\rho,\theta_1) + c_2 G_2(\rho,\theta_2))]$$
 (28)

when expressed in polar coordinates for easier visualization. In this expression, the delta functions of  $G_1$  ( $\rho$ ,  $\theta_1$ ) and  $G_2$  ( $\rho$ ,  $\theta_2$ ) are separately collinear along their respective directions of  $\theta_1$  and  $\theta_2$ . The intensity function of equation (28), however, indicates the possible existence of interaction between  $G_1$  ( $\rho$ ,  $\theta_1$ ) and  $G_2$  ( $\rho$ ,  $\theta_2$ ), as shown by

$$I(\rho, \theta) = \frac{1}{\lambda^2 f^2} + c_1 G_1(\rho, \theta_1) + c_2 G_2(\rho, \theta_2) +^2$$

$$= \frac{1}{\lambda^2 f^2} + (c_1^2 G_1^2(\rho, \theta_1) + 2c_1 G_1(\rho, \theta_1) + c_2 G_2(\rho, \theta_2) + c_2^2 G_2^2(\rho, \theta_2))$$

$$+ c_2^2 G_2^2(\rho, \theta_2)$$
(29)

When  $\theta_1$  differs from  $\theta_2$ , the interaction term concerns only the delta functions at the origin. When  $\theta_1 = \theta_2$ , there will be no additional interaction unless the periods of  $g_1(x, y)$  and  $g_2(x, y)$  are integer multiples, which as table 2 indicates is not likely with the ROSA Model WRD-6420 detector when the Ronchi gratings are properly designed.

Now, let us generalize the discussion for any sampling aperture diameter so as to consider convolution smoothing and interaction in the spatial frequency domain. Expression (28) is now rewritten as

$$\begin{bmatrix} a(x,y) & \left(c_{1} g_{1}(x,y) + c_{2} g_{2}(x,y)\right) \end{bmatrix} = \frac{1}{\lambda f} \begin{bmatrix} A(\rho,\theta) & ** & \left(c_{1} G_{1}(\rho,\theta_{1}) + c_{2} G_{2}(\rho,\theta_{2})\right) \end{bmatrix} = \frac{1}{\lambda f} \begin{bmatrix} A(\rho,\theta) & ** & c_{1} G_{1}(\rho,\theta_{1}) + A(\rho,\theta) & ** \\ c_{2} G_{2}(\rho,\theta_{2}) \end{bmatrix}$$

$$c_{2} G_{2}(\rho,\theta_{2})$$

$$(30)$$

The intensity function for equation (30) is

$$I(\rho,\theta) = \frac{1}{\lambda^{2} f^{2}} \left[ \left( A(\rho,\theta) ** c_{1} G(\rho,\theta_{1})^{\frac{1}{2}} + 2 \left( A(\rho,\theta) ** c_{1} G_{1}(\rho,\theta_{1}) \right) \right] + \left( A(\rho,\theta) ** c_{2} G_{2}(\rho,\theta_{2}) \right]^{2}$$

$$\left( A(\rho,\theta) ** c_{2} G_{2}(\rho,\theta_{2}) + \left( A(\rho,\theta) ** c_{2} G_{2}(\rho,\theta_{2}) \right)^{2} \right)^{2}$$

The first and third terms of equation (31) are additive where they overlap in  $(\rho, \theta)$  space owing to the convolution broadening. The second term produces a multiplicative function at the origin that is added to those of the first and third terms. Additionally, the multiplicative interaction of the amplitude functions in  $(\rho, \theta)$  space occurs where the functions of terms one and three overlap. Although this interaction could be considerable for very small sampling apertures, in the Systems Concepts Section a number of strategies will be discussed for uniquely determining grating frequency and direction when the sampling aperture illuminates more than one grating function.

This discussion, although being somewhat eneral in interpretation to the real world, pertains mainly to the idealized or theoretical Ronchi spectra. Real world spectra will contain even-order harmonics with amplitudes somewhat proportional to their deviation from the theoretical. The real world effect on the theoretical data will result in the potential for overlapping spectra of odd and even harmonics with an associated loss in spatial frequency discrimination.

# IV. SIMULATING OPS DETECTION OF RONCHI GRATINGS

A FORTRAN IV program, WRDET, has been prepared to simulate the concepts of the preceding section, wherein ideal Ronchi gratings of selected spatial frequencies are illuminated with collimated light passing through a circular sampling aperture. The intensity spectra derived from the convolved Fourier transforms for these two functions, i.e. the grating and the aperture functions, as given in equation (26), is then partitioned and summed for the appropriate ring and wedge elements of the ROSA detector configuration. The critical variables tested were sampling aperture diameter, Ronchi grating spatial frequency, and focal length of the transform lens.

In this Chapter, we will describe the major features of WRDET and present simulation results.

A. Program WRDET. • Program WRDET simulates detection of ideal Ronchi optical transmission gratings in an optical power spectrum analyzer using a ROSA detector. For a given transform lens focal length and diameter of the sampling aperture, the OPS intensity distributions for RONCHI gratings having spatial frequencies corresponding to mid-ring radii of the ROSA ring detector elements were partitioned according to the ROSA wedge and ring detector elements and integrated for selected wedge and ring detector elements. All calculations were accomplished for the HeNe laser light wavelength of 0.6328 micrometer ( $\mu$ m).

The discussion will follow the flow chart of the major parts of Program WRDET given in figure 19. A listing of the program is included as appendix A. Initialization of Program WRDET involves setting the values for the sampling aperture diameter, the transform lens focal length, the Ronchi grating spatial frequencies corresponding to the mid-ring radii for the selected ring detector elements, the inner and outer radii for the ring and wedge detector elements, and a list of the first four Bessel zero coefficients. An optical scaling factor for the Bessel function is computed, and this factor is used to compute the radii of the Bessel rings in the spatial frequency plane, as indicated in table 1.

The main DO loop of Program WRDET then increments through each selected grating frequency. For each selected spatial frequency, the amplitude and radial distances are computed for each delta function falling on the detector, as indicated in figures 11 and 12.

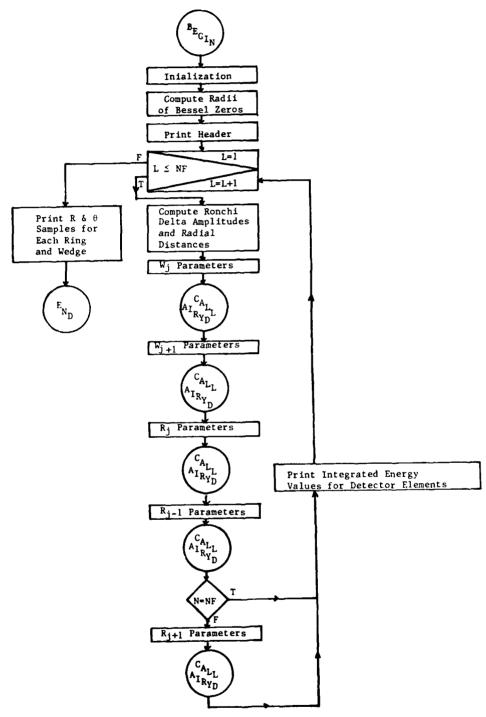


FIGURE 19. Flow Chart of the Main Components of Program WRDET.

For each mid-ring spatial frequency, the integrated OPS is computed for the selected ring  $R_j$  and its adjacent rings  $R_{j+1}$  and  $R_{j-1}$ . Similar computations are made for a wedge  $W_j$  and its neighbor  $W_{j+1}$  when the grating is oriented so that the Ronchi grating deltas are collinear along the bisector of the wedge  $W_j$ . These computations are made in Subroutine AIRYD, which is outlined in the flowchart in figure 20. This subroutine integrates the two-dimensional diffracted energy incident on a wedge or ring detector element in the spatial frequency plane by Simpson's Rule using polar coordinates. Thus, the subroutine performs the integration of equation (26) where the definite integrals have limits set by the indicated wedge or ring element.

When Subroutine AIRYD is called, the radial and angular sampling parameters are computed. Next, a table of normalized first-order Bessel amplitudes are computed for the appropriate scaling parameter, as indicated in figure 8. Then, nested integration DO loops increment through all angle and radial-distance sample points. For each sample point, the radial distance between that point and the position of each Ronchi delta function on the detector is used to determine the scaled Bessel amplitudes. The sum of these amplitudes for each—point are then squared to obtain the intensity estimate. Simpson's integration rule is applied for the radial and angular dimensions to provide a number representing the detector element signal.

The major assumption associated with Program WRDET involves the maximum radius of the first-order Bessel function used in the computation of diffraction amplitudes. The first-order Bessel function is infinite in extent and to make computation tractable, yet meaningful, required truncation of the Bessel function. As indicated in figure 10, the function has most of its energy within the central lobe, 83.8 percent, and the total energy contained by the Bessel function radii within the second, third, and fourth zeros are 91.0, 93.8, and 95.3 percent, respectively. In table 1, the radial distances for these zero crossings are shown for six aperture diameters and two transform lens focal length values. A realistic and effective compromise for the Bessel function truncation radius would be the fourth zero radius.

The line-printer output from Program WRDET needs to be explained. The results of the simulation data are presented in appendix B and will be discussed in detail subsequently. Each simulation run is on a seperate sheet having a header indicating programed values for transform lens focal length, sampling aperture diameter, radius to the fourth Bessel zero, optical wavelength, RSI detector model, and number of sampling divisions in the Bessel function to the fourth zero. The body of the printout lists the integrated values for equation (26) for detector rings  $R_{j+1}$ ,  $R_j$ , and  $R_{j+1}$  and detector wedges  $W_j$  and  $W_{j+1}$  for each mid-ring grating spatial frequency.

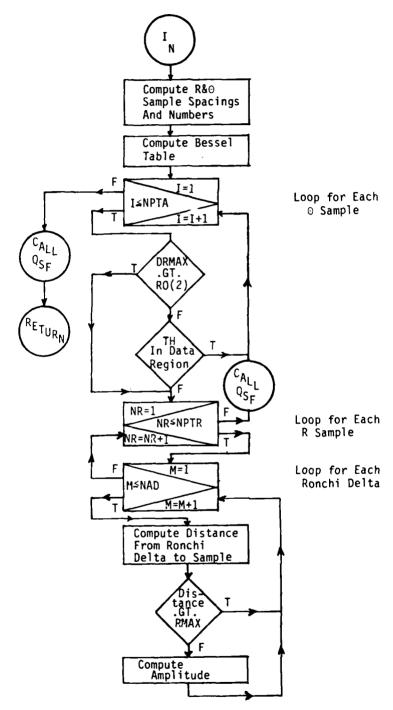


FIGURE 20. Flow Chart of Subroutine AIRYD.

It is important to note that the simulation values have not been scaled by the factor

$$I_{sf} = K^2 = \left[ \frac{B\pi D^2}{4\lambda f} \right]^{-2}$$
 (32)

as shown in equation (23) and equation (26). In the leaf, the values for the scaling factor are indicated for four transform lens focal length and four aperture diameters when B=1.0. To adjust the light input amplitude B so as to maintain normalized output from the values in table 4, we have

$$B = \frac{4\lambda f}{\pi D^2} = \left[\frac{1}{I_{st}}\right]^{-\frac{1}{2}}$$
 (33)

and the expected range of B, for the simulations to be presented, is well within operational optical capabilities.

B. Simulation Results. • Program WRDET was used to provide simulation data for the OPS detection of konchi gratings with a ROSA detector. The simulations are grouped into three data sets and summarized with their simulation conditions in table 5. Data Set 1A simulates detection conditions for the WRD-6420 detector with different transform lens focal lengths and sampling aperture diameters, and Data Set 1B simulates the WRD-6400 detector with similar conditions. Data Set 2 simulates data from uniform Ronchi grating deformations for the WRD-6420 detector, i.e. the Ronchi grating frequency is displaced some percentage from the mid-ring grating frequency in Data Set 2A and the Ronchi grating direction is displaced by an angular factor from the mid-wedge angle in Data Set 2B. Data Set 3 simulates a non-existant detector with equal ring widths (Data Set 3A) and with modifications of equal ring width (Data Set 3B). Table 5 lists the illustration number for the graphical presentation of the data and the appendix B page of the data listings.

**TABLE 4.** Intensity Scaling Factors.

$$I_{SF}^{=} = \frac{B\pi D^{2}}{4\lambda f}$$
 where B=1.0 and  $\lambda$ =0.6328x10<sup>-3</sup>mm

Aperture Diameter	f = 100.0 mm	f = 177.8 mm	f = 622.3 mm	f = 1016.0 mm
0.1	0.01540	0.99487	0.00040	0.00015
0.25	0.60174	0.19035	0.01554	0.00583
0.5	9.62780	3.04553	0.24861	0.09327
1.0	154.4472	48.72853	3.97784	1.49231

**TABLE 5.** Summary of Simulation Conditions with Illustration and Data Page References. (all measurements in mm)

Data Set 1A	•		D		
WRD-6420	Detector	0.50	0.25	0.10	0.075
	177.8	Fig. 21 B-1	Fig. 22 B-2,3	Fig. 23 B-4,5	No Data
f	100.0	Fig. 24 B-6	Fig. 25 B-7	Fig. 26 B-8	Fig. 27 B-9,10
Data Set 1B	:		D		
WRD-6400	Detector	0.50	0.25	0.10	0.075
	177.3	Fig. 31 B-11	Fig. 32 B-12	Fig. 33 B-13	No Data
f	100.0	No Data	Fig. 34 B-14	Fig. 35 B-15	Fig. 36 B-16

# Data Set 2A:

WRD-6420 Detector, f = 100.0 mm, Grating freq = factor x mid-ring freq

factor	D = 0.1		D = 0.	075
0.96 0.97 0.98 0.99 1.00 1.01 1.02 1.03 1.04	Table 14	B-17 B-18 B-19 B-20 B-8 B-21 B-22 B-23 B-24	Table 15	B-25 B-26 B-27 B-9,10 B-28 B-29

#### TABLE 5. Continued.

## Data Set 2B:

WRD-6420 Detector, D = 0.1 mm, f = 100.0 mm, Grating angle = wedge center + factor angle

## Factor angle

8-8
B-31
B-32
B-33
B-34
B-35

#### Data Set 3A:

Equal ring width detector, D = 0.1 mm

f

100	Fig.	40,	B-36
150			B-37
200			B-38

## Data Set 3B:

Modified equal ring width detector, D = 0.1 mm, f = 100.0 mm

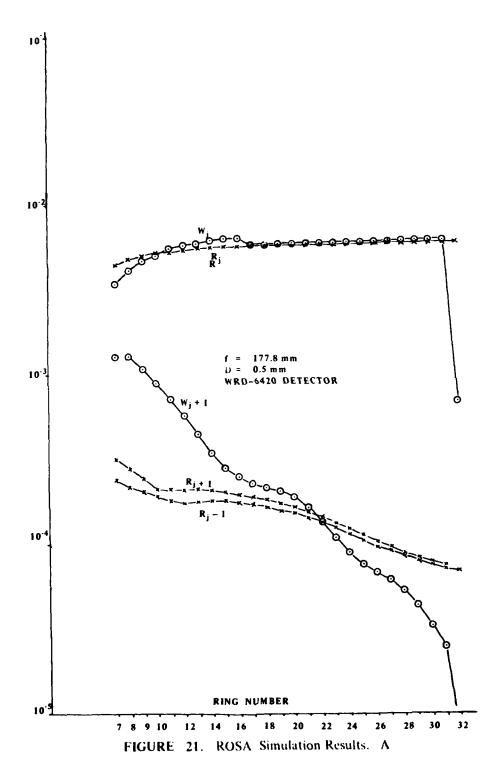
Mod-1 B-39 Mod-2 B-40 Mod-3 B-41 1. Data Set 1A – Detector WRD-6420 Simulations. Figures 21 through 27 contain plots of the simulation data for Data Set 1A. The purpose of this data set is to show the nature of the detector element responses and S/N for the WRD-6420 ROSA detector with different transform lens focal lengths (177.8 and 100.0 mm) and sampling aperture diameters (0.5, 0.25, 0.10, and 0.075 mm). In reviewing this data set, we will first look at the gross comparison of the curves and then at the details of curve configuration and curve differences. The WRD-6420 dimensional data in table 2 and figures 2 and 18 will be referred to frequently in the detailed discussions.

For a transform lens focal length of 177.8 mm, we note that the S/N for the rings and wedges  $(R_j/R_{j+1}, \text{ or } R_j/R_{j+1}, \text{ and } W_j/W_{j+1})$  increases sharply for the 0.5 mm sampling aperture and the signal ring  $R_j$  and wedge  $W_j$  values are generally of the same order of magnitude. As the aperture is made smaller, we see that the S/N decreases, the positive slope of the signal detector elements  $R_j$  and  $W_j$  increases, and the negative slope of the adjacent detector elements,  $R_{j+1}$ ,  $R_{j+1}$ , and  $W_{j+1}$ , decreases. For the smallest sampling aperture at this focal length, 0.1 mm, and S/N values for the wedges are positive throughout; whereas, the S/N values for the rings are less than one for the lower spatial frequencies.

For a transform lens focal length of 100.0 mm, the same generalizations are valid with the additional statement that the S/N values are higher. This is readily seen by comparing figures 24 and 21.

At this time, we will consider the details of curve configuration and curve differences. Graphical and tabular summaries will be introduced to aid in this analysis.

The similarity of figures 2: and 25 is important. We note that for figure 21, when f = 177.8 mm and D = 0.5 mm, the relative aperture, given by  $f^\# = f/d$ , is f/355.6: and for figure 24, when f = 100.0 mm and D = 0.25 mm, the relative aperture is f/400.0. As shown in table 1, the relative aperture provides the scaling function for the relative size of the Bessel function in the spatial frequency domain. The Bessel function zero crossings pertaining to Data Set 1 can be abstracted from table 1 and shown in table 6 as diameters between Bessel function zeros. Considering that 83.9 percent of the energy of the Bessel function is contained in the central maximum, i.e. the diameter between the first zero crossing, that only 7.1 percent of the energy is between the first and second zero crossings, and that 2.8 percent and 1.5 percent of the total energy occurs between the second to third and the third to fourth zero crossings, respectively, one can use the detector ring and wedge timensional data in table 2, with the Bessel function zero crossing dimensions to assist in understanding the ring and wedge data in figures 21 through 27.



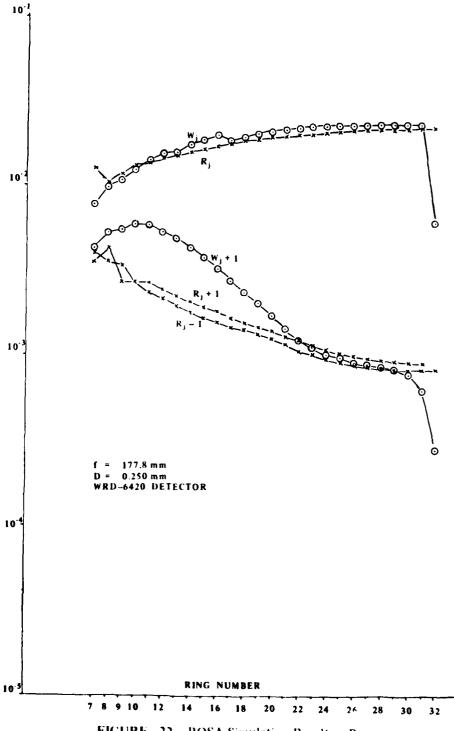
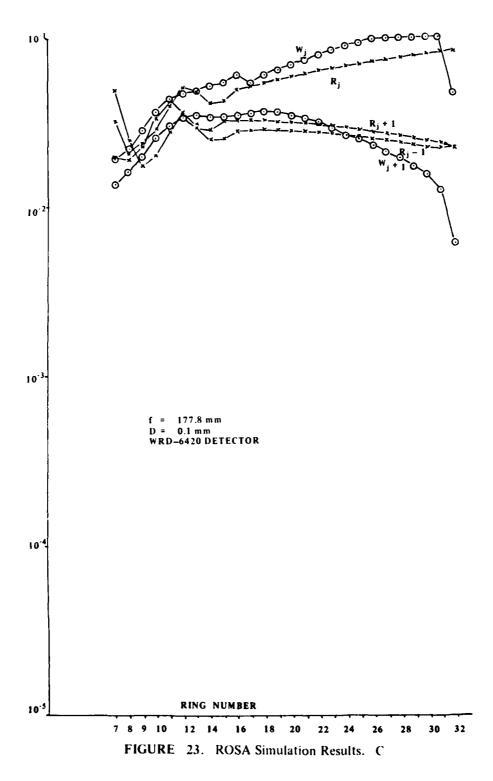
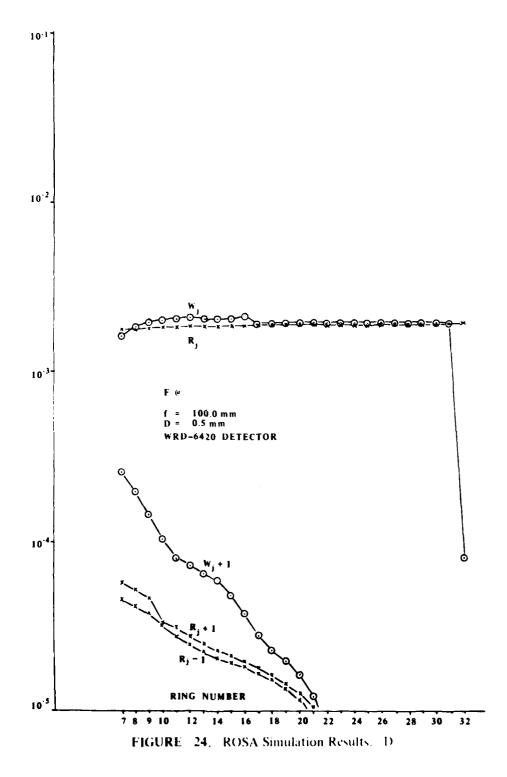
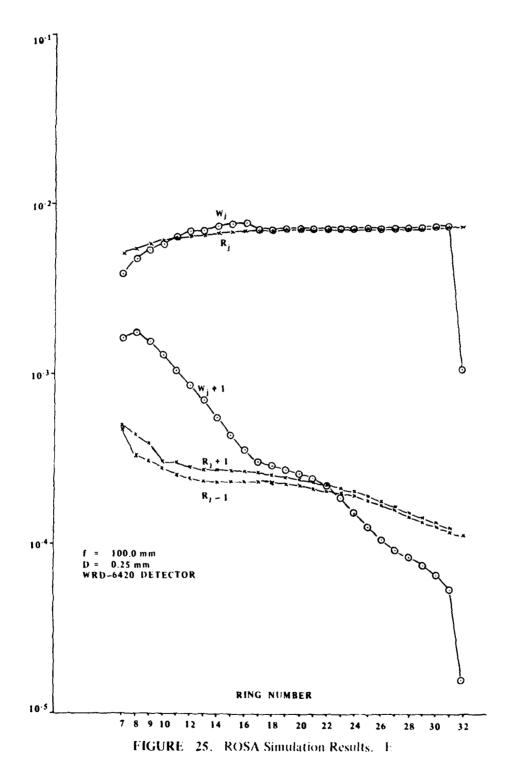
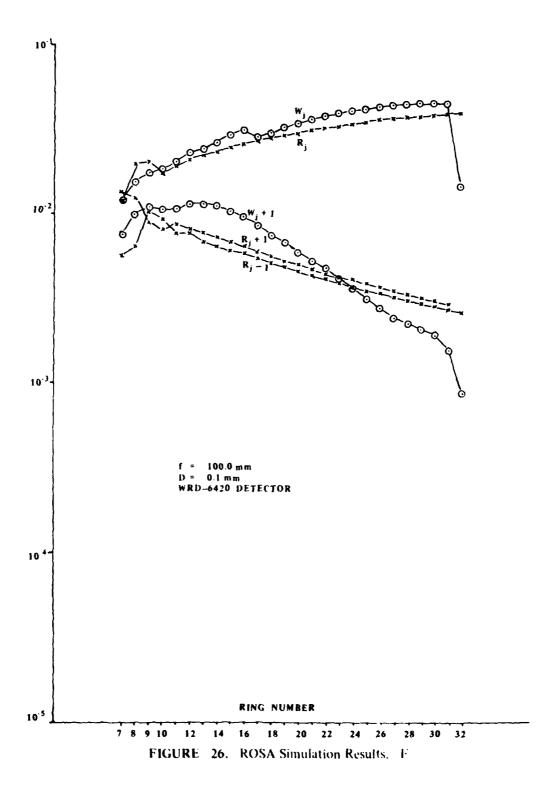


FIGURE 22. ROSA Simulation Results. B









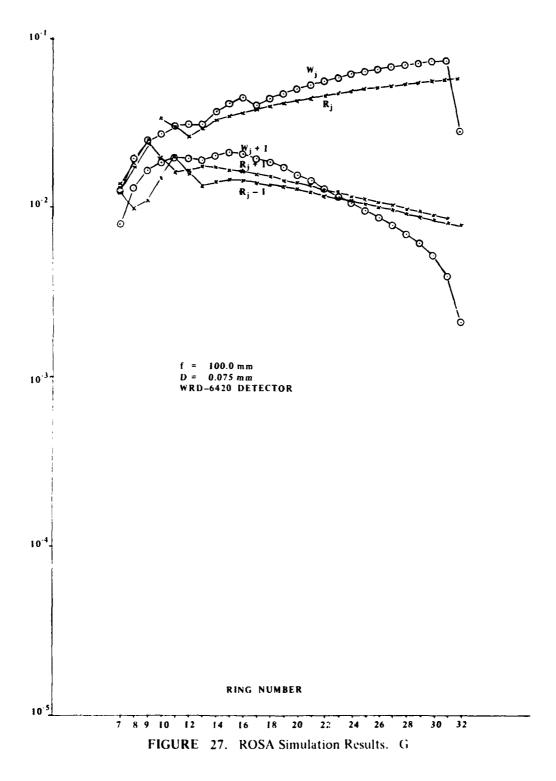


 TABLE
 6. Diameters Between Zero-Order Bessel Functions. Zeros for Selected Transform Lens

 Focal Lengths
 (f) and Sampling Aperature Diameters
 (D). (Dimensions in mm).

Zero Crossing	D = 0.50	f = 177.8 D = 0.50 D = 0.25 D = 0.10	D = 0.10	. = 0.50	f = 10 D = 0.25	0.0 D = 0.10	f = 100.0 f = 0.50 $f = 0.25$ $f = 0.10$ $f = 0.075$
1st Zero	0.550	1.098	2.746	0.308	0.618	1.544	2.058
2nd Zero	1,004	2.010	5.024	0.566	1.130	2.826	3.768
3rd Zero	1.458	2.914	7.286	0.820	1.640	4.098	5.464
4th Zero	1.908	3.818	9.544	1.074	2.146	5.366	7.156

Another useful type of data for interpretation of Data Set 1 is the location of the Ronchi Grating deltas for the mid-ring spatial frequencies associated with the WRD-6420 detector when the transform lens focal lengths are specified. Table 7 represents data of this type for a 177.8 mm transform lens focal length, and table 8 has similar data for a 100.0 mm lens.

The next data analysis aids to be introduced are the generalized ring and wedge models shown in figure 28. The ring model shows the Bessel functions, represented in plan view by the four zero crossing circles, located at the mid-ring radius, and each successive ring has a greater radius difference, as shown in table 2 and figures 17 and 18. The scale of the Bessel function is arbitary and can be adjusted to satisfy our interpretation of the mod and to fit the curve being interpreted. The wedge model of figure 28 represents the Besset functions positioned for a Ronchi grating spatial frequency of 30.39 line-pairs per millimeter when the 177.8 mm transform lens is employed. This corresponds to the data for Ring 13 in table 7. This wedge model has 3 general cases and 18 special cases, shown in figures 29 and 30, respectively. The general cases apply where all of the Bessel function energy within the fourth zero radius is incident on the detector wedges. For the first general case, the Bessel function is scaled so that the total significant energy is detected by  $W_i$  and the energy in  $W_{i+1}$  and  $W_{i+1}$  is considered insignificant. In general case two, all of the energy is contained in wedges W<sub>i-1</sub>, W<sub>i</sub>, and  $W_{i+1}$ ; and for general case three, the energy is incident on other adjacent wedges. The special cases apply when portions of the scaled Bessel function exist outside of the detector wedges. In figure 30, the special cases of the bottom row apply when the lower radius of the detector wedges (WLR) is greater than the axial distance of the delta harmonic  $r_p$  less the fourth zero radius of the Bessel function  $r_2$ . Likewise, the special cases in the top and middle rows of figure 30 apply when portions of the fourth zero circle are beyond the higher radius of the detector wedges (WHR). Table 9 represents a summary of the occurrences of special cases for selected simulation with the WRD-6420 detector, which will be useful in analyzing curves for detector signals.

Figure 21 can be analyzed as a simple example of a detailed curve analysis. The remaining curves in Data Sets 1A and 1B can be analyzed in like fashion. First, note that the scaled Bessel function at the origin has a fourth zero crossing radius less than the least radius of Ring 7 (tables 6 and 2). Next, note that with the first harmonic positioned at the mid-radius of Ring 7, there will be no signal contribution on Ring 7 owing to the Bessel function positioned at the third-order harmonic (tables 2, 6 and 7). This lack of signal is easily seen when the third-order Bessel function is positioned at an axial distance of 3.855 mm and when the radius of fourth zero crossing for f = 177.8 mm and D = 0.5 mm is 0.954 mm. When subtracted, the resulting radial distance (2.901 mm) is greater than the maximum ring radius (1.395 mm) for Ring 7. Thus,

TABLE 7. Summary of Ronchi Grating Deltas for 177.8 mm Transform Lens Focal Length (Detector WRD-6420).

Axial Distance of Ronchi Harmonics (mm) (Circled Distances Are Harmonics Beyond Detector)

Harmonic Delta	Intensity																									
$\frac{11}{0.0008}$		14.134	006.11																							
9		11.564	17.082	20.178	•																					
7		8.994	13 287	15 697	18,319	21.042																				
5		6.424	000.0	11 212	13.085	15.032	17.095	19.280	21,570	23.970																
3 0.011		3.855	5,694	6.727	7.851	9.019	10.258	11.567	12.941	14.382	15.891	17.466	19.107	26.817	22.590	24.438	26,340	28.311	30.351	32.457	34.629	36.861	39.171	41.541	43.974	46.476
$\frac{1}{0.101}$		1.285	1.300	2.242	2.617	3.006	3,419	3,856	4.314	4.794	5.297	5.822	6,369	6.939	7.530	8.146	8.780	9.437	10.117	10.819	11.543	12.287	13.057	13.847	14.658	15.492
0.250		<b>5</b> C	o C	· C	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	<b>.</b>	0	0	0	0	0	0
Mid-Ring Spatial Frequency		11.42	16.87	19.93	23.26	26.72	30.39	34.27	38.34	42.61	47.08	51.75	56.61	61.67	66.93	72.40	78.04	83.88	89.92	96.16	102.59	109.21	116.05	123.07	130.28	137.69
Ring No.	•	~ ∝	ο σ	10	11	12	13	14	15	16	17	18	19	50	21	22	23	24	52	56	27	28	53	30	31	32

 TABLE
 8. Summary of Ronchi Grating Deltas For 100.0 mm Transform

 Lens Focal Length (Detector WRD-6420).

Axial Distance of Ronchi Harmonics (mm) (Circled Distances Are Harmonics Beyond Detector)

Harmonic Delta Intensity	לון נפווס ון ל																								
11 0.0008	14.137	100.11																							
0.001	11.567	17.091	20.189																						
0.002	8.997	13.293	15.703	18.321	21.049																				
	6.426	9,495	11.216	13.086	15.035	17.101	19.281	21.569	23.970																
3.011	3.856	5.697	6.730	7.852	9.021	10.261	11.569	12.941	14.382	15.892	17.469	19.109	20.818	22.593	24.438	26.342	28.311	30.352	32,457	34.629	36.867	39.172	41.541	43.975	46,473
0.101	1.285	1.899	2.244	2.618	3.007	3.420	3.856	4.314	4.794	5.297	5.823	6.370	6.939	7.531	8.146	8.781	9.437	10.117	10.819	11.543	12.289	13.057	13.847	14.658	15,492
0.250	00	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
Mid-Ring Spatial Frequency	20.31	30.01	35.45	41.36	47.52	54.05	60.94	68.17	75.76	83.71	92.02	100.66	109.66	119.01	128.73	138.76	149.13	159.88	170.97	182.41	194.20	206.34	218.82	231.64	244.80
Ring No.	۲ ۰	0 0	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	52	56	27	28	59	30	31	32

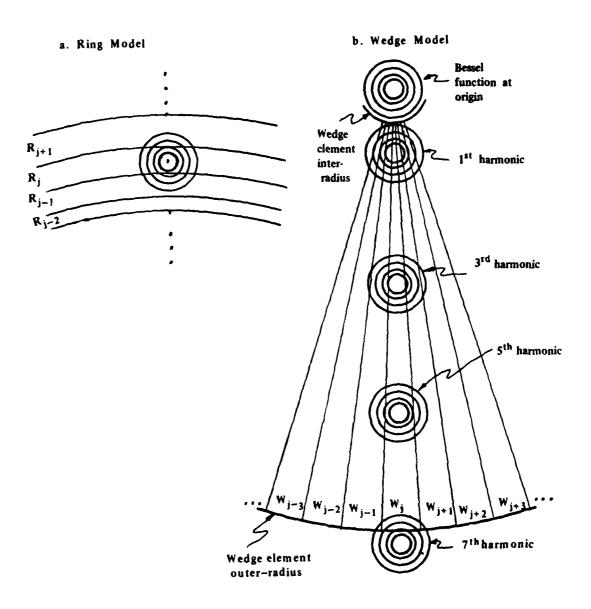
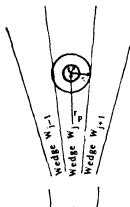


FIGURE 28. Generalized Ring and Wedge Models.

LET: rp = axial distance of ith delta harmonic.

 $r_1$  = radius of inscribed circle in wedge  $W_j$ , centered at  $r_p$ .  $r_2$  = radius of Bessel function  $4^{th}$  zero.

= radius of incribed circle in wedges  $W_{j+1} + W_j + W_{j+1}$ , centered at  $r_p$ .

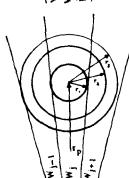


GENERAL CASE #1 - When  $r_2 \le r_1$ . Energy  $E_j$  on wedge  $W_j$  due to Bessel function centered at  $r_p$  is

$$E_j \approx l_i [1 - J_o^2 (\pi r_2 D/\lambda f)] = l_{r_2}$$

where I, is the intensity of the ith delta harmonic.

Energy  $E_{jh}$  on Wedge  $W_{j+1}$  is considered insignificant.



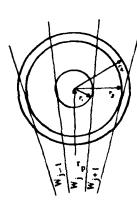
GENERAL CASE #2- When  $r_1 \le r_2 \le r_3$ . Energy  $E_j$  on wedge  $W_j$  is

$$E_j \approx I_{r_2} - I_i P'$$

where P' is percentage of Bessel function energy in sectors outside of  $W_i$ .

Energy Eih on wedge Wih

$$E_{1h} \approx I_i P'/2$$



GENERAL CASE #3 – When  $r_2 > r_3$ . As in General Case #2 Energy on  $W_j$  is

$$E_i \approx I_{r_2} - I_i pP'$$

Energy  $E_{i+1}$  on wedge  $W_{i+1}$  is

$$E_{i+1} \approx I_i (P' - P'')/2$$

where P" is percentage of Bessel function energy in sectors outside of

$$(W_{j+1} + W_j + W_{j+1}).$$

FIGURE 29. Three General Cases for Estimating Bessel Function Energy Incident on a ROSA Wedge Detector Flement.

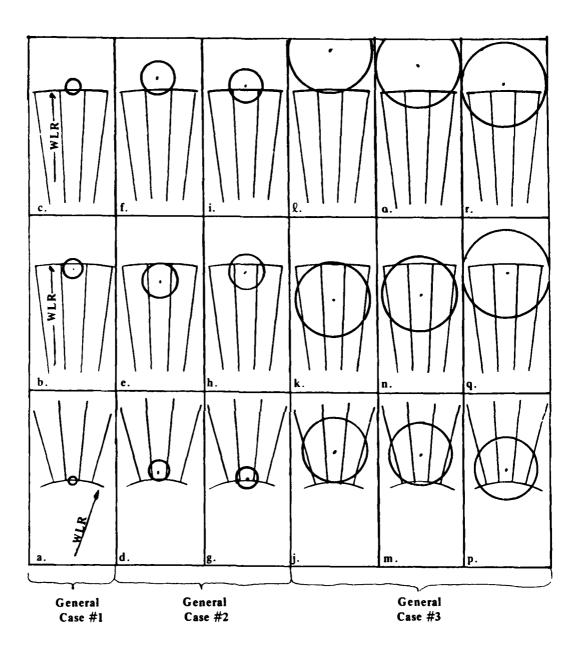


FIGURE 30. Eighteen Special Cases for Estimating Bessel Function Energy Incident on a ROSA Wedge Detector Element.

 TABLE
 9. Occurrence of Special Cases Shown in Figure 30 When Program WRDET Simulated

 Wedge Detection for ROSA Detector Model WRD-6420.

622.3 mm $f = 1016.0$ mm 0.5 mm $D = 0.5$ mm	, a,	ص ص ص ص ص ص ص ک ک ک کر ہد ہد	Z 00 00 00 K
f = 622 D = 0.5	σ.σ.σ.σ.σ.σ.σ.σ.σ.σ.σ.σ.σ.σ.σ.σ.σ.σ.σ.	,	ZOOOK
տ D = 0.1 mm	99999999 99999999 0000 0000 0000		Z O OO OO K
f = 177.8 mm n D = 0.5 mm	aaa = I	·	шн
1 D = 1.0 mm	മമ ധ മ		U
D = 0.1 mm	ν. σ.	Ç <b>≥</b> ≈ ⊙ ∝ ⊙	<b>z</b> 00 K
f = 100.0 mm D = 0.25 mm	σσσχς. I.S	ш⊷	π μ
E		ပ	ပ
g c	7 8 8 0 1 2 1 0 0 1 2	13 17 17 19	20 22 22 22 22 24 27 28 29 31 31

the ring detector signals for conditions of figure 21 are due to a single Bessel function positioned at the mid-ring radius. The  $R_j$  curve is directly relatable to the plots of ring widths in figure 17 and 18, and the shapes of  $R_{j+1}$  and  $R_{j+1}$  curves can also be related to these plots.

The wedge signals for figure 21 can be analyzed from table 7, which defines the axial distances and intensities of Ronchi deltas, from figures 29 and 30, which describe the general and special cases for estimating wedge signals, and from table 9, which summarizes the occurrences of the special cases. It will be noted that all  $W_1$  curves in figures 21 through 27 have a discontinuity between Ring 16 and Ring 17. This discontinuity is due to the transition from the occurrence of the first and third harmonics on the detector for the Ring 16 data to the first harmonic on the detector when the third harmonic is off of the detector for the Ring 17 data, as seen from tables 7 and 9. The slope changes in the  $W_{j+1}$  curves can be related to the diameter of the Bessel function zeros in table 6, the wedge width data in table 2, and the slope changes in figure 10.

Table 10 summarizes the number of detector elements with S/N greater than 1.0 for the data in Data Set 1A. It should be noted that when the  $f^{\#}$  is less than about 1,000, all 26 rings and 32 wedges have S/N greater than 1.0, and the S/N improves inversely with  $f^{\#}$ .

2. Data Set 1B - Detector WRD 6400 Simulations. Table 5 lists the simulation conditions under which Data Set 1B was obtained. The essential differences between these data and those of Data Set 1A were the detectors, which have been described in the section Geometry of ROSA Detectors. Data Set 1B simulation results obtained with the WRD-6400 detector are presented in figures 31 through 36, and a quick comparison with their counterparts in Data Set 1A will show significant differences. The simulation results of Data Set 1B are generally less well-behaved and have lower S/N ratios. Details of the plots can be explained by using the plots of mid-ring radii for the two detectors in figures 15 and 16, the plots of the ring widths in figures 17 and 18, the dimensions of the two detectors in tables 2 and 3, and the summaries of Ronchi grating deltas for the 177.8 and 100.0 mm transform lens focal lengths shown in tables 11 and 12, respectively.

**TABLE 10.** Detector Elements with S/N > 1 In Data Set 1A.

Number of Detector Elements with S/N>1

	f	D	f/D	Rings	Wedges
Fig. 2	177.8 mm	0.5 mm	355	26	32
22	2 177.8	0.25	711	26	32
23	177.8	0.10	1778	21	32
2	100.0	0.5	200	26	32
2	5 100.0	0.25	400	26	32
2	6 100.0	0.10	1000	25	32
2	7 100.0	0.075	1333	23	32

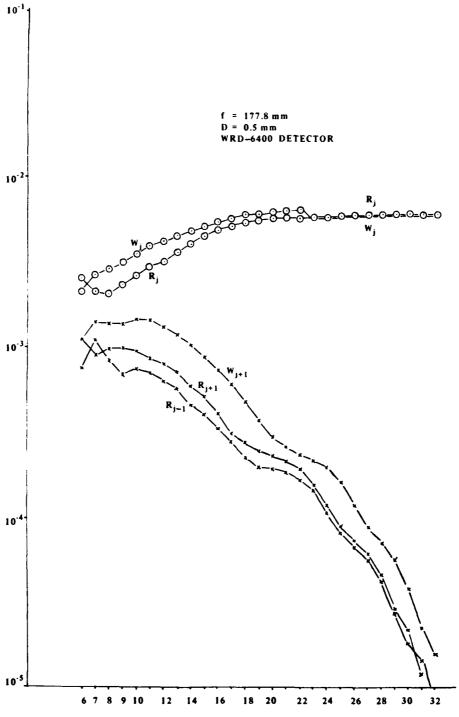


FIGURE 31. ROSA Simulation Results. H

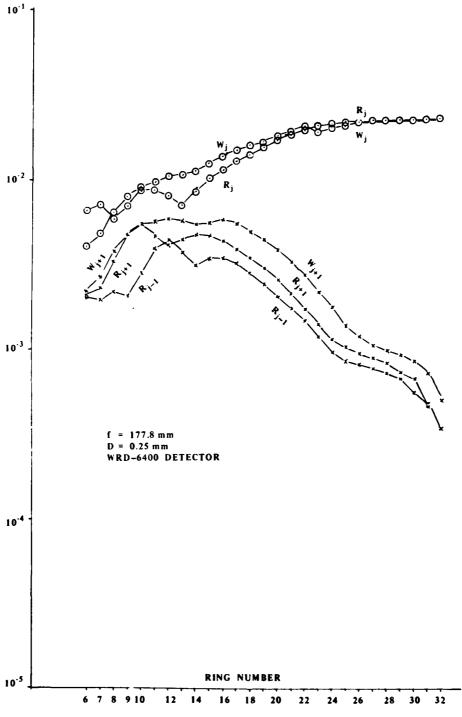
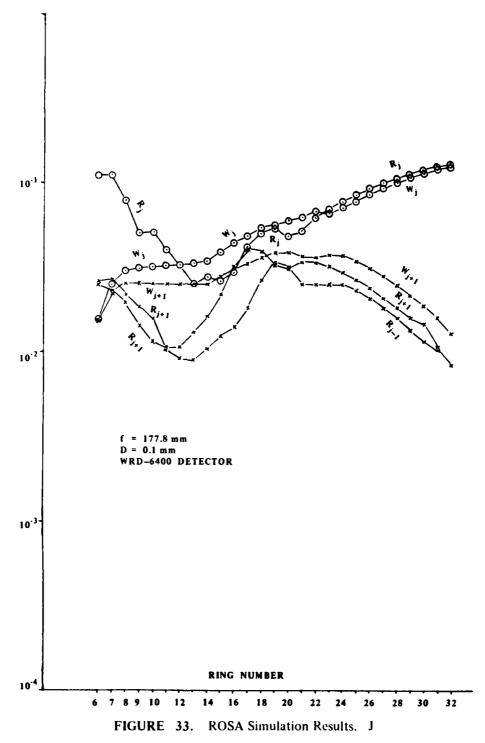


FIGURE 32. ROSA Simulation Results. 1



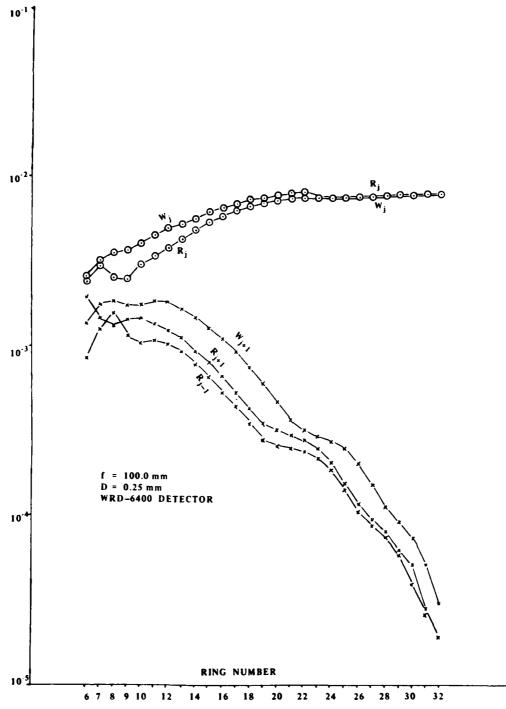


FIGURE 34. ROSA Simulation Results. K

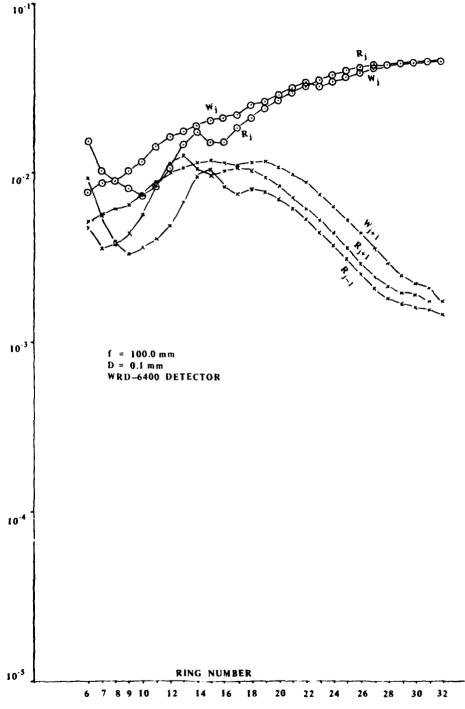


FIGURE 35. ROSA Simulation Results. L

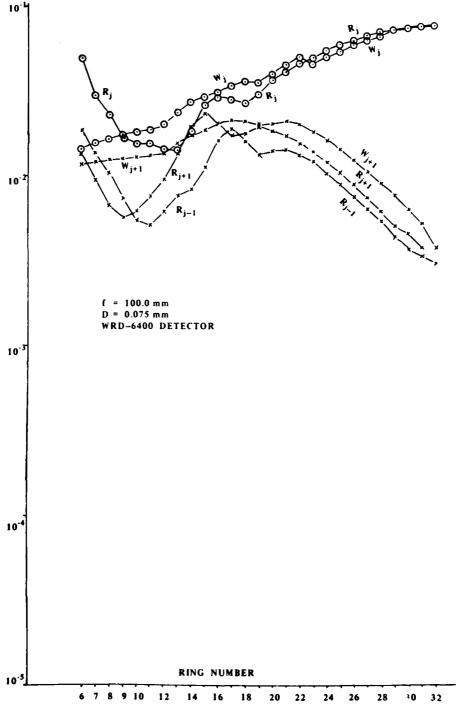


FIGURE 36. ROSA Simulation Results. M

TABLE 11. Summary of Ronchi Grating Deltas For 177.8 mm Transform Lens Focal Length (Detector WRD-6400).

Axial Distance of Ronchi Harmonics (mm) (Circled Distances Are Harmonics Beyond Detector)

Harmonic Delta Intensity	(a - cilian i - cilian																									
11 0.0008	6.423	8.899	10.260	11,757	14.641	15.248	17.277																			
9	5.255	7.281	8,395	9.620	11.979	12.475	14.136	16.030	18.166																	
0.002	4.088	5,663	6.529	7.482	9.317	9,703	10.995	12.467	14,129	16,004	18.130	20,524														
5	2.920										٠.,					•										
3 0.011	1.752 2.079	2.427	2.798	3.207	3.993	4.158	4.712	5.343	6.055	6.829	7.770	8.796	9.961	11.274	12.755	14.420	16.242	18.348	20.664	23.239	26.091	29.247	32.721	36.545	40.744	45.338
0.101	0.584	809	.933	690.	.219	.386	.571	.781	.018	.286	.590	.932	.320	.758	.252	908.	.424	.116	.888	.746	769.	.749	206.	.182	. 581	.113
0.250	00	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
Mid-Ring Spatial Frequency	5.19	7.19	8.29	9.50	11.83	12.32	13.96	15.83	17.94	20.32	23.02	56.06	29.51	33.40	37.79	42.72	48.21	54.36	61.22	68.35	77.30	86.65	96.94	108.27	120.71	134,32
Ring No.	9	œ	0	10	11	12	13	14	15	16	17	13	19	20	21	22	23	24	52	56	27	28	53	30	31	32

TABLE 12. Summary of Ronchi Grating Deltas For 100.0 mm Transform Len. Teal Length (Detector WRD-6400).

Axial Distance of Ronchi Harmonics (mm) (Circled Distances Are Harmonics Beyond Detector)

Harmonic Delta		
11 0.0008	6,432 7,630 8,896 10,267 11,764 13,407 15,244 17,284	
9	5.262 6.242 7.278 8.400 9.625 10.969 12.472 14.141 16.026 18.162	
7.00.00	4.093 4.855 5.661 6.534 7.486 8.530 9.701 10.999 12.465 14.126 16.004 18.126	
5 0.004	2.924 3.468 4.044 4.667 5.347 6.929 7.856 8.903 10.090 11.432 12.947 14.622 16.602 18.791 21.259 24.027	
3 0.011	1.754 2.081 2.426 2.800 3.208 3.656 4.714 4.714 5.342 6.054 6.054 6.859 7.768 8.797 11.275 11.275 11.275 12.755 12	29.245 32.719 36.546 40.743 45.333
0.101		9.748 10.906 12.182 13.581 15.113
0.250	000000000000000000000000000000000000000	20000
Mid-Ring Spatial Frequency	9.24 10.96 12.78 16.90 19.26 21.90 24.83 31.89 46.34 46.34 67.19 96.65 108.86 137.44	154.05 172.35 192.51 214.62 238.83
Ring No.	61 11 12 13 13 14 13 13 13 13 13 13 13 13 13 13 13 13 13	28 30 31 32

The simulation data for the WRD-6400 detector becomes particularily ill-behaved for both transform lens focal lengths when the sampling aperture has a diameter of 0.1 mm or less. An example of the manner in which a S/N value less than 1.0 mm is obtained for the f = 100.0 mm, D = 0.1 mm data shown in figure 35 is illustrated in figure 37 where the sections through the zero and first-order harmonics have been plotted for the first harmonic centered on Ring 12. If we algebraically add the two curves, square the results, and then integrate over the Ring 12 and Ring 13 areas, we find that the  $R_1/R_{1+1}$  is less than one.

It will also be noted that the wedge data have lower S/N ratios for the WRD-6400 detector because of the smaller wedge angles when compared to those of the WRD-6420 detector.

Table 13 summarizes the number of detector elements with S/N greater than 1.0 for Data Set 1B. When this data is compared with the similar data in table 10 for the WRD-6420 detector, we see more rings with S/N greater than 1.0, but it must be remembered that the S/N are in general lower, especially for the lower and middle detector rings, as shown in figures 38 and 39 for f = 100.0 mm and D = 0.1 mm.

3. Data Set 2A – Ronchi Grating Deformation. Table 5 lists the simulation conditions under which Data Set 2A was obtained. The purpose of this data set was to examine the change in S/N when the Ronchi grating was subjected to simple linear deformations. These linear deformations were obtained by multiplying the mid-ring spatial frequency by a factor that had a value between 0.96 and 1.04. Note that this is not the equivalent to selecting a deformation and then computing the S/N values for each ring detector element. For example, a 4 percent deformation having its first harmonic centered on Ring 7 for f = 100.0 mm with the WRD-6420 detector is only 0.051 mm; whereas, the same percent of deformation for the Ring 32 spatial frequency would amount to a deformation of 0.620 mm. In either case, however, the effect of the deformation is to move the position of the first harmonic grating function from its mid-ring position. Figures 38 and 39 plot the mid-ring S/N values for  $R_i/R_{i-1}$  and  $R_i/R_{i+1}$  for the WRD-6420 and the WRD-6400 detector respectively when f = 100.0 mm and D = 0.10 mm. Table 14 lists the S/N values for grating deformations associated with the WRD-6420 detector. Figure 38 plots S/N values for no deformation (f = 1.0) while figure 40 plots S/N for selected rings from table 14. Table 15 is similar to that of table 14, except that D = 0.075 mm instead of 0.10 mm.

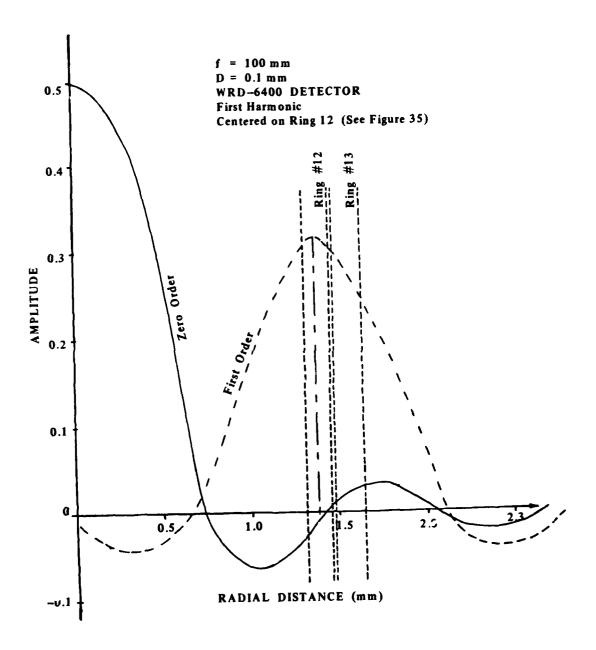
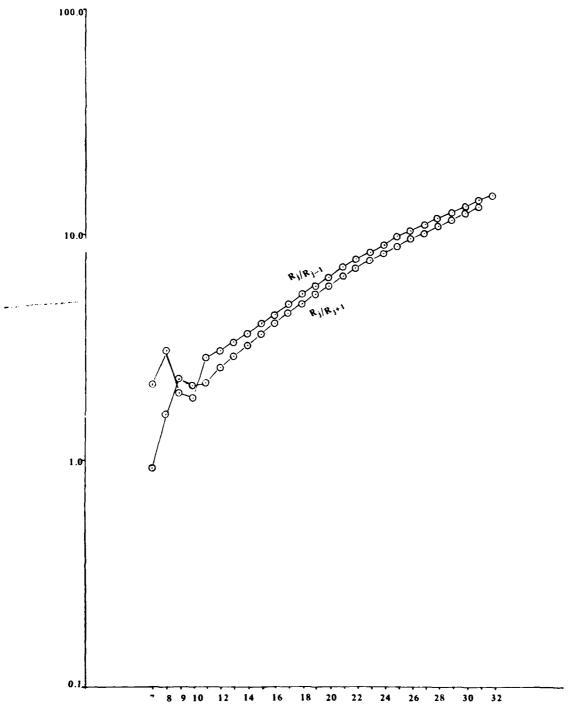


FIGURE 37. Example for S/N Less Than 1.0.

**TABLE 13.** Detector Elements with S/N > 1 In Data Set 1B.

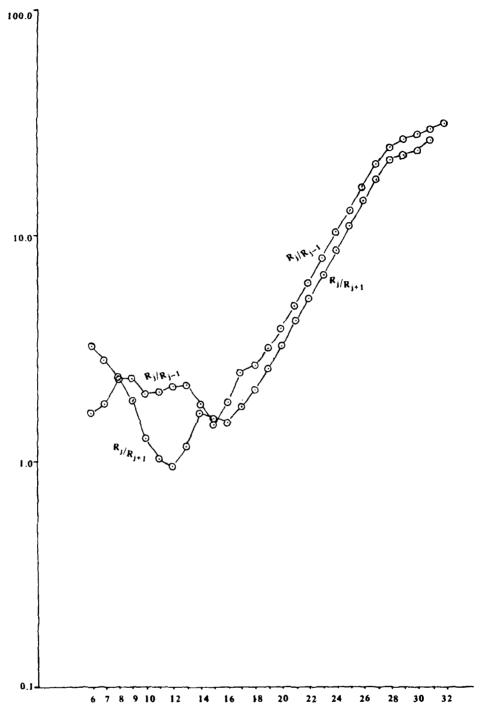
Number of Detector Elements with S/N>1

		f	D	f/D	Rings	Wedges
Fig.	31	177.8 mm	0.5 mm	355	27	32
	32	177.8 mm	0.25 mm	711	27	32
	33	177.8 mm	0.10 mm	1778	26	32
	34	100.0	0.25 mm	400	27	32
	35	100.0	0.10 mm	1000	26	32
	36	100.0	0.075 mm	1333	26	32



Note: S/N for  $R_1/R_{1-1}$  and  $R_1/R_{1+1}$  When f = 100.0 mm, D = 0.1/ mm, and WRD-6420 DETECTOR.

FIGURE 38. Signal-to-Noise Plots. A



Note: S/N for  $R_j/R_{j+1}$  and  $R_j/R_{j+1}$  When f = 100.0 mm, D = 0.1 mm, and WRD-6400 DETECTOR.

FIGURE 39. Signal-to-Noise Plots. B

TABLE 14. S/N for Ronchi Grating Deformations, (Grating Freq. = Factor X Mid-Radius Freq.) f = 100.0 mm, D = 0.1 mm, (Detector WRD-6400).

	1.04	0.76	1.28	1.64	1.37	1.32	1.37	1.37	1.36	1.33	1.29	1.25	1.18	1.12	1.04	0.97	0.89	0.31	0.73	0.66	0.59	0.52	0.46	0.41	0.36	0.31	,
	1.03	08.0	1.36	1.79	1.53	1.49	1.60	1.65	1.68	1.70	1.70	1.72	1.68	1.67	1.61	1.57	1.50	1.43	1.36	1.28	17.1	1.12	1.04	0.97	0.88	0.82	,
	1.02	0.83	1.44	1.94	1.71	1.71	1.87	1.98	5.09	2.19	2.26	2.37	2.40	2.49	2,50	2.54	2.54	2.53	2.51	2.49	75.2	2.39	2.34	2.28	2.19	2.13	,
-	1.01	0.87	1.53	2.11	1.91	1.95	2.17	2.39	2,60	2.81	3.01	3.28	3.44	3.71	3.87	4.12	4.30	4.46	4.63	4.82	4.99	90.5	5.21	5,35	5.40	5.54	
R <sub>j</sub> /R <sub>j</sub> +1 FACTOR	1.00	0.32	1.61	2.30	2.16	2.21	2.59	2.90	3.22	3.65	4.02	4.51	4.96	5.55	5.97	6.59	7.13	7.68	8.27	8.91	9.65	10.18	10.91	11.71	12.33	13.27	
	0.99	96.0	1.72	2.50	2.40	2.55	3.03	3.51	4.06	4.69	5.36	6.25	7.00	8,03	8.90	10.04	11.03	12.10	13.22	14.42	15./1	16.77	18.07	19.37	20.41	21.61	1
	0.93	1.01	1.83	2.72	2.70	2.95	3.57	4.27	5.03	6.05	7.08	8.43	9.26	11.04	12.20	13.61	14.81	15.83	16.82	17.86	18.75	19.35	20.01	20.45	20.53	20.81	•
	0.97	1.07	1.94	2.97	3.04	3.36	4.23	5.20	6.35	7.70	60.6	10.82	12.10	13.56	14.42	15.37	15.96	16.26	16.51	16.78	16.86	16.73	16.73	16.64	16.41	16.49	•
	96.0	1.13	5.06	3.23	3.42	3.87	5.00	6.30	7.82	3.50	11.08	12.72	13.56	14.27	14.30	14.40	14.25	13.94	13.68	13.54	13.28	12.90	12.77	12.64	12.44	12.56	,
Quid	£ .	7	∞	6	10	Ξ	12	13	14	15	16	17	13	13	20	21	22	23	54	55	56	27	58	53	30	31	۲.
	1.04	2.52	3.36	5.65	2.83	4.77	5.71	7.30	9.01	11.05	13.13	15.20	16.26	17.01	16.83	16.65	16.06	15.54	15.20	14.94	14.67	14.32	14.21	14.04	13.80	13.86	14 64
	1.03	2.44	3.73	2.46	2.56	4.22	4.89	5.98	7.22	8.75	10.48	12.50	14.18	15.91	16.92	17.94	18.24	18.34	18.48	18.53	13.50	18.35	18.34	19.25	18.07	18.17	12 12
	1.32	2.36	3.51	2.23	2.32	3.72	3.30	4.32	5.49	6.78	7.98	9.48	10.64	12.58	13.98	15.71	16.91	17.94	19.00	19.97	20.65	21.28	21.31	22.19	22.38	22.65	22 63
	1.01	. 23	33	~	0	-	7	<b>&lt;</b> †																ထ	75	7	12
- Ö		(1)	ς.	6	2	۳.	د	4.0	4,53	5.23	5.97	6.33	7.79	8.87	9.90	11.27	12.42	13.48	14.77	16.14	17.30	13,42	19.80	20.3	22.(	23.2	24
<sup>Р</sup> j/Рj-: FACTOR	1.50	2.20 2																									
P <sub>J</sub> / <sub>P</sub> FACT	0.39 1.00	2.20	3.03	2.00	1.90	2.86	3.09	3.31	3.67	4.06	4.42	4.97	5.45	5.36	6.50	7.22	7.81	8,35	9.05		10.43	11.06	11.90	12.63	13.32	14.18	14 38
R <sub>j</sub> 7P FACT		2.13 2.20	2.33 3.09	1.85 2.00	1.73 1.90	2.53 2.86	2.63 3.39	2.77 3.31	2.94 3.67	3,13 4,06	3.33 4.42	3.57 4.97	3.76 5.45	4.00 5.96	4.16 6.50	4.44 7.22	4.64 7.81	4.76 8.35	4.95 9.02	9.80	5.30 10.43	5.40 11.06	5.59 11.90	5.68 12.63	5.73 13.32	5.35 14.18	5 26 14 38
P <sub>j</sub> 72 FACT	0.39	2.06 2.13 2.20	2.76 2.93 3.09	1.73 1.85 2.00	1.57 1.73 1.90	2.23 2.53 2.86	2.26 2.63 3.09	2.30 2.77 3.31	2.37 2.94 3.67	2,44 3,13 4,06	2.51 3.33 4.42	2.59 3.57 4.97	2.62 3.76 5.45	2.67 4.00 5.96	2.67 4.16 6.50	2.73 4.44 7.22	2.72 4.64 7.81	2.67 4.76 8.35	2.65 4.95 9.02	5.18 9.80	2.58 5.30 10.43	2.51 5.40 11.06	2.47 5.59 11.90	2.39 5.68 12.63	2.29 5.73 13.32	2.21 5.35 14.18	2 10 5 26 14 38
P <sub>J</sub> / <sub>P</sub> FACT	5.38 0.39	1.98 2.06 2.13 2.20	2.60 2.76 2.93 3.09	1.61 1.73 1.85 2.00	1,43 1,57 1,73 1,90	1,96 2,23 2,53 2,86	1,95 2,26 2,63 3,09	1.93 2.30 2.77 3.31	1.32 2.37 2.94 3.67	1.36 2.44 3.13 4.06	1.90 2.51 3.33 4.42	1.89 2.59 3.57 4.97	1.84 2.62 3.76 5.45	1.80 2.67 4.00 5.96	1.72 2.67 4.16 6.50	1.63 2.73 4.44 7.22	1.61 2.72 4.64 7.81	1.51 2.67 4.76 8.35	1.43 2.65 4.95 9.02	2.65 5.18 9.80	1.26 2.58 5.30 10.43	1.17 2.51 5.40 11.06	1.10 2.47 5.59 11.90	1.01 2.39 5.68 12.63	0.32 2.23 5.73 13.32	0.34 2.21 5.35 14.18	0 77 2 10 5 26 14 38
c. LL	0.97 0.98 0.99	1.98 2.06 2.13 2.20	2.60 2.76 2.93 3.09	1.51 1.61 1.73 1.85 2.00	1.30 1.43 1.57 1.73 1.90	1,73 1,96 2,23 2,53 2,86	1.63 1.95 2.26 2.63 3.09	1.61 1.93 2.30 2.77 3.31	1.51 1.32 2.37 2.94 3.67	1.51 1.36 2.44 3.13 4.06	1.44 1.90 2.51 3.33 4.42	1.33 1.89 2.59 3.57 4.97	1.29 1.84 2.62 3.76 5.45	1.22 1.80 2.67 4.00 5.96	1.12 1.72 2.67 4.16 6.50	1.04 1.63 2.73 4.44 7.22	0.35 1.61 2.72 4.64 7.81	0.36 1.51 2.67 4.76 8.35	0.77 1.43 2.65 4.95 9.02	1.36 2.65 5.18 9.80	0.62 1.26 2.58 5.30 10.43	0.55 1.17 2.51 5.40 11.06	0.43 1.10 2.47 5.59 11.90	0.43 1.01 2.39 5.68 12.63	0.37 0.92 2.29 5.73 13.32	9.33 0.34 2.21 5.35 14.18	0.28 0.77 2.10 5.86 14.98

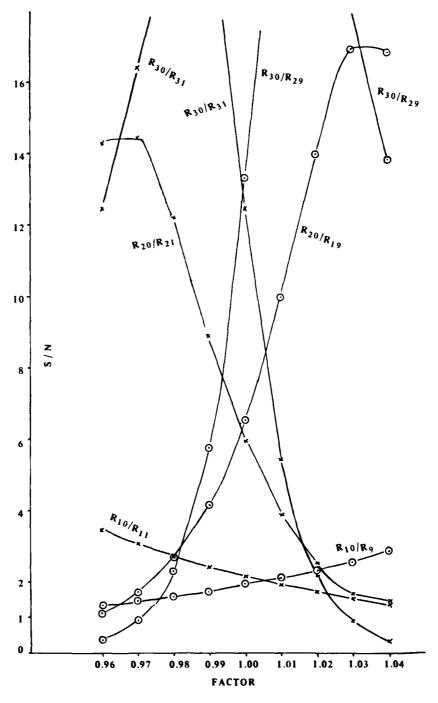


FIGURE 40. Plots of Selected Data From Table 14.

TABLE 15. S/N for Ronchi Ruling Deformations (Grating Freq. = Factor X Mid-Radius Freq.)f = 100.0 mm, D = 0.075 mm, (Detector WRD-6400).

	1.04	1.00	0.78	0.82	1.37	1.36	1.10	1.08	1.14	1.14	1.12	1.10	1.07	1.04	0.99	96.0	0.91	0.85	0.80	0.74	0.69	0.63	0.58	0.53	0.47	0.43	
	1.02	1.05	0.80	0.89	1.54	1.58	1.33	1.34	1.47	1.53	1.57	1.63	1.66	1.71	1.72	1.77	1.78	1.79	1.81	1.81	1.82	1.80	1.78	1.76	1.73	1.71	ı
	1.01	1.08	0.89	0.93	1.63	1.71	1.46	1.49	1.67	1.78	1.86	1.98	2.08	2.20	2.28	2.45	2.52	2.62	2.74	2.84	2.97	3.05	3.15	3.24	3.32	3.41	
Rj/Rj+1 FACTOR	1.00	1.11	0.93	0.97	1.73	1.84	1.58	1.17	1.91	2.08	2.25	2.42	2.61	2.85	3.05	3,33	3.58	3,85	4.18	4.48	4.85	5.18	5.54	5.93	6.29	6.75	•
	0.99	1.13	0.97	1.00	1.84	1.99	1.76	1.86	2.18	2.43	5.66	2.98	3,30	3.70	4.09	4.61	5.12	2.67	6.33	6.99	7.78	8.50	9.30	10.16	10.98	11.90	,
	0.98	1.15	1.02	1.04	1.95	2.15	1.94	5.09	2.50	2.82	3.20	3.68	4.19	4.84	5.48	6.36	7.22	8.15	9.25	10.25	11.40	12.36	13.31	14.22	14.95	15.68	,
	96.0	1.21	1.11	1.12	2.21	2.55	2.37	2.64	3.31	3.96	4.67	99.5	6.72	8.04	9.56	10.68	11.75	12.44	12.80	12.81	12.63	12.17	11.75	11.32	10.88	10.52	
Ring	No.	7	∞	6	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	52	<u>26</u>	27	28	53	30	31	32
	1.04	1.20	2.00	2.97	2.88	1.87	2.32	3.41	3.95	5.12	5.25	6.33	7.50	8.92	10.43	12.22	13.49	14.37	14.88	14.81	14.42	13.71	13.06	12.43	11.85	11.40	10.96
	1.02	1.12	1.95	2.43	2.56	1.65	1.94	2.74	3.04	3.22	3.58	4.11	4.63	5.26	5.98	96.9	7.90	8.90	10.11	11.41	12.68	13.74	14.91	15.88	16.62	17.32	17.71
	1.01	1.09	1.84	2.34	.42	. 55	11	46	89	9/	6	4			4	_	4	_	0	_		_	2	0	98	Ω.	82
³j′Rj-1 ∙ACTOR				•••	~	_	٠.	2	2.	2	2.9	۳. ښ	3.6	4.03	4.4	5.0	5.5	6.10	6.8	7.6	8.42	9.19	10.1	11.1	11.5	12.9	13.
R. FA	1.00	1.05																								7.14 12.9	
R <sub>j</sub>	0.99 1.00	1.02 1.05	1.78	2.24	2.28	1.45	1.63	1.56	2.32	2.37	2.51	2.72	2.90	3.10	3.32	3.62	3.87	4.12	4.44	4.81	5.17	5.50	5.92	6.33	6.72	7.14	7.52
R <sub>j</sub>		1.02	1.72 1.78	2.15 2.24	2.16 2.28	1.37 1.45	1.49 1.63	1.99  1.56	2.08 2.32	2.05 2.37	2.12 2.51	2.24 2.72	2.31 2.90	2.41 3.10	2.50 3.32	2.63 3.62	2.72 3.87	2.80 4.12	2.91 4.44	3.04 4.81	3.14 5.17	3.22 5.50	3.33 5.92 1	3.43 6.33 1	3.50 6.72	7.14	3.62 7.52 1
R <sub>.</sub> j	66.0	0.99 1.02	1.66 1.72 1.78	2.06 2.15 2.24	2.04 2.16 2.28	1.28 1.37 1.45	1.37 1.49 1.63	1.79 1.99 1.56	1.84 2.08 2.32	1.77 2.05 2.37	1.79 2.12 2.51	1.84 2.24 2.72	1.86 2.31 2.90	1.88 2.41 3.10	1.89 2.50 3.32	1.93 2.63 3.62	1.94 2.72 3.87	1.93 2.80 4.12	1.93 2.91 4.44	1.94 3.04 4.81	1.93 3.14 5.17	1.90 3.22 5.50	1.89 3.33 5.92 1	1.86 3.43 6.33 1	1.82 3.50 6.72 1	3.57 7.14	1.73 3.62 7.52 1

- 4. Data Set 2B Ronchi Grating Rotation. This data set, as shown in table 16, was obtained to investigate S/N values when the Ronchi gratings were rotated from the wedge bisector. The f and D conditions under which the data were obtained are the same as figure 38 and table 14. The results, as expected, show a decrease to a S/N value of 1.0 when the grating is rotated 2.5°, neglecting a small but finite separator between wedges.
- 5. Data Set 3A Equal Ring Width Detector. In section 4, the simulation data indicated response differences for the two detectors. This motivated an attempt to redesign the ROSA detector to perform better. Data Set 3A represents simulation data from a detector with equal ring spacing when D = 0.1 mm and the transform lens focal length were 100.0, 150.0, and 200.0 mm.

A summary for a ROSA type, equal ring width detector is tabulated in table 17. This detector had 32 rings and 32 wedges, with the mid-ring radii 0.5 mm apart and with 0.0254 mm (1.0 mil) allowance for detector element sperators. Table 17 gives the mid-ring spatial frequencies for f = 100.0 mm, f = 150.0 mm, and f = 200.0 mm and the Ronchi grating delta positions when the first harmonic was positioned at the mid-ring. These detector data can be compared with similar data in tables 2, 3, 7, 8, 11, and 12.

Simulation data for the equal ring width detector are plotted in figures 41 through 43 for D = 0.1 mm and f = 100.0 mm, f = 150.0 mm, and f = 200.0 mm, respectively. For a quick appraisal of the results, compare figure 41 with figure 26 and figure 35, and note that although the absolute response is reduced for the rings and wedges, the S/N is increased and almost constant for the rings. Additionally, note that rings 3 through 32 and wedges 3 through 32 all have S/N greater than 1.0. Figures 42 and 43 indicate that S/N decreases with increased transform lens focal length, and the noise seen in figure 40, for the lower rings, becomes more sever as f increases. Table 18 summarizes the number of detector elements with S/N greater than 1.0 for Data Set 3A.

6. Data Set 3B - Modified Equal Ring Width Detector. Although there were noisy variations in the simulation data for Data Set 3A for the lower rings, a brief attempt was made to adjust ring width to minimize this noise. However, these attempts were unsatisfactory, and the data appears in appendix B as indicated in table 5.

**TABLE 16.** S/N For Grating Rotations From Wedge Bisector. f = 100.0 mm, D = 0.1 mm, (Detector WRD-6420).

## ROTATION FROM WEDGE BISECTOR

Ring	$\phi = \phi.0$	$\phi = 0.5^{\circ}$	φ = 1.0°	φ = 1.5°	φ = 2.0°	φ = 2.50
7	1.62	1.52	1.39	1.26	1.13	1.00
8	1.57	1.48	1.36	1.24	1.12	1.00
9	1.61	1.50	1.38	1.25	1.12	1.00
10	1.71	1.58	1.43	1.28	1.14	1.00
11	1.88	1.71	1.53	1.34	1.16	1.00
12	2.01	1.80	1.59	1.38	1.18	1.00
13	2.08	1.83	1.59	1.37	1.17	1.00
14	2.40	2.05	1.74	1.46	1.21	1.00
15	2.77	2.31	1.90	1.55	1.25	1.00
16	3.24	2.62	2.10	1.66	1.29	1.00
17	3.33	2.61	2.04	1.61	1.27	1.00
18	4.01	3.03	2.29	1.73	1.32	1.00
19	4.81	3.51	2.56	1.87	1.37	1.00
20	5.74	4.06	2.86	2.01	1.42	1.00
21	6.79	4.67	3.18	2.16	1.47	1.00
22	8.00	5.34	3.51	2.31	1.52	1.00
23	9.43	6.10	3.87	2.45	1.56	1.00
24	11.14	<b>6.9</b> 8	4.26	2.61	1.61	1.00
25	13.16	8.04	4.71	2.77	1.66	1.00
26	15.41	9.29	5.24	2.96	1.71	1.00
27	17.63	10.75	5.87	3.18	1.77	1.00
28	19.82	12.33	6.59	3.43	1.83	1.00
29	21.12	13.98	7.43	3.73	1.91	1.00
30	23.41	16.14	8.51	4.09	2.00	1.00
31	28.53	20.42	10.38	4.64	2.12	1.00
32	16.52	13.50	8.62	4.41	2.10	1.00

TABLE 17. Summary for a ROSA-Type Detector With Equal Ring Widths.

	Order	Delta Infensity																															
.10R)	Ξ	သ		11.000	16.500																												
RONCHI GRAIING DELTA POSITIONS (mm) (CIRCLED DISTANCES ARE HARMONICS BEYOND DETECTOR)	თ	0.001		9.000	13,500	18,000																											
POSITIO	7	0.002		7.000	10.500	14,000	17.500	21.000																									
4G DELTA	S	0.004		5.000	7.500	10,000	12.500	15,000	17.500	29.000	22,500	25.000																					
RONCHI GRATING DELTA POSITIONS (mm) DISTANCES ARE HARMONICS BEYOND DET	ო	0.011		3.000	4.500	000.9	7.500	9.000	10.500	12,000	13,500	15,000	16.500	18,000	19.500	21,000	22.500	24.000	25,500	27,090	28,500	30.000	31,500	33,000	34.500	36,000	37.500	39.000	40,500	42,000	43.50)	45.000	40.000
RONCE LED DIS	1	0.101		1.000	1.5000	2.000	2.500	3.000	3.500	4.000	4.500	5.000	5.500	000.9	6.500	7.000	7.500	8.000	8.500	9.000	9.500	10,000	10.590	11.000	11.500	12,000	12,500	13,000	13.500	14,000	14.500	15.000	12.0.6
(CIRC	0	0.250		C	0	0	0	0	0	0	0	0	0	0	0	0	0	0	Ç	0	0	0	0	0	0	0	0	0	0	0	O	0	>
	_	f = 200.0		7.30	11.85	15,80	19.75	23.70	27.65	31.61	35.56	39.51	43.46	47.41	51.36	55.31	59.26	63.21	67.16	71.11	75.06	79.01	32.96	86.92	90.87	94.82	38.77	102.72	106.67	110.62	114.57	116.52	14. 221
	MID-RING SPATIAL FREQUENCY	f = 150.0		10.53	15.30	21.07	26.34	31.61	36.87	42.14	47.41	52.68	57, <sup>n</sup> 4	63.21	68.48	73.75	79.01	84.28	89.55	94.82	100.08	105.35	110.62	115.89	121.15	126.42	131,69	136.96	142.23	147.49	152.76	158.03	00.001
	Ω Σ	f = 100.0		15.80	23.70	31.61	39.51	47.41	55.31	63.21	71.11	79.01	86.92	94.82	102.72	110.62	118.52	126.42	134.32	142.23	150.13	158.03	165.93	173.83	181.73	189.63	197.53	205.44	213.34	221.24	229.14	237.04	50° FF 3
		Radius Difference		0.4746	=	Ξ	=	z	=	=	=	=	=	z	=	=	=	÷	Ξ	z	=	=	=	=	=	£	=	=	=	=	=	= =	
		Maximum Radius	0.5000	1.2373	1,7373	2,2373	2.7373	3.2373	3,7373	4.2373	4.7373	5.2373	5.7373	6.2373	6.7373	7.2373	7,7373	8.2373	8.7373	9.2373	9.7373	10.2373	10.7373	11.2373	11.7373	12.2373	12,7373	13.2373	13.7373	14.2373	14.7373	15.2373	7 . 7 . 7 7
		Mid-Radius	•	1.000	1.5	2.0	2.5	3.0	3.5	4.0	4.5	5.0	5.5	0.9	6.5	7.0	7.5	3.0	8.5	9.0	9.5	10.0	10.5	11.0	11.5	12.0	12.5	13.0	13.5	14.0	14.5	15.0	1.7
		Least Radius	0.0000	0.7627	1.2627	1.7627	2.2627	2.7627	3.2627	3.7627	4.2627	4.7627	7.2627	5.7627	6.2627	6.7627	7.2627	7.7627	8.2627	8.7627	9.2627	9.7627	10.2627	10.7627	11.2627	11.7627	12.2627	12.7627	13.2627	13.7627	14.2627	14.7627	
		Ring No.	- 6	ı m	4	2	9	7	က	6	0.	Ξ	12	13	14	12	16	17	13	19	50	21	22	23	54	52	9.	27	28	53	20	33	;

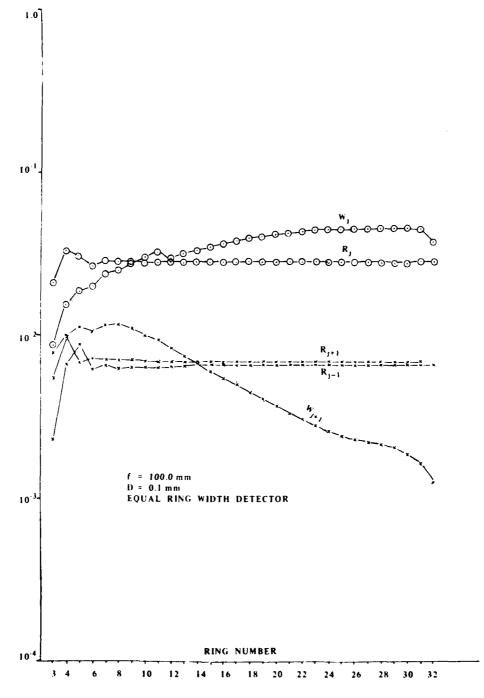


FIGURE 41. ROSA Simulation Results. N

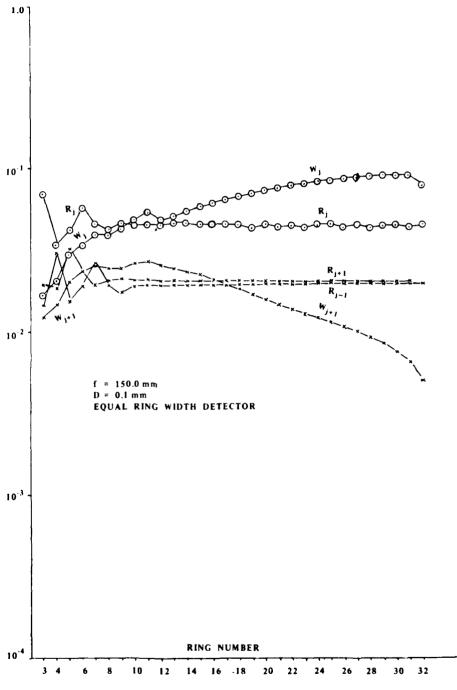
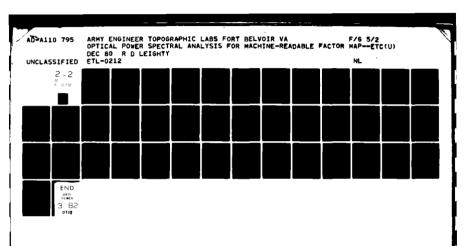
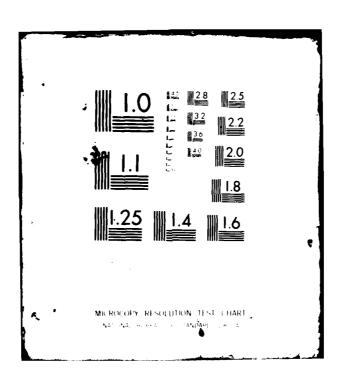


FIGURE 42. ROSA Simulation Results. O





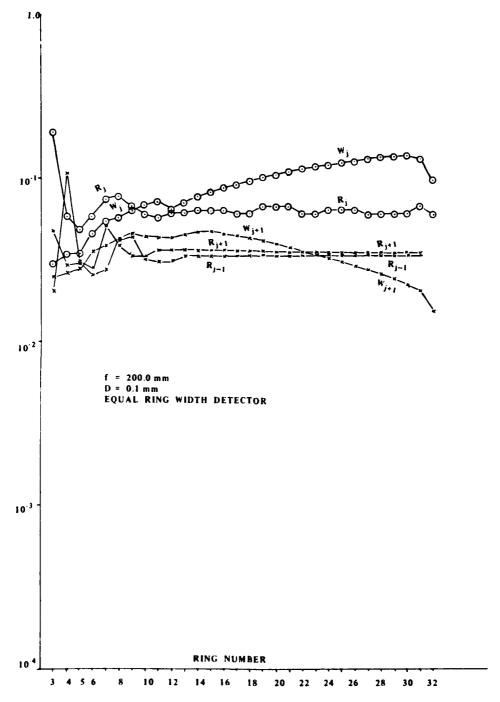


FIGURE 43. ROSA Simulation Results. P

**TABLE 18.** Detector Elements With S/N > 1 In Data Set 3A (Equal Ring Width Detector).

				Number of De Elements with S/N>1	
	f	D	f/D	Rings	Wedges
Fig. 40	100.0 mm	0.1 mm	1000	30	32
41	150.0	0.1	1500	30	32
42	200.0	0.1	2000	29	32

## V. PRELIMINARY OPTICAL SUBSYSTEM DESIGN FOR GRATING MAP SYSTEMS

In the preceding section, we determined that Ronchi gratings having spatial frequencies, such that the first harmonic of the grating transform is positioned at the midradius of the detector ring, would yield a unique detection of the grating frequency if the sampling aperture diameter and transform lens focal length are properly selected. In that section, we also determined that the direction of the Ronchi ruling could be determined uniquely if the grating was aligned perpendicular to the bisector of a detector wedge. In this section, we will be more pragmatic and will consider the preliminary optical subsystem design of grating map systems. We will see how optical system parameters affect the amount of information that can be recorded, and we will see how the interaction of parameters force the optical designers to make trade-offs for realistic optical system specifications. Yet we will not have enough information to design a system because of the dependence upon the grating fabrication capability, which will be discussed in the following section.

A. Basic Optical Subsystem Design. • Suppose we have a Ronchi grating map fabrication capability with a minimum writing spot diameter d. The maximum grating spatial frequency of the recorder system is then

$$w_{max} = 1/2d \tag{34}$$

and the minimum period of the grating is

$$P_{\min} = 1/w_{\max} = 2d$$
 25)

Knowing the dimensions of the frequency plane detector, we can use the relation

$$f = R_{max}/\lambda w_{max}$$
 (36)

to determine the transform lens focal length f of the system, given the mid-radius of the most distant detector ring  $R_{m,a,\kappa}$  and the wavelength  $\lambda$  of the laser light.

The minimum detectable grating spatial frequency  $|\mathbf{w}_{\min}|$  is related to the sampling aperture diameter D. To show this relationship, we note that

$$\mathbf{w}_{min} = 1/\mathbf{P}_{max} \tag{37}$$

where  $P_{max}$  represents the Ronchi grating period associated with the minimum grating spatial frequency  $w_{min}$ . We know that the Ronchi grating period must be less than the sampling aperture diameter D to enable detection of Ronchi frequency spectra. We choose

$$P_{max} \leq D/N \tag{38}$$

where the factor N = 2.5 enables at least 2.5 periods of the grating to be sampled with safety; a factor smaller than 2.0 will result in frequency spectra of a line or a line and an edge. Thus, the minimum detectable Ronchi grating spatial frequency should be

$$w_{\min} \geqslant 2.5/D \tag{39}$$

For example, if D = 0.1 mm, then a choice for  $w_{min}$  would be 25 1p/mm. A clear choice for  $w_{min}$  can be obtained by the association

$$w_{\min} = R_{\min}/\lambda f \tag{40}$$

where  $R_{min}$  is the mid-radius of the detector ring closest to the optical axis that will satisfy equation (39).

Sampling aperture diameter D and transform lens focal length f also influence S/N as the simulation data in the previous section indicates. For an f# less than 1000, i.e.

$$f^{\#} = f/D < 1000$$
 (41)

the simulation assures S/N > 1.0 for WRD-6420 detectors for 26 rings and 32 wedges (table 10) or 27 rings and 32 wedges for the WRD-6400 detectors (table 13). Higher  $t^{\#}$  combinations can be used as indicated in tables 13 and 18.

The diameter of the sampling aperture, coupled with detector responsivity, will determine the power requirements for the system's laser light source. (Data are not available on laser power requirements at this time.) Available laser power, sample aperture diameter, and detector responsivity will determine the maximum sample rates and decision-making software that can be optimized to operate within these constraints. Sampling and decision-making should be possible at microsecond rates.

Selection of the sampling aperture diameter is of major importance for the S/N of the detected signal, and it determines the resolution of the factor map sampling. Selection of the sampling aperture diameter should be consistent with the precision of

the factor map. Table 19 indicates the relation between selected sampling aperture diameters for various map reduction ratios and their equivalent diameters when projected onto a map or the ground surface. For example, a 22" x 29" (558.8 mm x 736.6 mm) factor map having a scale of 1:50,000 when reduced 10x will have a format size of 55.9 by 73.7 mm, which is suitable for commercial 70-mm chips or roll films. If a 0.1 mm diameter sampling aperture is used for grating detection at this reduction, it has an equivalent of 50 meters on the ground. Complete readout of the factor map could be accomplished with 411,612 samples. Knowing the aperture diameter and sample spacing and knowing the format size of the grating map can be used to establish specifications for the optical or mechanical scanning components.

- B. System Design Trade-Offs. For any given set of design parameters, there is sufficient motivation to investigate approaches that will yield a more cost-effective system design. One potential means for accomplishing this design is to put more factor maps on the same recording material. For example, above we indicated that a 70-mm chip could be used to encode grating maps with 10x reduction, and if we now consider 35-mm grating maps with a 20x reduction, then we could put four grating maps on a 70-mm film chip. Likewise 16 seperate 16-mm grating maps might fit on a 70-mm film chip with 40x reduction, and with 65x reduction 98 seperate factor maps could be encoded on a 4 by 5.5-inch (10 by 14cm) microfiche format. Although factor map reductions of this magnitude are not practical, we will now discuss system trade-offs at the designer's disposal that may lead to smaller grating map formats for selected applications.
- 1. Focal Length Trade-Offs. Table 19 is of value in selecting the sampling aperture diameter when given a desirable level of factor map reduction and the map sample resolution. From the simulation data, we found that the  $f^{\#}$  of the optical system (41) was a major factor in determining the S/N for Ronchi Grating Detection. The reason, of course, relates to the aperture diameter scaling of the Bessel function as shown in table 1. Thus, if we achieved acceptable S/N results for D = 0.1 mm and f = 100.0 mm, i.e. f/D = 1000, then we would expect equivalent S/N results for D = 0.05 mm and f = 50.0 mm. Although this is true, we must also keep in mind that given a grating of spatial frequency  $w_0$  a change in f will effect a change in the position of the grating harmonics on the detector, e.g.

$$f_1/f_2 = R_1/R_2$$
 (42)

where R<sub>i</sub> is the radius from the optical axis to the first harmonic of the grating function.

 TABLE 19.
 Sampling Aperture Diameters Projected Onto Map and Ground Surface For Selected

 Map Reduction Ratios.

4AP SIZE: 22" x 23" (558.8 mm x 736.6 mm) MAP SCALE: 1:50,000 EQUIVALENT MAP SAMPLE DIA./GROUND SAMPLE DIA.

SAMPLING APERATURE DIAMETER

			,			т
0.75mm	3.15	THE LE	11.25mm	E S. C.	30.0mm 30.05	13.75mm
0.50mm	2.5mm.25m	15. CM	1.5mm.15.1		18	32 Smm
0.25ฑฑ	Lang ?	J. 2. 2. 18. 18. 2. 2.	3.15mm. 5.1.6	15. Carried St. 25.	moos CI	
9.10mm	mer o		1	2. Jamil John		Ţ
0.375mm	1815	THE CO. LEWIS TO.	1.124.00.25	nest mass. 1	3 commission	4 315mm Fm
ე.ეგო	10.25mm	O SOMM	0.15mm	1.0mm	2:00	3.25
. 025mm	0.125mm	0.25mm	0.375mm 5m	0.50mm	1.00mm	1.62.5mm.75
0.01mm	0.05.11	ļ	ms. 1.0	10.20mm	D. A. Orm	3.65mm
Commensial Format	5" × 7"	7 Jrum		35mm	15mm	Microfiche Image
l Format	111.5mm x 147.4mm	55.3 x 73.7	37.3 x 49.2	27,3 x 36,3	ر ا ا ا ا ا ا ا ا ا ا ا ا ا ا ا ا ا ا ا	8,5 x 31,3
Map Reduction Reduced Ratio	- 5x	ř	-15x		¥5.	-654

Or if we fix the radius  $R_o$ , such as a mid-ring radius of the detector, then a change in f must be reflected in a change in the spatial frequency, i.e.

$$f_1/f_2 = w_2/w_1 (43)$$

Thus, if we reduce the focal length by a factor of 2.0, we must increase the grating spatial frequency by a factor of 2.0 to keep the first harmonic of the grating at radius  $R_o$ . We will see in the next chapter that this trade-off is not generally applicable because it implies a capability for fabricating gratings at arbitrary spatial frequencies.

2. Laser Wavelength Trade-Offs. There is another trade-off available; we can change the wavelength  $\lambda$  of the laser light source within certain limits. As seen from (36) and (40), the wavelength of the laser light source is the scalar-relating focal length f, the grating spatial frequency w, and the radial distance from the optical axis R. Also, table 1 indicates that the size of the Bessel function for any  $f^{\#}$  is directly related to the wavelength  $\lambda$ .

Table 20 lists some common gas lasers, their associated wavelengths, and a ratio value of the wavelength compared to the common HeNe wavelength. Using the expression for ratios of the Bessel function in table 1 and the laser wavelengths in table 20, we can compute equivalent sampling aperture diameters, as shown in table 21. Here the radius to the fourth Bessel zeros are given for detected values of f and D with  $\lambda = 0.6328 \times 10^{-3}$  mm. The equivalent D<sub>2</sub> for other  $\lambda_2$ , which yields the same Bessel radii, are given by

$$D_2 = D_1 (\lambda_2/\lambda_1) \tag{44}$$

and are shown to the right of table 21. Figure 44 graphs f/D versus radii from the optical axis for two selected Bessel zeros and two laser wavelengths. Changing from HeNe to HeCd lasers reduces the radius of the Bessel zeros by nearly a factor of 2.

Of equal importance, we can improve S/N by selecting a shorter wavelength. Modification of equation (41) to reflect this sensitivity to  $\lambda$  is given by

$$(\lambda_2/\lambda_1) f^{\#} = (\lambda_2/\lambda_1) (f/D) < 1000$$
 (45)

When the wavelength of the light source is changed, it should be remembered that the mid-ring spatial frequencies will change accordingly, as shown in Table 22

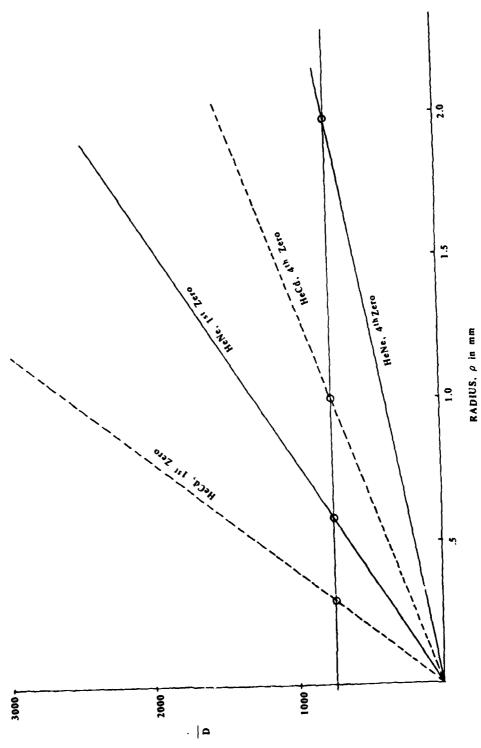
TABLE 20. Common Gas Lasers and Their Associated Wavelengths,  $\lambda$ .

Gas Lasers (CW)	Ratio $\frac{\lambda}{1/\lambda}$ HeNe
HeNe , $\lambda = 0.6328 \times 10^{-3} \text{ mm}$	1,000
Ar , $\lambda_1 = 0.5145 \times 10^{-3} \text{ mm}$	0.813
$\lambda_2 = 0.4880 \times 10^{-3} \text{ mm}$	0.771
HeCd , $\lambda_1 = 0.4416 \times 10^{-3} \text{ mm}$	0.698
$\lambda_2 = 0.3250 \times 10^{-3} \text{ mm}$	0.514
Gas Lasers (Pulsed)	
Ne , $\lambda = 0.5401 \times 10^{-3} \text{ mm}$	0.854
$N_2$ , $\lambda = 0.3371 \times 10^{-3} \text{ mm}$	0.533

TABLE 21. Equivalent Sampling Aperture Diameters for Selected Laser Wavelengths.

/ : 0 = 1

	0.325 x 10 <sup>-3</sup>	0.051	0.128	0.257	0.514
EQUIVALENT SAMPLING APERTURE DIAMETERS (D2) FOR SELECTED LASER WAVELENGTHS (+2)	$f = 100.0$ $f = 177.8$ $f = 622.3$ $f = 1016.0$ $0.5145 \times 10^{-3}$ $0.488 \times 10^{-3}$ $0.4416 \times 10^{-3}$ $0.325 \times 10^{-3}$	0.070	0.174	0.349	0.698
EQUIVALENT SAMPLING APERTURE DIAMETERS (02) SELECTED LASER WAVELENGTH	0.488 x 10 <sup>-3</sup>	0.0771	0.193	0.386	0.771
	0.5145 x 10 <sup>-3</sup>	0.081	0.203	0.386	0.813
S	f = 1016.0	1	,	5.4533	ı
RADIUS TO FOURTH BESSEL ZERO FOR TRANSFORM LENS FOCAL LENGTHS	f = 622.3	1		3,3401	,
US TO FOURTH FOR NSFORM LENS	f = 177.8	4.7716	t	0.9543	0.4772
αi	f = 100.0	2.6837	1.0735	0.5367	•
Sampling Aperture	Diameter $( = 0.6328 \times 10^{-3})$	0.1	0.25	0.5	1.0



**FIGURE 44.** The f/D vs  $\rho$  (radius from optical axis) for Two Selected Bessel Zeros and Two Laser Wavelengths.

TABLE 22. ROSA Detector (Model WRD-6420) Mid-Ring Spatial Frequencies for Four Laser Wavelengths.

MID-RING SPATIAL FREQUENCIES

= 100.0 mm f = 177.8 mm f = 177.8 mm f = 177.8 mm f = 100.0 mm f = 100.0 mm f = 177.8 mm f = 100.0 mm f = 100		. = 0.5145	х 10~ тт	. = 0.4880	$= 0.4880 \times 10^{-3}$ mm	. = 0,4416	= 0.4416 x 10 <sup>-3</sup> mm	· = 0.3250 x 10 <sup>-</sup>	х 10-' тт
26.33     14.81     29.99     16.37       32.38     18.21     35.78     20.12       38.91     21.89     43.00     24.19       45.96     25.85     50.79     28.57       53.63     30.16     59.26     33.33       61.62     34.66     68.09     38.30       70.08     39.42     77.45     43.56       79.02     44.44     87.32     49.11       88.40     49.72     97.69     54.94       98.24     55.25     108.56     61.06       108.55     67.11     131.86     74.16       119.32     67.11     131.86     74.16       119.32     67.11     131.86     74.16       119.32     67.11     131.86     74.16       119.32     67.11     131.86     74.16       142.19     79.97     157.13     88.38       154.32     86.80     170.54     95.92       166.93     93.88     184.47     103.75       166.93     193.38     188.76     120.19       221.70     124.69     245.00     137.79       236.54     133.04     261.39     147.01       251.82     144.63     245.00     137.79	f = 100.0 m	Ε	177.8	100.0		100.0	177.8	f = 100.0 mm	f = 177.8 mm
32.38       18.21       35.78       20.12         38.91       21.89       43.00       24.19         45.96       25.85       50.79       28.15         53.63       30.16       59.26       33.33         61.62       34.66       68.09       38.30         70.08       39.42       77.45       43.56         70.08       39.42       77.45       43.56         79.02       44.44       87.32       49.11         88.40       49.72       97.69       54.94         98.24       55.25       108.56       61.06         108.55       67.11       131.86       67.46         119.32       67.11       131.86       67.46         119.32       67.11       131.86       67.46         119.32       67.11       131.86       74.16         143.21       79.97       157.13       88.38         166.93       93.88       184.47       103.75         166.93       93.88       184.47       103.75         193.38       108.76       229.10       128.86         221.70       124.69       2245.00       137.79         246.56       144.61 <td>24.98</td> <td></td> <td>14.05</td> <td>26.33</td> <td>14.81</td> <td>29.99</td> <td>16.37</td> <td>39.54</td> <td>22.24</td>	24.98		14.05	26.33	14.81	29.99	16.37	39.54	22.24
38.91       21.89       43.00       24.19         45.96       25.85       50.79       28.57         53.63       30.16       59.26       33.33         61.62       34.66       68.09       38.30         70.08       39.42       77.45       43.56         70.02       44.44       87.32       49.11         88.40       49.72       97.69       54.94         98.24       55.25       108.56       61.06         108.55       67.11       131.86       74.16         119.32       67.11       131.86       74.16         119.32       67.11       131.86       74.16         130.53       73.42       144.25       81.13         142.19       79.7       157.13       88.38         156.93       184.47       103.75         166.93       101.20       198.85       111.84         193.38       101.20       198.85       111.84         193.38       108.76       229.10       128.85         221.70       124.69       229.10       128.85         221.70       124.69       245.00       137.79         251.82       147.01       25	30.71		17.27	32,38	18.21	35.78	20.12	48.62	27.34
45.96       25.85       50.79       28.57         53.63       30.16       59.26       33.33         61.62       34.66       68.09       38.30         70.08       34.44       44.45       43.56         79.02       44.44       87.32       49.11         88.40       49.72       97.69       54.94         98.24       55.25       108.56       61.06         108.55       61.05       119.95       67.46         119.32       67.11       131.86       74.16         130.53       73.42       144.25       81.31         142.19       79.97       144.25       81.31         142.19       79.97       157.13       88.38         166.93       101.20       198.85       111.84         179.44       101.20       198.85       111.84         193.38       104.47       103.75         207.32       116.60       229.10       128.88         221.70       124.69       245.00       137.79         286.54       141.63       229.10       137.79         281.82       141.63       229.10       137.79         281.86       147.01       <	36.91		20.76	38,91	21.89	43.00	24.19	58.43	32.86
53.63       30.16       59.26       33.33         61.62       34.66       68.09       38.30         70.08       39.42       77.45       49.11         88.40       49.72       97.69       54.94         98.24       55.25       108.56       61.06         108.55       61.05       119.95       67.46         119.32       67.11       131.86       74.16         130.53       73.42       144.25       81.13         142.19       79.34       144.25       81.13         16.93       93.88       184.47       103.75         16.93       93.88       184.47       103.75         16.93       101.20       198.85       111.84         179.94       101.20       198.85       111.84         193.38       106.76       229.10       128.85         207.32       116.60       229.10       128.85         236.54       147.01       228.85       147.01         251.82       141.63       229.10       137.79         267.56       150.48       229.67       166.30         283.75       156.51       266.51         283.75       158.94	43.60		24.52	45.96	25.85	50.79	28.57	69.02	38.82
61.62 34.66 68.09 38.30 70.08 39.42 77.45 43.56 70.08 39.42 77.45 43.56 70.08 39.44 87.32 49.11 88.40 49.72 97.69 54.94 98.24 55.25 108.56 61.06 119.32 67.11 131.86 67.46 119.32 67.11 131.86 113 142.19 79.97 157.13 88.38 154.32 86.80 170.54 95.92 166.93 93.88 184.47 103.75 179.94 101.20 198.85 111.84 193.38 116.60 229.10 128.85 221.70 124.69 245.00 137.79 236.54 133.04 261.39 147.01 251.82 141.63 229.67 166.30 251.82 141.63 229.67 166.30 250.37 168.94 331.93 186.69 317.44 178.54 350.79 197.30	50.86		28.61	53,63	30.16	59.26	33,33	80.52	45.29
70.08       39.42       77.45       43.56         79.02       44.44       87.32       49.11         88.40       49.72       97.69       54.94         98.24       55.25       108.56       61.06         108.55       61.05       119.95       67.46         119.32       67.11       131.86       67.46         119.32       67.11       131.86       74.16         130.53       73.42       144.25       81.13         144.21       79.97       157.13       88.38         154.32       86.80       170.54       95.92         166.93       93.88       184.47       103.75         166.93       93.88       184.47       103.75         193.38       101.20       198.85       111.84         193.38       108.76       229.10       120.19         221.70       124.69       245.00       137.79         236.54       133.04       261.39       147.01         251.82       141.63       278.28       156.51         267.56       156.30       295.67       166.30         283.75       168.94       313.93       186.96         317.44	58.45		32.87	61,62	34.66	68.09	38.30	92.52	52.04
42.25         79.02         44,44         87.32         49.11           47.16         88.40         49.72         97.69         54.94           57.41         98.24         55.25         108.56         61.06           57.90         108.55         67.11         131.86         61.06           62.65         119.32         67.11         131.86         74.16           69.63         130.53         73.42         144.25         81.13           75.85         142.19         79.97         157.13         88.38           82.33         142.19         79.97         157.13         88.38           82.53         142.19         79.97         157.13         88.38           82.33         142.19         79.97         157.13         88.38           82.34         142.23         86.80         198.38         111.84           103.16         193.38         101.20         198.85         111.84           110.59         221.70         124.69         245.00         137.79           118.27         221.70         124.69         245.00         137.79           126.18         267.56         150.48         251.20         166.30 </td <td>66.47</td> <td></td> <td>37,39</td> <td>70.08</td> <td>39.42</td> <td>77.45</td> <td>43.56</td> <td>105.23</td> <td>59.18</td>	66.47		37,39	70.08	39.42	77.45	43.56	105.23	59.18
47.16         88.40         49.72         97.69         54.94           52.41         98.24         55.25         108.56         61.06           57.90         108.55         61.05         119.95         67.46           62.65         119.32         61.05         119.95         67.46           62.65         119.32         67.11         131.86         74.16           69.63         130.53         73.42         144.25         81.13           75.85         142.19         79.97         157.13         88.38           82.33         154.32         86.80         170.54         95.92           89.05         166.93         93.88         184.47         103.75           95.99         179.94         101.20         198.85         111.84           103.16         198.76         213.70         120.19           110.59         207.32         116.60         229.10         128.88           118.27         221.70         124.69         245.00         137.79           126.18         251.82         141.63         278.28         156.51           142.73         267.56         150.48         295.67         166.30	74.95		42.25	79.02	44.44	87,32	49.11	118.65	66.73
52.41         98.24         55.25         108.56         61.06           57.90         108.55         61.05         119.95         67.46           62.65         119.32         61.05         119.95         67.46           62.65         119.32         67.11         131.86         74.16           69.63         130.53         73.42         144.25         81.13           75.85         142.19         79.97         157.13         88.38           82.33         154.32         86.80         170.54         95.92           89.05         166.93         93.88         184.47         103.75           95.99         179.94         101.20         198.85         111.84           103.16         193.38         108.76         213.70         120.19           110.59         207.32         116.60         229.10         128.85           118.27         221.70         124.69         245.00         137.79           126.18         251.82         141.63         278.28         156.51           142.73         267.56         150.48         295.67         166.30           160.24         300.37         168.94         313.93         167.79	83.85		47.16	88.40	49.72	69.76	54.94	132.74	74.66
57.90         108.55         61.05         119.95         67.46           62.65         119.32         67.11         131.86         74.16           69.63         130.53         73.42         144.25         81.13           75.85         130.53         73.42         144.25         81.13           82.33         154.32         86.80         170.54         95.92           89.05         166.93         93.88         184.47         103.75           95.99         179.94         100.20         198.85         111.84           103.16         193.38         108.76         223.70         120.19           110.59         221.70         124.69         245.00         137.79           126.18         236.54         133.04         261.39         147.01           134.34         251.82         141.63         278.28         156.51           142.73         267.56         150.48         295.67         166.30           160.24         300.37         168.94         331.93         186.96           169.34         317.44         178.54         350.79         197.30	93.18		52,41	98.24	55.25	108.56	61.06	147.51	82.96
62.65         119.32         67.11         131.86         74.16           69.63         130.53         73.42         144.25         81.13           7.85         130.53         73.42         144.25         81.13           82.33         144.25         81.13         88.38           82.33         154.32         86.80         170.54         95.92           89.05         166.93         93.88         184.47         103.75           95.99         179.94         101.20         198.85         111.84           103.16         193.38         108.76         223.70         120.19           110.59         221.70         124.69         245.00         137.79           126.18         236.54         133.04         261.39         147.01           134.34         251.82         141.63         278.28         156.51           142.73         267.56         150.48         295.67         166.30           160.24         300.37         168.94         313.56         176.36           169.34         317.44         178.54         350.79         197.30	102,95		57.90	108.55	61.05	119.95	67.46	162.98	91.67
69.63         130.53         73.42         144.25         81.13           75.85         142.19         79.97         157.13         88.38           82.33         154.32         86.80         170.54         95.92           89.05         166.93         93.88         184.47         103.75           95.99         179.94         101.20         198.85         110.3           103.16         193.38         108.76         229.10         128.85           110.59         207.32         116.60         229.10         128.85           118.27         221.70         124.69         245.00         137.79           126.18         236.54         133.04         261.39         147.01           134.34         251.82         141.63         278.28         156.51           142.73         267.56         150.48         295.67         166.30           150.24         300.37         168.94         313.56         176.36           160.24         317.44         178.54         350.79         197.30	113.18		62.65	119,32	67.11	131.85	74.16	179.17	100.77
75.85         142.19         79.97         157.13         88.38           82.33         154.32         86.80         170.54         95.92           89.05         166.93         93.88         184.47         103.75           95.99         179.94         101.20         198.85         111.84           103.16         193.38         108.76         213.70         120.19           110.59         207.32         116.60         229.10         128.85           118.27         221.70         124.69         245.00         137.79           126.18         236.54         133.04         261.39         147.01           134.34         251.82         141.63         278.28         156.51           142.73         267.56         150.48         295.67         166.30           151.37         283.75         168.94         313.93         186.69           160.24         300.37         168.94         313.93         186.69           169.34         317.44         178.54         350.79         197.30	123.81		69.63	130.53	73.42	144.25	81.13	196.00	110.24
82.33 154.32 86.80 170.54 95.92 89.05 166.93 93.88 184.47 103.75 95.99 179.94 101.20 198.85 111.84 103.16 193.38 108.76 229.10 128.85 116.60 229.10 128.85 118.27 221.70 124.69 245.00 137.79 126.18 251.82 141.63 278.28 156.51 142.73 257.56 150.48 295.67 166.30 151.37 283.75 168.94 331.93 186.69 169.34 317.44 178.54 350.79 197.30	134.87		75.85	142.19	79.97	157.13	88.38	213.51	120.08
89.05     166.93     93.88     184.47     103.75       95.99     179.94     101.20     198.85     111.84       103.16     193.38     108.76     213.70     120.19       110.59     207.32     116.60     229.10     128.85       118.27     236.54     133.04     261.39     147.01       126.18     251.82     141.63     278.28     156.51       142.73     257.56     150.48     295.67     166.30       151.37     283.75     168.94     331.93     186.69       160.24     300.37     178.54     350.79     197.30	146.38		82.33	154.32	86.80	170.54	95.92	231.72	130.33
95.99 179.94 101.20 198.85 111.84 103.16 193.38 108.76 213.70 120.19 120.19 120.19 110.59 207.32 116.60 229.10 128.85 118.27 221.70 124.69 245.00 137.79 126.18 251.82 141.63 275.00 137.79 142.73 257.56 150.48 295.67 166.30 151.37 287.59 150.34 313.56 150.24 317.44 178.54 350.79 197.30	158.33		89.05	166.93	93.88	184.47	103.75	250,65	140.97
103.16     193.38     108.76     213.70     120.19       110.59     207.32     116.60     229.10     128.85       118.27     221.70     124.69     245.00     137.79       126.18     236.54     133.04     261.39     147.01       134.34     251.82     141.63     229.28     156.51       142.73     267.56     150.48     295.67     166.30       151.37     283.75     168.94     331.93     186.69       160.24     300.37     168.94     331.93     186.69       169.34     317.44     178.54     350.79     197.30	170.67		95.99	179.94	101.20	198.85	111.84	270.18	151.96
110.59     207.32     116.60     229.10     128.85       118.27     221.70     124.69     245.00     137.79       126.18     236.54     133.04     261.39     147.01       134.34     251.82     141.63     278.28     156.51       142.73     267.56     150.48     295.67     166.30       151.37     283.75     168.94     313.56     176.36       160.24     300.37     168.94     311.93     186.69       169.34     317.44     178.54     350.79     197.30	183.42		103.16	193.38	108.76	213.70	120.19	290.37	163.31
118.27     221.70     124,69     245.00     137.79       126.18     236.54     133.04     261.39     147.01       134.34     251.82     141.63     278.28     156.51       142.73     267.56     150.48     295.67     166.30       151.37     283.75     158.59     313.56     176.36       160.24     300.37     168.94     313.93     186.69       169.34     317.44     178.54     350.79     197.30	196.64		110.59	207.32	116.60	229.10	128.85	311.29	175.08
126.18     236.54     133.04     261.39     147.01       134.34     251.82     141.63     278.28     156.51       142.73     267.56     150.48     295.67     166.30       151.37     283.75     159.59     131.56     176.36       160.24     300.37     168.94     31.93     186.69       169.34     317.44     178.54     350.79     197.30	210.28		118.27	221.70	124.69	245.00	137.79	332.89	187.23
134,34     251.82     141.63     278.28     156.51       142,73     267.56     150,48     295.67     166.30       151,37     283.75     159.59     313.56     176.36       160,24     300,37     168.94     331.93     186.69       169,34     317.44     178.54     350.79     197.30	224,35		126.18	236.54	133.04	261.39	147.01	355.17	199.76
142.73     267.56     150.48     295.67     166.30       151.37     283.75     159.59     313.56     176.36       160.24     300.37     168.94     331.93     186.69       169.34     317.44     178.54     350.79     197.30	238,85		134.34	251.82	141.63	278.28	156.51	378.12	212.67
151.37 283.75 159.59 313.56 176.36 160.24 300.37 168.94 331.93 186.69 169.34 317.44 178.54 350.79 197.30	253.73		142.73	267.56	150,48	295.67	166.30	401.75	225.96
160.24 300.37 168.94 331.93 186.69 169.34 317.44 178.54 350.79 197.30	269.14		151.37	283.75	159.59	313.56	176.36	426.06	239,63
169.34 317.44 178.54 350.79 197.30	284.90	_	160.24	300.37	168.94	331.93	186.69	451.02	253.66
	301.09		169.34	317.44	178.54	350.79	197.30	476.65	268.08

for the WRD-6420 detector. Also, the change in sensitivity of the ROSA detectors at shorter wavelengths must be considered, which will require higher laser power levels for equivalent output signals.

3. Trade-Offs For Position Of Input Transparency. Although the optical configuration shown in figure 4 is most commonly used in OPS systems, there is another configuration of potential value. In this configuration, the grating transparency normal to the optical axis is placed behind the transform lens, as shown in figure 45 (a), for the grating positions 2 and 3 instead of at the conventional position 1, Goodman<sup>5</sup> discusses this configuration as involving diffraction of the converging cone of rays in the object plane that is detected and explained in the focal plane by Fresnel diffraction. An interesting aspect of this arrangement is that the aperture function transform, as indicated by figure 45 (b), remains the same, no matter where the transparency is placed between the transform lens and the detector and even though the diameter of the physical sampling aperture decreases by a ratio of d/f. This aspect is due to the constant  $f^{\#}$  of the optical system. Moving the transparency behind the transform lens does however change the scale of the spectra in proportion to d/f. In figure 45 (c), the first two harmonics of a Ronchi grating spectrum are shown. Now consider this grating to be placed at one of the indicated positions in figure 45 (a). The physical location of the harmonics in the focal plane space is scaled according to

$$u = \frac{w}{\lambda f} - \frac{d}{f} \tag{46}$$

Thus in figure 45 (d, e, f), we see the size of the spectrum on the detector decreasing as the transparency is moved closer to the detector. Also, the amplitude in the converging cone of incident light will be more intense by K' = K f/d as the physical sampling aperture becomes smaller. This is also indicated in figure 45 (d, e, f).

Trade-offs associated with this approach involve using smaller physical sampling apertures, with some flexibility of making adjustments or changing selections versus the complexity of maintaining multiple sets of decision criteria if the frequency plane scaling flexibility is exercised. Graphically it can be seen from figure 45 that S/N should decrease when figure 45 (b) is convolved with the spectra of figure 45 (e and f)

<sup>&</sup>lt;sup>5</sup>J. W. Goodman, Introduction To Fourier Optics, McGraw-Hill Book Company, San Francisco, CA, 1968.

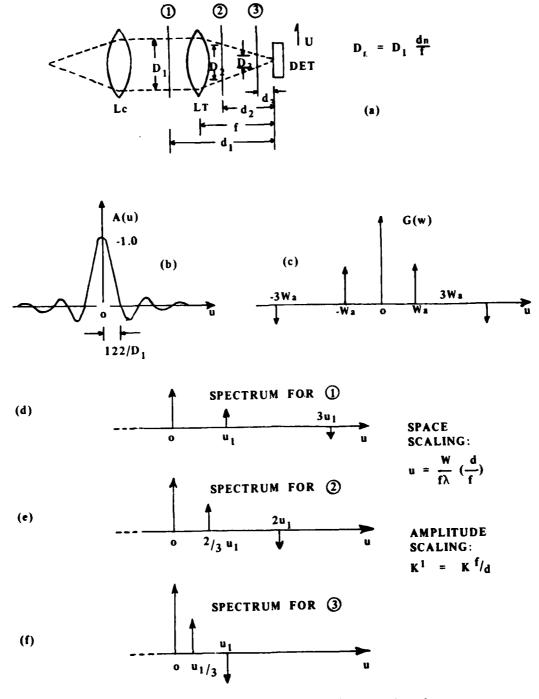


FIGURE 45. Gratings Placed Before and After Transform Lenses.

for the transparency positions 2 and 3, which should not be considered a generalization until further investigated. Another possible limitation of this approach involves aberrations in the detector plane introduced by placing the transparency in the converging beam of light. The major aberation will be spherical aberration, and it should increase in severity as d/f becomes smaller.

Additionally, the wavelength trade-offs discussed in the previous section can be coupled with those of this section to provide additional flexibility if desired.

### VI. FABRICATION OF GRATING MAPS

In the previous chapter, the preliminary optical subsystem design and trade-off considerations for grating map systems were outlined. We saw that the system depended upon the grating map fabrication capability. In this chapter, we look at the technology for producing grating maps and complete the preliminary system design discussion. Then, approaches for extending capabilities to produce gratings with increased storage capacity will be outlined.

A. Fabrication Requirements. • For our purposes, a grating map is an optical transparency with factor map information encoded by Ronchi gratings at selected spatial frequencies and directions. Producing a grating map requires a capability to transform factor map codings into codings that can be used to produce the required gratings. For each class of data on the factor map, a unique Ronchi grating should be generated in terms of spatial frequency and direction. Figure 46 indicates conceptually how a grating map could be produced. Here the factor map at the upper left is transformed to a grating map at the lower right by a technique that essentially involves spatial masking with a seperate grating for each factor map data class. In addition to the grating map, there must be an associated legend indicating the correspondence between the gratings and the factor map data classes. Also, a need exists for a capability to register automatically the transparency in the optical system, e.g. reference marks permitting automatic registration of the grating map in the optical system.

Although the grating map could be produced by cutting masks, it would be impractical because (1) it is labor intensive and (2) it would require a photographic reduction capability to achieve a micrographic image for mass storage.

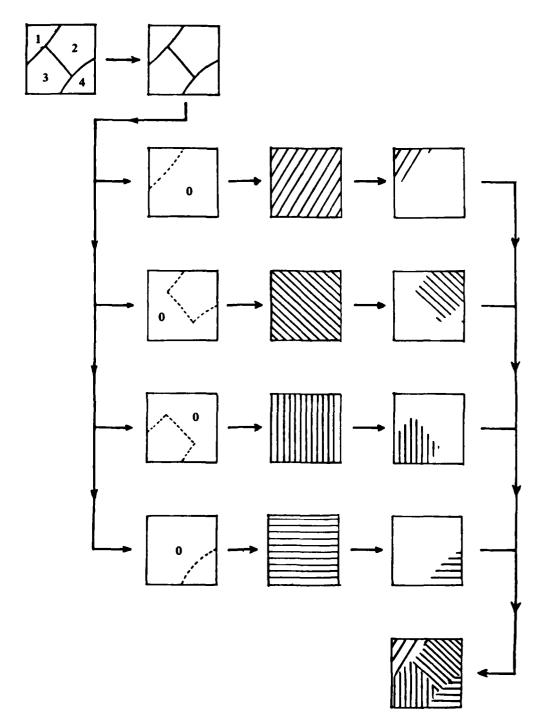


FIGURE 46. Generating the Grating Map.

A more practical approach would be to use a digital computer to program a modulated light scanning system that would write the gratings at the desired scale. We will assume the digital system can be programed to accept factor map boundary data from a factor map and to generate a signal for driving the light modulator and scanner in synchronism. Two modes of scanning are available: vector scan and raster scan. The vector mode requires a random access capability, but provides faster, simpler and better performing grating recording capability; whereas, the raster mode is strictly sequential, but produces severe limitations on the signal processing and writing speeds.

Table 23 lists important parameters for grating map recorders. We will briefly review these parameters.

Printing Spot -- The size and shape of the printing spot on the recording medium will largely determine the resolution of the system. In general, the intensity profile of the printing spot will be Gaussian and not be a perfect square pulse. When the beam shape departs from an optimum, it is often necessary to provide a pixel overlap. The effective beam size and shape is mainly determined by the apertures in the system, which act as spatial filters.

Geometric Precision – Geometric distortions of many types plague scanning printers. Deviations from orthogonality of the X and Y scanning axes cause distortions in the output image. The point-to-point accuracy of the scanner across the format determines the geometric precision of the scanner and should be on the order of 0.1 of the pixel size. Rescan error is important when two images are superimposed, and line start jitter can differentially displace scan lines in raster scan systems.

Radiometric Precision – The minimum intensity of the scanning system determines the minimum density, or fog level, of the image. This parameter becomes particularily important where the rate of change of intensity to distance is large. For example, if a grating with a spatial frequency approaching that associated with the spot size is to be written in the raster mode where the scan direction is transverse to the grating, the rate of change of the intensity level will determine the grating modulation at that frequency. If the signal changes from 'full on' to 'full off' in one pixel distance, the digital-to-analog converters and the following electronics are "strained." The bandwidth of the system is defined by the rate of change of the signal rather than the pulse width. The radiometric errors should not exceed one-half of the least significant bit of the image data.

Writing Speed ~ The throughput time or writing speed to produce an image from start to stop has been reduced significantly during the past several years, often at the expense of geometric and radiometric fidelity.

### TABLE 23. Parameters For Grating Recorders.

Printing Spot Size Shape Pixel overlap

Geometric Precision
Orthogonality of axes
Point-to-point accuracy
Rescan error
Line start jitter

Radiometric Precision
Minimum intensity
Rate of change of signal level
Radiometric error

Writing Speed

Operation and Maintenance Operability Maintainability Reliability Operation and Maintainence – In addition to being reliable, systems must be simple to operate and maintain.

B. The State of Technology. • Table 24 contains a partial list of several technologies for producing Ronchi grating transparencies, including examples of available equipment. The completeness of the descriptive statements in terms of the parameters of table 23 illustrate the diversity and nonuniformity of the specifications with which manufacturers describe their equipment.

Although the equipment listed in table 24 was developed to generate hardcopy images from a computer, two listed systems appear to have the specifications necessary to make grating maps. The two systems are Electron Beam Recorder (EBR), produced by Image Graphics Inc., and the Cathode Ray Tube (CRT) system, produced by Information International Inc. Both systems have raster- and vector-scan modes. The high resolution EBR produces line widths from 3 to 90  $\mu$ m (micrometers) by dithering a 3- $\mu$ m printing spot around any of 32,768 x 32,768 addressable points, and the CRT system adjusts spot size from 3.6 to 19.6  $\mu$ m for vector scanning. Both systems have recording speed, format size, and geometric fidelity advantages over the other systems.

Without available test data, a question arises of how precisely either system could produce a Ronchi grating for a selected spatial frequency within their operational range. For example, an ideal Ronchi grating will have sharp discontinuities in its optical density profiles; whereas, gratings produced by Gaussian-scanned printing spots will have smoother transitions, and the result will be a degraded Ronchi grating. The severity of degradation is dependent upon the beam profile. The effect of this degradation is to produce even and odd harmonics in the grating spectrum, which will decrease the S/N of the detected gratings. However, a limited testing program for generating gratings at a few selected spatial frequencies would resolve these questions.

C. Further Discussion of System Design Trade-Offs. • For this preliminary report, we assume that the above EBR and CRT systems will produce useful gratings. What then can we say about the optical system for detection of these gratings and how many data classes can we expect to encode and decode with these systems? Although it will be a continuation of the discussions of design trade-offs (see section 5B), this section will be concerned only with the EBR fabrication system.

TABLE 24. Examples of Grating Recording Systems.

# ELECTRON BEAM RECORDER

shades, optical density of 0 to 2.3, geometrical fidelity 0.03%, repeatability of sequential images 0.003%, 35 mm to 5.5 inch image formats, variety of films for recording. (Image Graphics Inc. produces twelve selectable from 6 um to 250 um with standard electron gun or 3 um to 90 um with high resolution electron gun, 125,000 points/sec plotting rate in vector mode, raster scan rates variable up to 2 KHz, dynamic range 64 gray Image Graphics, Inc., Model Cartographic EBR, 3 um spot diameter, 32,768 x 32,768 addressable points, vector and raster plotting, vector mode line width versions of the EBR with the major differences between units being the size of film and resolution.)

### CATHODE RAY TUBE

- Dicomed, Model D-46 Digital Image Recorder, 2048 x 2048 spots on 70 mm format, raster plot only, 64 intensity levels.
- Dicomed, Model D-47 Color Digital Image Recorder, 2048 x 2048 pixels, 20 um spot diameter, 70 mm format, records on Ektrachrome Type 6115 film, 3 filters, exposure range 2.0 D, point spacing linearity 0.25%. .
- spot size 10 um, number of addressable points  $16,384 \times 16,384$ , plotting area 79.4 mm x 79.4 mm, accuracy  $\pm$  0.5%, 32 intensity levels, line generation Calcomp Inc, Model 1670 Graphic COM Recorder, random address and vector generation, rate 5 msec.
- ಭ Information International Inc., Model PFR-4, spot size programmable from 3.6 um 19.6 um,  $64,000 \times 64,000$  addressable points, 7.5 cm x 7.5 cm display, linearity 0.05%, 512 intensity levels, 0 to 3.15 density range, computer corrections for distortions, writing speed 400,000 points/sec.

# TABLE 24. Continued.

### DRUM PLOTTER

Optronics, Model P-1500 Photowrite, sampling spots 12.5, 25, 50, 100, or 200 um, density range 2.5D, 64 gray levels, light emitting diode light source, positional accuracy 2 um, maximum data rate 60 KHz.

### FLAT-BED PLOTTER

- Optronics, Model S-3200 Specwrite, Raster plotter, rasters 1, 5, 10, 25, 50, and 100 um, density 0 to 2.5, 64 gray levels, positional accuracy 1 um/5 cm, Maximum data rate 2.5 Kpoints/sec.
- Perkin-Elmer Corp., Model 1010, LED light source for black and white images has 2 to 500 um spot size while color system uses CRT and filters with resolution of 5 to 50 lp.mm, 1024 gray levels, X and Y stage travel 25 cm, X and Y repeatability 1 um. ρ.

## LASER RECORDER

- Goodyear Aerospace Corp., Laser Recording System, 40 1/pmm, density dynamic range 0.2 to 2.4, 20 Mbit/sec data rate, geometric fidelity ± 0.05%, sheet or roll film up to 9.5 inches.
  - CBS, Model Laser Image Processing System, spot size 10, 20, or 40 um, resolution 37.5, 19.8, or 9.4 lp/mm, film chip size 70 x 160 mm, 4096 x 4096 pixels, grey levels 256, 0 to 2.56 density, write time for 1024 x 1024 pixels is nine minutes. ф.

# LASER PHOTO FACSIMILE

Harris Corp. Model Laser Photo, Resolution 256 samples/inch, dynamic range 0.1 to 1.75, data rates 1 minute/picture (8.5 x 11 inches).

The minimum spatial frequency grating generated by the EBR system with a line width of 90 µm is 5.5 Line-pairs per millimeter (LP/mm) and the maximum spatial frequency grating generated with a 3-µm-line width is 166.7 1/mm. From this information, we want to determine the best system for the parameters of sampling aperture diameter D, the focal length of the transform lens f, and the maximum number of detectable gratings corresponding to seperate combinations of rings and wedges of the ROSA detector. To assist this discussion, table 25 presents an example worksheet in selecting the grating detection system parameter velocity. In addition to restricting this design to the EBR gratings, we assume that a West to applying criteria. However, the approach is general, and other criteria could be recorded.

In Trial 1 of table 25, the objective is to good an initial estimate for the parameter values by computing f from equation (36), w<sub>min</sub> from equation (39), and D from equation (41). The result is a nonstandard value for f, and D was larger than specified. In Trial 2, a standarized value for f (6 inch: ) is given, the other values are computed. and a larger D value is obtained. In Trial 3, values for f and D are given and the value f# is found to be larger than desired. Reducing f to 100.0 mm, while keeping D = 0.10 mm in Trial 4, results in  $w_{max}$  at detector Ring 32 being much greater than the high spatial frequency EBR capability, and w<sub>m in</sub> for Ring 7 has a spatial period that violates equation (39). Next, table 2 is used to find the detector ring having a spatial frequency equal to or less than the EBR high spatial frequency capability, and Trial 5 indicates this to be Ring 25. Likewise, the lowest ring satisfying equation (39) is found to be Ring 9 from table 2. This solution yields a total of 17 rings and 32 wedges for encoding 544 unique gratings. The decoding system would have a focal length of 100.0 mm, and the sampling aperture would be 0.10 mm, as per the specifications. The trials that follow explore possibilities of improving the capabilities by employing different laser wavelengths. As shown in table 25, Trial 9 achieves a similar number of rings and wedges, but would require a higher powered HeCd laser because of the lower WRD-6420 sensitivity at  $\lambda = 0.3250 \text{ x} \cdot 10^{-3} \text{ mm}$ . Thus, with all trade-offs considered, Trial 5 appears to offer the best set of preliminary design values. A similar approach could be used to investigate the applicability of the WRD-6400 detector or an equal ring width detector if the intended application could support a detector development effort. Likewise, this approach could be used to design and/or assist in the selection of other viable systems from those listed in table 24.

TABLE 25. Example Worksheet for Selection of Grating Detection System Parameter Values.

FOR: EBR GRATING WITH MAX. FREQ. = 166.7 %=/mm AND MIN. FREQ. = 5.5 %=/mm MRD-6420 JETECTOR WITH  $R_{max}$  = 15.49 mm and  $R_{min}$  = 1.01 mm. = 0.6328 x  $10^{-3}$  mm UNLESS OTHERWISE STATED IN COMMENTS.

COMMENTS	NONSTD. f, D LARGER THAN DESIRED	D LARGER THAN DESIRED	f# LARGER THAN DESIRED	(E39) VIOLATED	ACCEPTABLE, 17 RINGS & 32 WEDGES	: = 0.5145 x 10 <sup>-3</sup> mm, ACCEPTABLE 15 RINGS & 32 WEDGES	. = 0.5145 x 10 <sup>-3</sup> mm, SUBOPTIMUM f <sup>-</sup> 22 RINGS & 32 WEDGES	. = 0.4880 x 10 <sup>-2</sup> mm. SUBCPTIMUM ** 21 RINGS & 32 WEDGE's	. = 0.3250 x 10 <sup>-3</sup> mm, ACCEPTABLE 17 RINGS & 32 WEDGE <sup>c</sup>	x = 0.4416 x 10 <sup>-3</sup> mm, ACCEPTABLE 16 RINGS & 32 WEDGES
f/D	1000(6)	636(E41)	1524(E41)	1000(E41)	z	813(E45)	1445(E45)	1371(E45)	931(E45)	1063(E45)
( mm )	0.146(E41)	0.238(E39)	0.100(6)	=	2	E	z	Ξ	=	=
Wim ( <sup>£</sup> o/mm)	17.02(E39)	10.52(E40)		20.31(£40)	30.01 $(12,R_3)$	24.98 (T22,R <sup>7</sup> )	24.52 (T22,R <sub>13</sub> )	25.82 (T22,R <sub>12</sub> )	27.34	$[L_1 = 2.41](E40)$ $[L_{R11} = 2.62](T2)$
M ( is / mm)	166.7(G)	160.6(E36)	160.6(36)	244.8(E36)	159.88 (T2,R;5)	158.33 (T22,R <sub>22</sub> )	160.24 (T22,R <sub>21</sub> )	159.59 (T22,R₃≎)	163.31	$[\mu = 11.221(E36)]$ $[\mu_{R,F} = 10.82](T2)$
f (mm)	146.86(36)	152.4(G)	152.4(6)	100.0(6)	:		177.8(6)	ž	=	152.4(G)
TRIAL		2	ю	4	æ	ø	7	∞	6	10

 $\overline{\text{KEY}}$ : (G) - GIVEN; (E36) - EQUATION 36 FROM TEXT: (T2,R<sub>2.5.</sub>) - TABLE 2, RING 25 FROM TEXT [ $\zeta$  = 11.22] = COMPUTED RADIAL DISTANCE, [ $\zeta$ <sub>2.6.</sub> = 10.82] - TABULAR RADIAL DISTANCE FOR RING-26.

- D. Extending The Storage Capacity of Grating Maps. The discussion of grating fabrication and the information storage capacity of a grating map would not be complete without advancing some concepts that improve the storage capacity if required. In the preceding section, we developed an example design showing that the EBR system may have the potential to encode Ronchi gratings at 17 spatial frequencies and 32 directions for a total of 544 thematic data classes for sampling with a 0.10 mm aperture. For centain classes of data, this number of data classes is more than sufficient, but suppose the need existed for producing grating maps with a larger set of data classes. This need might arise if contour maps are to be encoded for geographic areas having severe relief display problems. Another need for a large number of data classes might arise from a requirement to combine factor maps so as to keep the total number of graphics to a minimum. Nevertheless, these added capabilities will not be gained without paying some price. We will look at a few concepts for increasing capabilities and the price to be paid for the increase.
- 1. Amplitude Coding. All discussions have been concerned with binary Ronchi gratings in the form of optical transparencies, i.e. square wave gratings with maximum and minimum transmission values only. Table 24 indicates that the EBR can produce a modulated recording having 64 shades of grey over an optical density range of 0 to 2.3. Theoretically, this method should provide an encoding capability for 17 spatial frequencies, 32 directions, and 64 amplitudes equal to 17 x.32 x 64 = 34,816 separate data classes. In reality, little margin is left for noise associated with system variability. Also, at low grating amplitudes, very low level OPS signal detection problems will be experienced. Thus, it is reasonable to select a subset of the 64 grey levels, say 10 levels, which produce high S/N results similar to that associated with the binary gratings. Just 10 amplitude levels may provide an encoding capability for 3,481 data classes with the EBR. With only two levels, the storage capability of the binary gratings will be doubled.

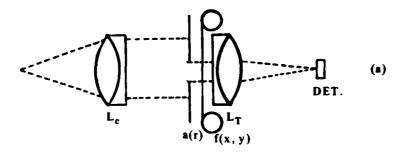
To obtain additional storage capacity in this manner will require a grating preparation capability that assures the desired uniformity. Also, the quality of the signal processing system must be such that the various signal levels can be unambiguously discriminated. For example, the laser light source must have a high degree of stability over short and long time periods. Thus, a simple laser for binary grating fabrication capability must be replaced by a stabilized laser when the multi-level gratings are employed. Similarly, the electronics must have temporal stability and perhaps more precision. The software for decoding the multi-level grating detection data increases in complexity and time required per decision as the number of grating amplitude levels increases.

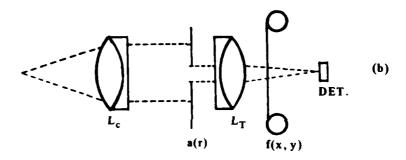
- 2. Multiple Gratings. Combinations of superimposed gratings, each of which is aligned so that their separate spectrums will not fall on the same detector wedge, provide another means for increasing storage capacity, however, this approach is not as simple or powerful as the amplitude codings. An analytic explanation of this approach will not be advanced here, but one can easily conceptualize that in addition to the separate spectra of the individual gratings, there will be interaction spectra that tend to cloud the S/N mental picture. This approach could cause additional complexity in decision-making software to determine whether superimposed gratings or separate contiguous gratings existed in the sampling aperture.
- 3. Color Gratings. Amplitude coding and multiple grating codes can be used with gratings prepared on color transparencies. Separate lasers or narrow band filtered light will be required to decode the color transparency data. Table 20 indicates a range of blue through red optical wavelengths available in common gas lasers. Although it would appear to be promising this approach must be tested.

### VII. SYSTEMS CONCEPTS

The previous two chapters indicated optical subsystem design and trade-off considerations for grating map systems, outlined the technology associated with grating map fabrication. In this chapter, we outline more general optical subsystem concepts and integrate these with the other subsystems, i.e. the electronic, the digital, and the storage and retrieval subsystems, to present a more unified view of the major system features. An example system is then described in some detail to illustrate subsystem interrelations.

- A. Basic Subsystems. Important components of the optical, electronic, digital and storage and retrieval subsystems will be reviewed.
- 1. Optical subsystem. The major components of a standard OPS optical subsystem are as indicated in figure 4, and the preceding two chapters addressed their design considerations for OPS detection of grating maps. The basic optical configuration is duplicated in figure 47(a), where, along with figure 47(b and c), the different configurations for placing a transparency in a stationary light beam are indicated. The arrangement shown in figure 47(b) (which was given before in V, B, 3) and the single lens arrangement shown in figure 47(c) represents a further development that is simpler in concept, but will, in general, produce greater aberrations because of the severe requirements satisfied only by expensive lens systems. One- or two-dimensional sampling is





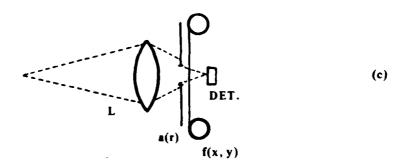
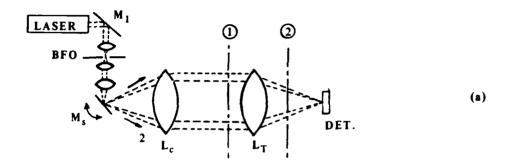


FIGURE 47. Optical Arrangements for Stationary Light Beam OPS Systems.

accomplished with these optical configurations by translating the sampling aperture a(r), or more preferably by translating the transparency, while the sampling aperture remains fixed and centered on the optical axis.

In general, stationary light beam OPS systems, which translate the transparency to obtain sample data over an area, provide excellent research systems, but as with the automated microdensitometers, these arrangements are usually too slow for operational applications. Faster OPS sampling systems can be realized by moving a telecentric sampling beam, i.e. a collimated beam parallel to the optical axis, over a stationary transparency. Two approaches will be outlined. The first approach, shown in figure 48(a and b) for one- and two-dimensional arrangements respectively, uses glass lenses and galvanometers to move and form a telecentric scanner, with samples in plane 1 and 2. Here we will briefly review the two-dimensional arrangement of figure 48(b). The beam-forming optics (BFO) are primarily responsible for producing a clean, collimated beam of a given diameter. This beam is focused at the center of rotation of a galvanometer mirror M<sub>s1</sub> and this spot is relayed by the relay optics (RO) to the center of rotation of a second galvanometer mirror M<sub>s2</sub>, which scans orthogonal to that of the first. Generally, the galvanometers are moved under computer control so that the sampling beam raster discretely scans the transparency, and a matrix of sample points are obtained; however, random access scanning can also be applied. These systems have their limitations in that galvanometer retrace time is significant, and the galvanometer resolution and accuracy must be exceptional to obtain an orthogonal N by N sample matrix with a high number of points and with a high reproducibility. Additionally if the input transparency is large, then the lenses must also be large and expensive.

The second approach for OPS sampling with scanning telecentric beams is illustrated in figure 49. Here, reflecting optics in the form of parabolic mirrors reflect the beams similar to the manner that lenses refract light. The arrangements in figure 49 are analogous to the three configurations using lenses in figure 47, and also to those in figure 48. In figure 49, the first parabolic mirror  $M_1$  focuses the collimated and sized beam onto a rotation multi-faceted mirror that reflects the beam to the first mirror, where it is collimated, diffracted by the transparency, as in (a). Parabolic mirror  $M_2$  then acts as a transforming element to form the diffraction pattern of the sampled transparency on the detector surface. The rotating mirror is usually driven by a stepping motor having a high number of resolvable steps per rotation T, which enables this approach to have the advantage in that it has no retrace time. Tilted facets on the rotating wheel provide the scanner with a two-dimensional raster capability, limited of course by the number of facets. Thus, this approach usually provides a better one-dimensional scanner with a motorized film drive mechanism giving the second and slower scan motion.



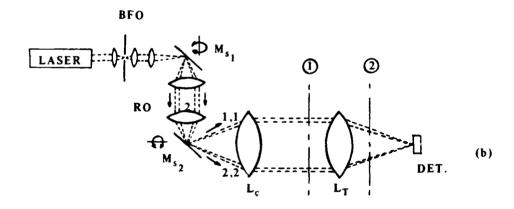


FIGURE 48. One- and Two-Dimensional Telecentric Beam-Scanning Arrangements Using Laser.

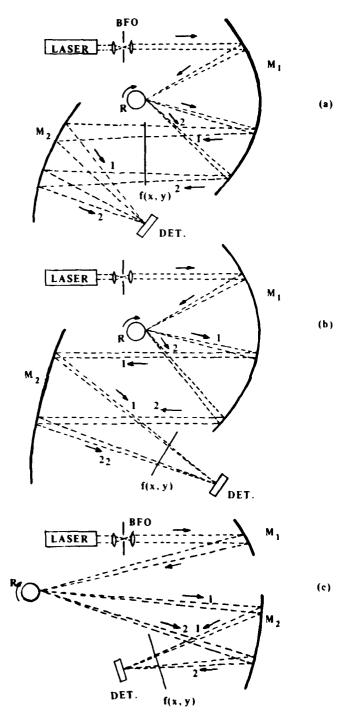


FIGURE 49. Optical Arrangements Using Parabolic Mirrors, Analogous to Figure 47 for Scanning Telecentric Beam.

2. Electronic Subsystem. For our purposes, we separate the electrical signal processing into electronic and digital subsystems arbitrarily, based upon whether the signal is analog or digital, respectively. Components of the electronic subsystem relate principally to the interface between the optical and digital subsystems. Analytical characterization of the ROSA optical and electronic processing is shown in figure 5. Here the detector changes the spatial light distribution in the spatial frequency plane to an ordered set of ele trical signals, one signal for each detector ring and wedge. These signals must then be amplified in a manner that preserves the nature of the signal. The signals can be sequentially amplified, or each signal can be amplified in parallel and then multiplexed as shown in figure 5. This is followed by an analog to digital (A/D) converter that quantizes the analog detector element signals into an ordered string of binary signals that are formatted for the digital computer system.

Interfacing an OPS detector with a digital computer system is not trivial because the signal has a potential dynamic range of 10<sup>6</sup> between the high level signal near d.c. and that in the high spatial frequency areas, which is near or within the noise level of the detector. The ROSA electronic system uses an autoranging second stage amplification that divides the signal into decades as described in Section 3.1 and more specifically in equation (10).

3. Digital Subsystem. The major component of the digital system is the digital computer. The computer serves as the heart and mind of the system in the sense that it directs and controls all operations within the system and makes classification decisions, which are reflected in the data or information that are output from the system. The subsystem does only what it is programed or hardwired to do; however, today's systems are sophisticated relative to digital machines of the not too distant past and they have significant capabilities. The digital subsystems can operate with today's minicomputers. Designs have flexibility and may choose to delegate selected processing, control, and decision-making responsibilities to lower-order microprocessors for one or more reasons.

Other components of the digital subsystem are the input/output devices used to communicate and interact with human operators.

4. Grating Map Storage and Retrieval Subsystem. A subsystem concerned with the storage and retrieval of the minified grating maps must provide not only a physical storage and retrieval capability but also an index of locations where grating maps are stored and must be returned to after use. This indexing function can be served by data base subsystems that are integral to the digital subsystem.

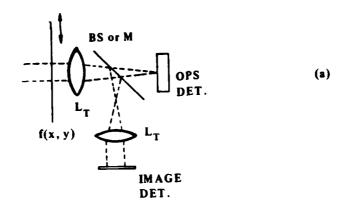
Automated and semi-automated components for physical storage and retrieval of large numbers of microfiche and smaller format transparencies are commercially available.

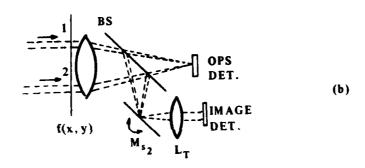
- B. Example System Concepts. The above discussion of basic subsystems will be supplemented with additional concepts for optical systems. This will be followed by a discussion of a simple system using minified grating maps, which will integrate subsystem concepts and show how the system is controlled and coordinated.
- 1. Additional Optical Subsystem Concepts. Previous discussions have emphasized the potential for an OPS detector in grating detection. Within automated systems context, it would often be convenient to be able to "see" the apertured portion of the input transparency sampled by the OPS detector, e.g. to aid in resolving boundaries between contiguous gratings within an OPS sampling aperture, to assist in registering the image and stage coordinates prior to sampling, or to help identify point and line data. An n x n photodiode array detector can be added to the OPS optical subsystems in figure 47(a) and figure 48(a and b) as shown in figure 50. The stationary beam optical subsystem in figure 50(a) is rather simple to implement, and the focal length of the inverse transform lens is chosen so that the sampled image fills the n x n photodiode array detector. In figure 50(b), a one-dimensional telecentric scanner may have a galvanometer scanner to direct properly the reconstructed image to the image detector, and in figure 50(c) the two-dimensional telecentric scanner requires two galvanometers. The corresponding galvanometer from figure 50(b and c) can be slaved to those of figure 48(a and b), respectively, to effect a simple coordinated scan.

Figure 51 indicates how multiple factor maps of the same geographic area may be sampled in a coordinated fashion. This is a simple extension of the system shown in figure 47(a).

Two example illustrations of how a spatial light modulator (SLM) may be used in an OPS system are shown in figures 52 and 53. Several types of SLM are currently under study at a number of laboratories for applications in coherent optical image processing systems. Casasent<sup>6</sup> presents a review of the technology. For the applications in these illustrations, an SLM such as the Itek Corporation Pockel's Readout Optical Modulator (PROM) device with record, read, and erase capabilities and properties of high dynamic range and analog image manipulation with bias adjustments can be used.

<sup>&</sup>lt;sup>6</sup>D. Casasent, "Spatial Light Modulators," Proc. IEEE, Vol. 65, No. 1, Jan 1977, pp. 143-157.





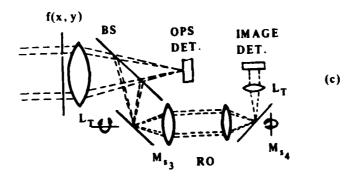
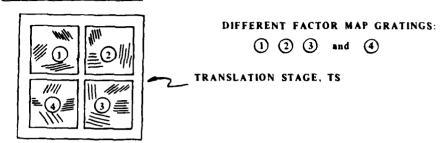
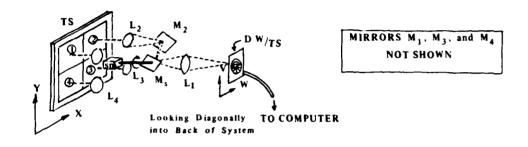
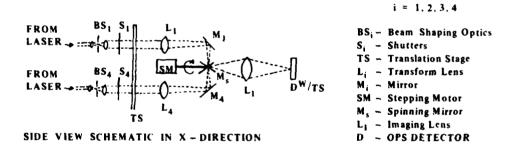


FIGURE 50. Addition of a Photodigde Array Detector to Enable "Seeing" of the Image Sampled by the OPS Detector.

### FACTOR MAP GRATINGS:







### **OPERATIONAL SEQUENCE:**

Grating to be sampled is selected by Computer (example, I), then Shutter  $S_1$  is opened and  $S_2$ ,  $S_3$ , and  $S_4$  are closed. Simultaneously, the stepping motor rotates Mirror  $M_s$  into position so that lens  $L_1$  can image the OPS from I onto the Detector, D. Detector D is mounted on a translation stage that is serve driven to center tag Detector on the optical axis and thus compensate for alignment errors in positioning the rotating Mirror,  $M_s$ .

The registered gratings are mounted on a translation stage which moves orthogonally so as to allow four sample beams to illuminate the same grating coordinates.

FIGURE 51. Concepts for Multiple-Coordinated Factor Map Gratings.

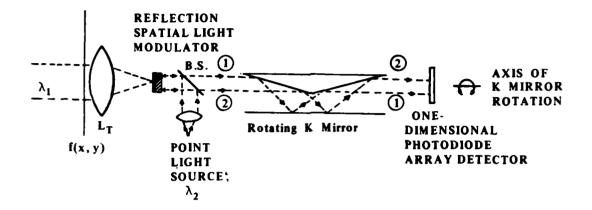


FIGURE 52. Example of an OPS Configuration Using a Spatial Light Modulator, a Rotating K Mirror, and a One-Dimensional Photodiode Array Detector.

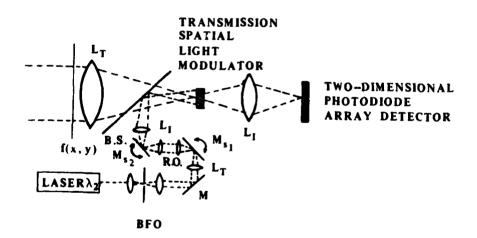


FIGURE 53. Example of an OPS Configuration Using a Spatial Light Modulator, a Two-Dimensional Scanner and a Two-Dimensional Photodiode Array Detector.

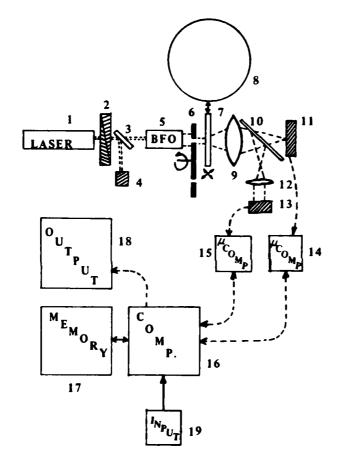
The example shown in figure 52 has an SLM that records the spectrum of the sampled portion of the transparency. The SLM is a reflection device with a dichroic filter on its face and is nearest to the transform lens. This filter passes the OPS record light of wavelength  $\lambda_1$ , while serving as a reflector for the collimated readout light  $\lambda_2$ . The light is doubly modulated image-wise by the OPS record during its two passes through the SLM crystal. A rotating K mirror serves to rotate the spectrum on a one-dimensional detector. Decision criteria associated with this system would determine the spatial radius and direction of the first harmonic of the grating being sampled. The K mirror rotates so as to keep the optical axis stationary, with the image rotating at twice the angular velocity as the prism.

For the example shown in figure 53, the OPS pattern is recorded in the SLM. By changing the electrical bias on the device, the positive pattern is changed to a negative pattern and thresholded. A scanning spot traces a high-resolution, two-dimensional raster over the SLM and light is transmitted through the device only above the negative threshold so that detection and identification of the grating direction and spatial frequency is rather simple with a two-dimensional photodiode array detector. In this illustration, a transmission SLM is shown, but a reflection SLM could be used by moving all components associated with the scanner to the opposite side of the SLM as in figure 52.

2. A Simple System Example. A simple automated system for machine readable factor maps is shown in figure 54. The purpose of this discussion is to indicate the coordination of the previously discussed components of an automated OPSA system and to present some additional concepts not developed earlier. We will first briefly review the system components and how they are coordinated, then we will present a scenario related to the possible use of such a system.

Most components of the optical subsystem in figure 54 have been discussed previously except for the variable optical density wedge (2) and laser intensity level detector (4), which may serve in combination to monitor and control the laser output by feedback through the computer. The rotatable disc with sampling apertures (6) also operates under computer control, as does the two-dimensional translation stage (7). The grating map storage and retrieval subsystem (8) is similar to a carousel that contains grating map transparencies with more than one grating map per transparency. This subsystem also has capability for loading and unloading the translation stage with transparencies under computer control.

Electronic subsystem components, except the detectors, have not been shown in figure 54 so as to keep the illustration simple and uncluttered. The two de-



### SYSTEM COMPONENTS

- 1. LASER
- Variable Optical Density Wedge
- 3. Beam Splitter
- 4. LASER Intensity
  Level Detector
- 5. Beam Forming Optics
- 6. Rotatable Disc with
- Sampling Apertures
  7. Grating Map Transparency
  on Two-Dimensional
  Translation Stage
- 8. Grating Map Storeage and Retrieval System
- 9. Transform Lens
- 10. Beam Splitter
- 11. OPS Detector
- 12. Inverse Transform Lens
- 13. Photodiode Array Detector
- 14. Micro-Computer for 11
- 15. Micro-Computer for 13
- 16. Mini-Computer
- 17. Memory Devices
- 18. Output Devices
- 19. Input Terminal

FIGURE 54. A Simple Automated OPSA System for Reading Optically Stored MGI Factor Maps.

tectors, similar to those in figure 50(a), are used for sampling the optical power spectrum with a ROSA detector (11) and a two-dimensional photodiode array detector (13) for sampling the input image.

A microcomputer (14 and 15) can be interfaced directly to each detector to improve system efficiency by removing processing, control, and decision tasks from the central computer. These microcomputers can be micro programed to accomplish the data acquisition and formatting temporary storage in local buffers, the low level data processing and decision-making, and the data transfer directly to memory via a DMA (direct memory access). The microcomputers are controlled by a central minicomputer (16) that serves to coordinate and control subsystem operations and to process data for internal use or to satisfy requirements placed in the system. The central computer controls the laser output level by periodically sampling the laser intensity level detector (4) signal after A/D electronic conversion (A/D converter not shown). The central computer then translates the variable optical density wedge via a solenoid or stepping motor to effect the desired light level input for the system. It also controls the movement of the two-dimensional translation stage (7), the rotatable disc with sampling apertures (6), and the grating map transparency storage and retrieval system (8). The central computer accepts a problem statement for a geographic area (19) and selects appropriate factor map transparencies with the aid of a data base management system and other collateral data in memory. The selected solution approach will dictate the geographic areas to be scanned, the sample spacing, and the sampling aperture diameter. The central computer then controls movement of the two-dimensional translation stages (7), the rotatable disc with sampling apertures (6), and the grating map transparency storage and retrieval system.

The spatial image detector is used to register the transparency in the stage coordinate system. The grating legend, stored in memory for the sampled transparency, provides information to decide grating spatial frequency and direction to obtain data classifications. These decisions are processed in MGI application programs and the results are output in readable form (18).

A short scenario of the manner in which the system of figure 54 may be used in a MGI application problem follows. The problem statement is presented to the system by an operator through the input station (19) by problem type with selected parameters defined, e.g. for a cross-country mobility problem, the parameters may be initial geographic location, final destination, type of vehicle, number of vehicles, etc. Application software then selects types of data desired and checks the data base to determine if these data types are available for the problem area.

Suppose this concerned MGI Terrain Factor Maps stored as Ronchi grating maps on transparencies is an automated storage and retrieval system as in figure 54. The computer system then controls retrieval of a selected factor map (transparency) from the storage carousel and inserts it into a holder on the two-dimensional translation stages. A short automated registration procedure is accomplished with the aid of the photo diode array detector to align the transparency coordinate system with the translation stage coordinate system. Now the stage coordinates can be computed to obtain the desired transparency sampling. Each time the stages are incremented to a new sampling location, the ROSA detector's microcomputer is directed to obtain a set of detector element samples. While the stage is translating to the next sample location, the sampled data can be decoded and only the factor map class symbol is stored temporarily in a buffer within the microcomputer. These processed data are then block transmitted to central memory via direct memory access when the buffer is full or the sampling completed. Other factor map data for the same area, e.g. soils, slopes, vegetation, etc., can oe processed in like manner. The central computer can then use these spatial data, along with temporal data, e.g. local weather history and projected weather, to compute or decide on the cross-country mobility data class for each sample location. Processed data can then be formatted and output on a monitor and/or plotter for inspection and/or distribution.

A somewhat similar program to the system in figure 54 is flow charted in figure 55. This simple example relates to only one of many possible ways in which an automated grating map storage and retrieval capability may be employed as a machine-readable MGI factor map mass store system. These concepts must now be tested and verified for correctness as well as completeness. The potentials at this preliminary stage are quite promising.

### VIII. SUMMARY

This report analysized optical power spectral (OPS) approaches to machinereadable factor maps for use in terrain information systems. The objective was to offer a more compact, simpler, and cheaper factor map data base storage and retrieval systems than would be available by all digital technology. The basic concept of the system involves use of OPSA for decoding data from reduced factor maps that have been encoded by spatial frequency and direction of Ronchi optical gratings.

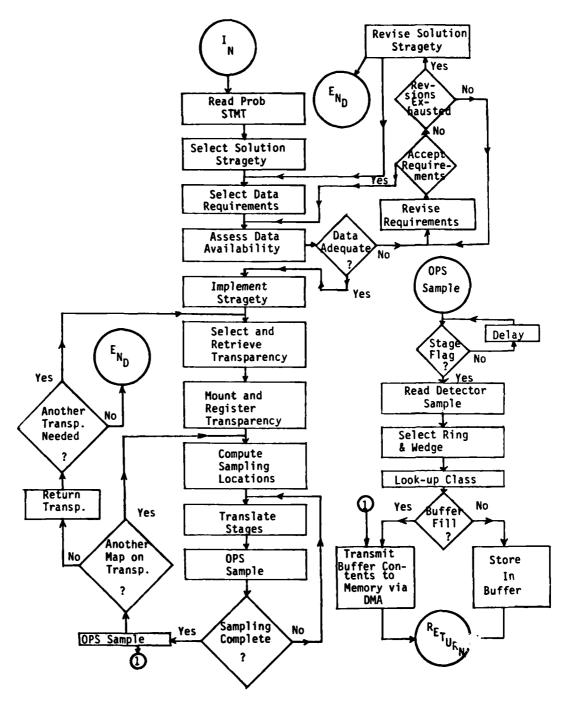


FIGURE 55. Program Associated With Automated OPSA System in Figure 54.

An OPSA system consists of a coherent optical sampling subsystem, an electronic detection and signal processing system, and a digital computer with associated software for control and decision-making. In Chapter III, an analytical characterization of an OPSA system was discussed when the input transparencies are ideal Ronchi optical gratings. Particular attention was given to characterizing the resultant optical signals from ROSA (Recording Optical Spectrum Analyzer) photodiode detectors having 32 concentric ring detectors on one semi-circle and 32 equally sized wedge detectors on the conjugate semi-circle. This result formed the basis for presentating a computer simulation program in the following chapter, along with simulation results from its use under a wide range of operational parameters with two commercially available ROSA detectors of slightly different detector element configuration. One detector had mid-radii of the ring elements spaced logrithmically, and the other detector had linear spacings. These simulation results indicated that as many as 27 rings and 32 wedges yield factor map encoding potentials for 864 thematic data classes (27 x 32) with detection signal-to-noise ratios greater than 1.0 when the f#, i.e. the ratio of the transform lens focal length to the sampling aperture diameter, is less than 1,000. These results motivated an attempt to redesign the ROSA detector element configuration to effect better performance. The detector redesigns with equal ring element spacings resulted in a capability of detecting 30 rings and 32 wedges, i.e. 960 thematic data classes, with a signal-to-noise ratio greater than 1.0.

Preliminary design of an optical subsystem for detection of grating maps is developed in Chapter V to indicate how the interaction of system parameters forces the designer to make trade-offs for realistic optical system specification. Here particular attention is given to sampling aperture diameter, which determines the resolution of factor map sampling. For example, a 22- by 29-inch factor map having a scale of 1:50,000 when reduced 10x will have a format size of 55.9 mm by 73.7 mm, which is suitable for commercial 70-mm chips or roll films, and a 0.1-mm-diameter sampling aperture will have an equivalent resolution of 50 meters on the ground. Trade-offs leading to smaller grating map formats are then investigated. Significant findings indicate that a 0.051-mm sampling aperture having approximately a 25-meter ground resolution can have the same signal-to-noise results as the 0.1 mm aperture with 50-meter ground resolution if the laser light wavelength is changed from the HeNe 0.6328 $\mu$ m to HeOd at 0.350 $\mu$ m.

In Chapter VI, the technology for producing grating maps is reviewed and approaches for extending capabilities to produce gratings with increased storage capacity are outlined. Two systems appear to have the specifications necessary for generating grating maps: the electron beam recorder made by Image Graphics Inc., and the cathode ray tube system available from Information International Inc. However, without test

data there is a question of how precisely either system could produce a Ronchi grating for a selected spatial frequency within their operational range. An example worksheet (table 25) is given to outline selection of the grating detection system parameter values, which indicates that the election beam recorder has a potential to encode Ronchi gratings at 17 selected spatial frequencies and 32 directions for a total of 544 thematic data classes. Means for increasing the number of thematic data classes are discussed for amplitude coding, e.g. with 10 gray scale levels for the Ronchi gratings the electron beam recorder could encode 3,481 separate thematic data classes in a single grating map. Likewise, multiple gratings composed of superimposed gratings or gratings prepared in color transparencies decoded by selected laser light wavelength illumination provide potential for increasing data capacity in a grating map.

In Chapter VII, concepts for the optical, electronic, digital, and storage and retrieval subsystems are described. For example, several optical subsystem configurations are described and illustrated for (1) stationary light beam optical subsystems with moving input transparencies and (2) a telecentric scanning beam optical subsystem with stationary input transparencies. It is shown that one-or two-dimensional telecentric scanning can be accomplished with either the standard refractive optics afforded by glass lenses or by reflective optics with parabolic mirrors. Integration of a photodiode array detector into an OPSA optical subsystem is presented to assist in registering image and stage coordinate systems as well as serving as a possible aid in resolving boundaries between contiguous gratings on an input grating map. It is shown how spatial light modulations, such as Itek's PROM device, might be used in OPSA systems.

Also in this Chapter, coordination of the various subsystems into an integrated automated system is described in an example scenario. This system features a carousel for storing the reduced factor map data encoded as Ronchi gratings. The simple system uses a minicomputer as a central processor to coordinate and control the various subsystem operations and to process data for internal use. Microcomputers are interfaced to an OPS detector and to an image plane photodiode array detector to increase system efficiency by removing processing, control, and decision tasks from the central computer. OPSA samples can be preprocessed and classified within the microprocessors, and the reduced class nemonic can be stored in local buffers until transmission to central system memory via direct memory access when the buffer is full. This system could be programed to operate in a true automated fashion by accepting formatted problem statements for a defined geographic area and for a defined problem for which an application algorithm exists, e.g. cross-country mobility between selected points for a given class of vehicles. The central computer could select the appropriate factor map transparencies, transfer them sequentially to the sampling system, register them in the sampling coordinate system, and select the areas of the transparencies to be sampled, the sample spacing, and sampling aperture size. The OPSA detector microcomputer could process sample data while the translation stage is moving to the next sample position. The central

computer could use these spatial data, along with temporal data, e.g. local weather history and projected weather, to compute or decide on a problem answer for each sample location. The processed data could then be formatted and displayed for human inspection or placed in a computer file for access for map overprinting by automated cartography systems.

### IX. CONCLUSIONS

This preliminary investigation of optical power spectral analysis approaches to machine-readable factor maps for use in terrain information systems has developed information and data indicating that the concepts are feasible. Experimental testing of the simulated system concepts can provide data useful for system design and implementation planning.

